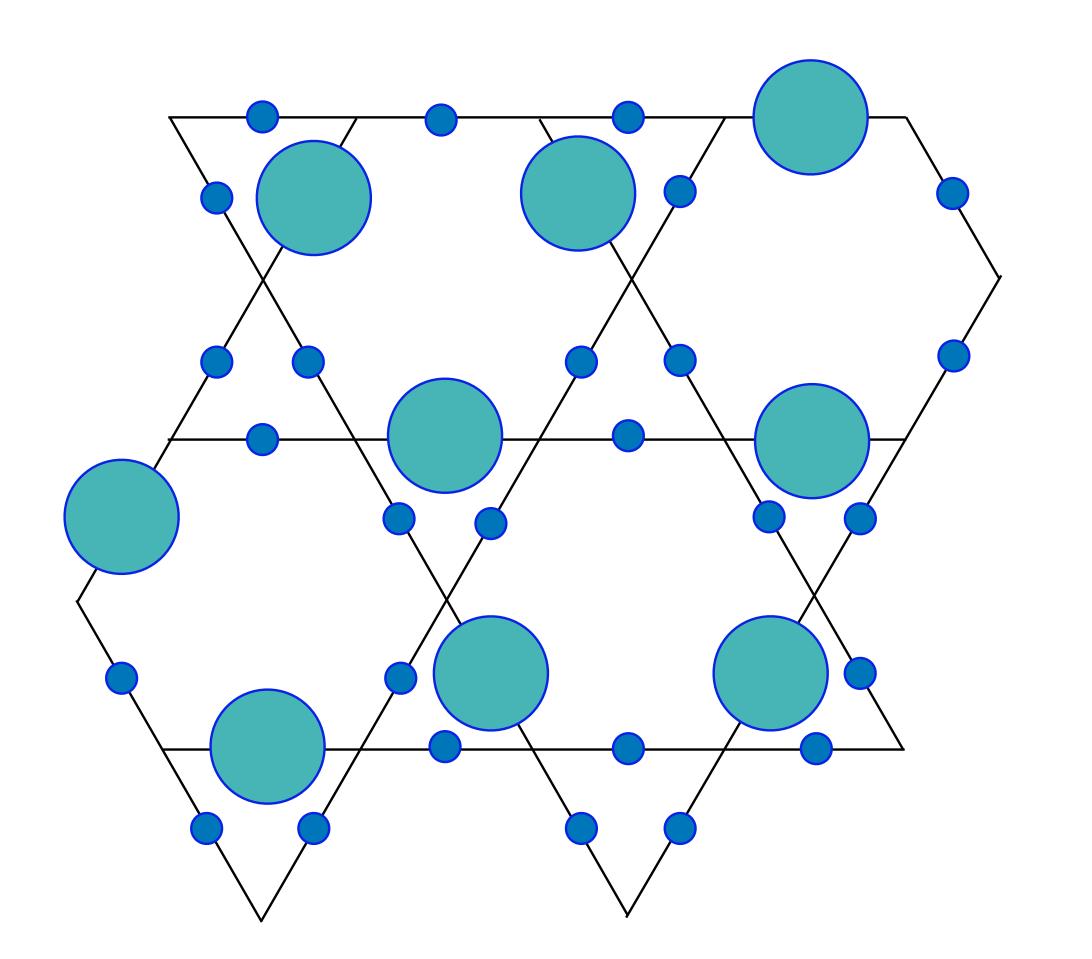
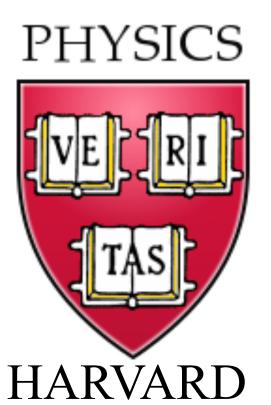
100 years of many-particle quantum mechanics: from Bose and Fermi to quantum materials and devices.



HUN-REN Wigner
Research Centre for Physics
Budapest
October 7, 2025

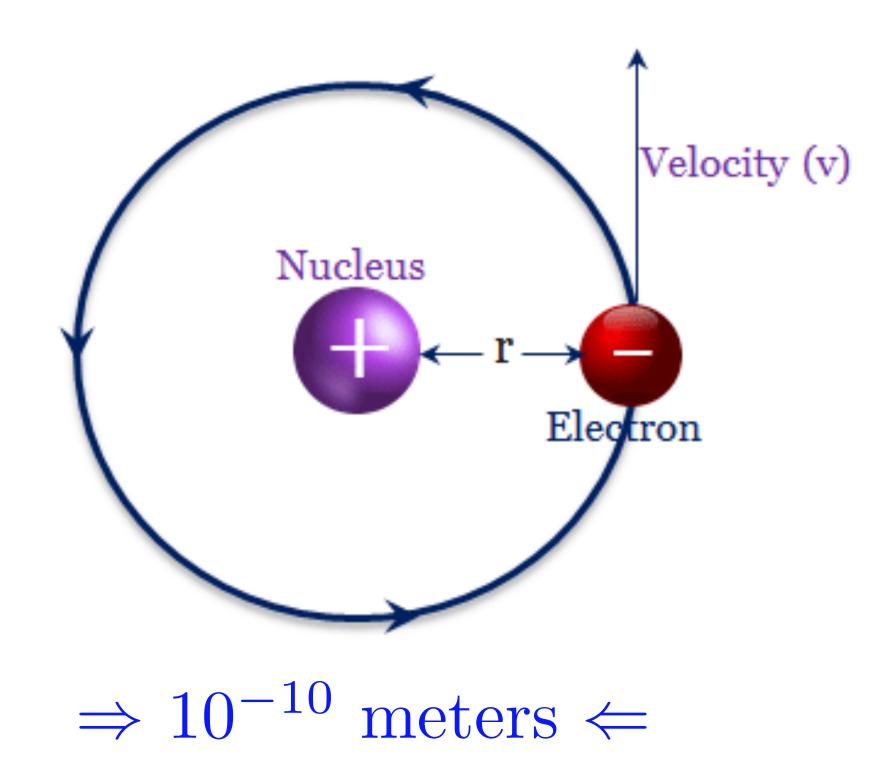
Subir Sachdev





Quantum mechanics 10 quantum materials: the first 100 years

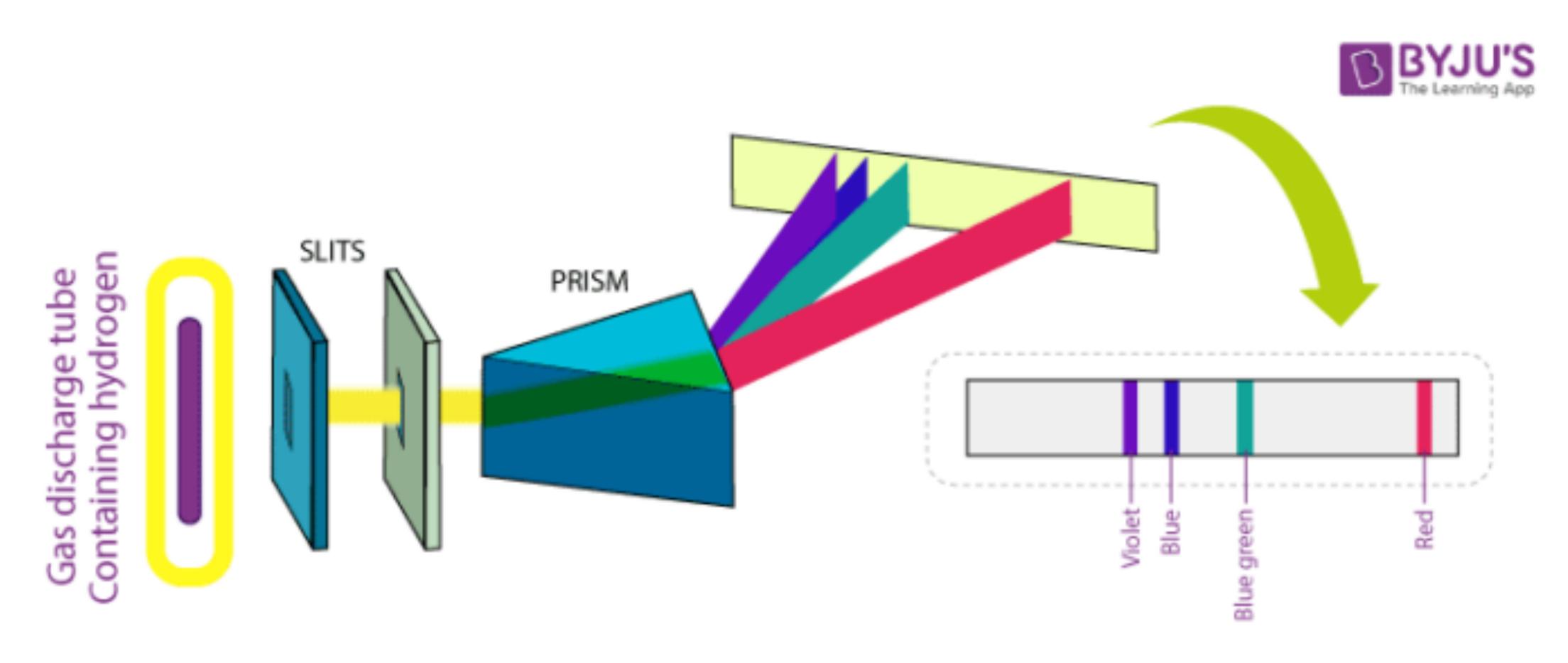
Hydrogen atom



The motion of the electron around the proton is *not* described by the same theory as the motion of the planets around the sun.

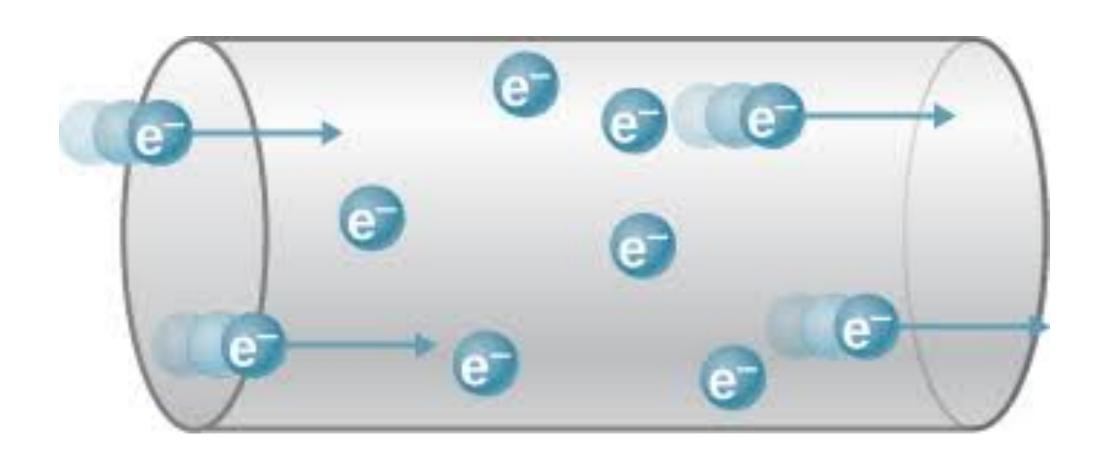
It is described by the quantum theory of Schrödinger and Heisenberg (1925).

• Schrödinger, Heisenberg (1925): Discovery of the equation obeyed by a single electron, replacing Newton's laws of motion. These equations precisely described the light emission spectrum of a single hydrogen atom.



Hydrogen emission spectrum

- Schrödinger, Heisenberg (1925): Discovery of the equation obeyed by a single electron, replacing Newton's laws of motion. These equations precisely described the light emission spectrum of a single hydrogen atom.
- Sommerfeld (1927): The same equations also describe the motion of $\sim 10^{23}$ electrons in a metal. Each electron is a **fermion**, named after Fermi (1926), which obey exclusion—at most one fermion can occupy each quantum orbital.



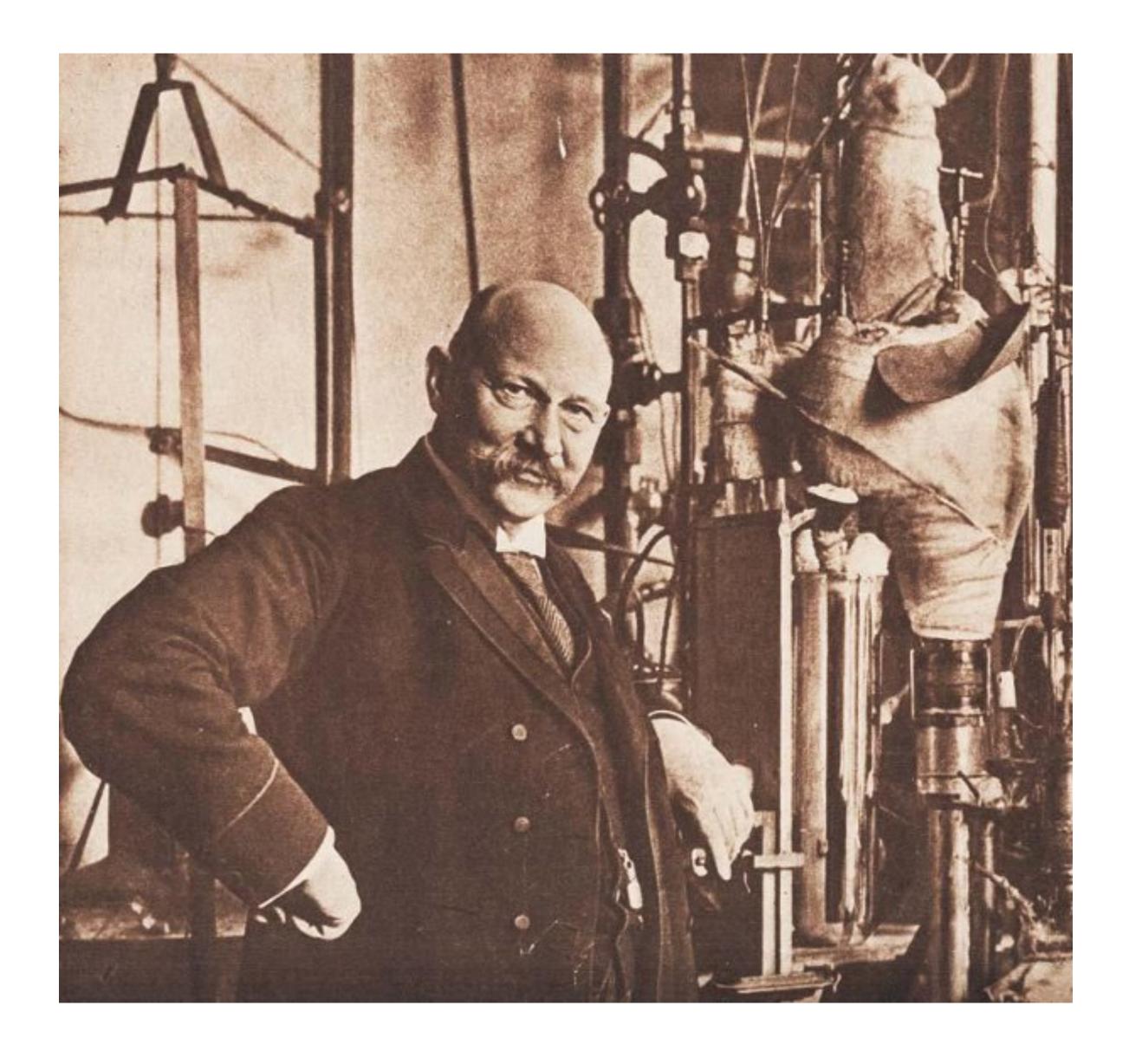
- Schrödinger, Heisenberg (1925): Discovery of the equation obeyed by a single electron, replacing Newton's laws of motion. These equations precisely described the light emission spectrum of a single hydrogen atom.
- Sommerfeld (1927): The same equations also describe the motion of $\sim 10^{23}$ electrons in a metal. Each electron is a **fermion**, named after Fermi (1926), which obey exclusion—at most one fermion can occupy each quantum orbital.
- Bose, Einstein (1924): Particles now known as **bosons**, which do not obey exclusion. Many bosons can condense into a single macroscopic quantum state, which is today understood to be the key to superfluidity and superconductivity.

- Schrödinger, Heisenberg (1925): Discovery of the equation obeyed by a single electron, replacing Newton's laws of motion. These equations precisely described the light emission spectrum of a single hydrogen atom.
- Sommerfeld (1927): The same equations also describe the motion of $\sim 10^{23}$ electrons in a metal. Each electron is a **fermion**, named after Fermi (1926), which obey exclusion—at most one fermion can occupy each quantum orbital.
- Bose, Einstein (1924): Particles now known as **bosons**, which do not obey exclusion. Many bosons can condense into a single macroscopic quantum state, which is today understood to be the key to superfluidity and superconductivity.
- Bardeen, Cooper, Schrieffer (1957): Pairs of electrons behave like **bosons**, and this is the explanation for superconductivity.

• Today: Many particles exhibit many emergent phenomena, related to quantum entanglement. These are crucial to understanding modern quantum materials, such as the high temperature superconductors.

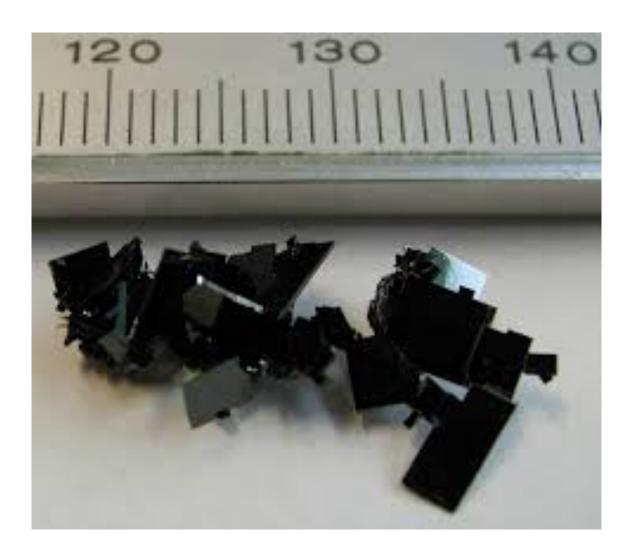
- Today: Many particles exhibit many emergent phenomena, related to quantum entanglement. These are crucial to understanding modern quantum materials, such as the high temperature superconductors.
- Ideas on multi-particle entanglement in quantum materials have strongly influenced quantum computing, especially quantum error correction (and vice versa).

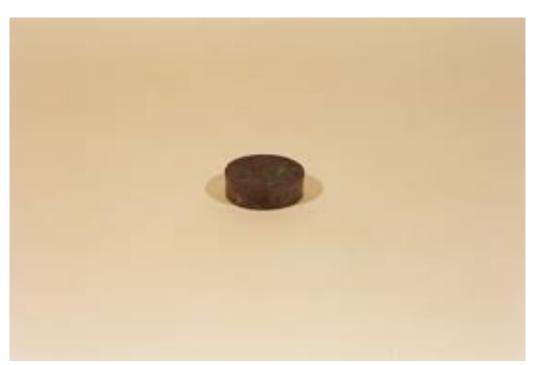
Superconductors

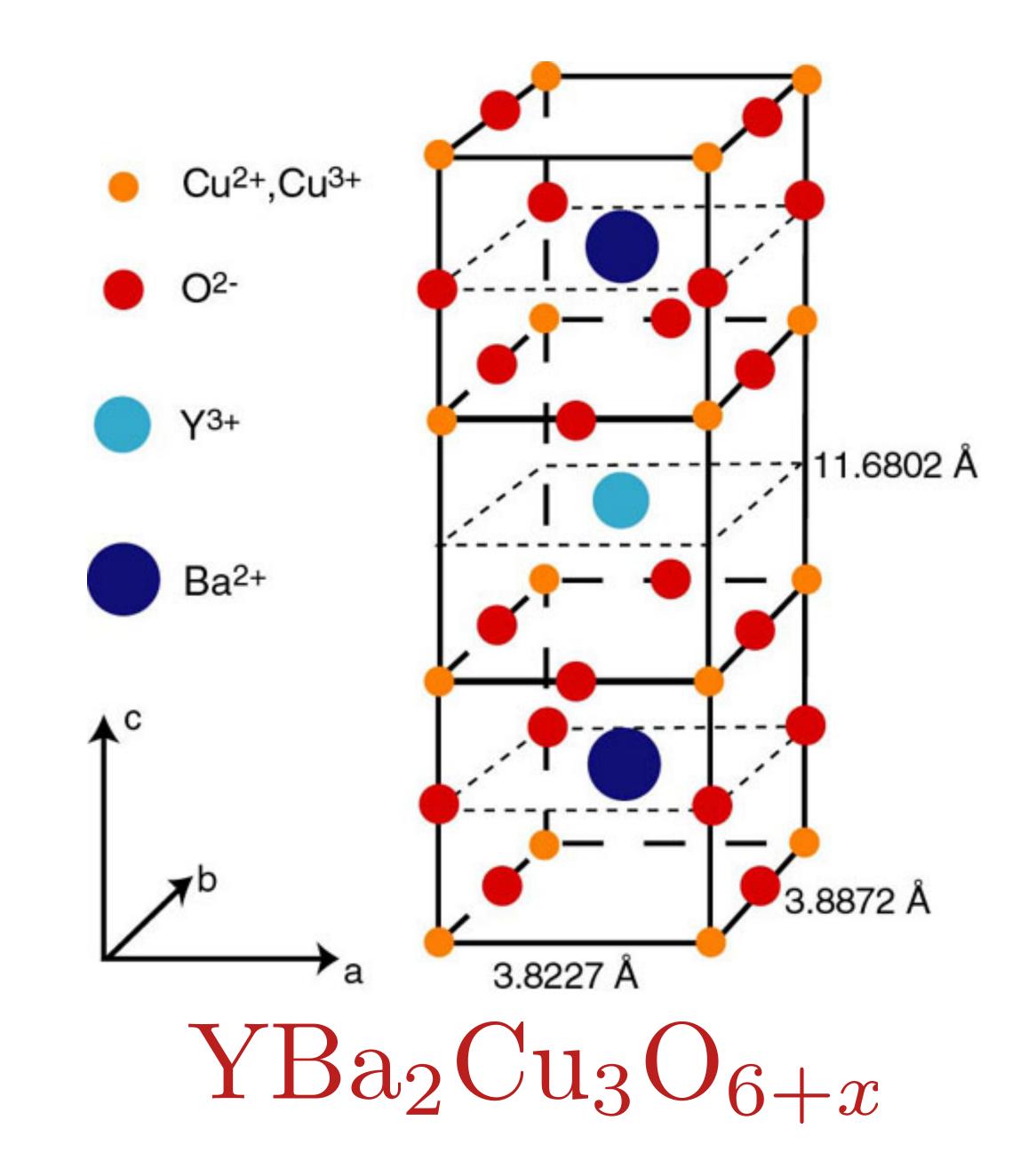


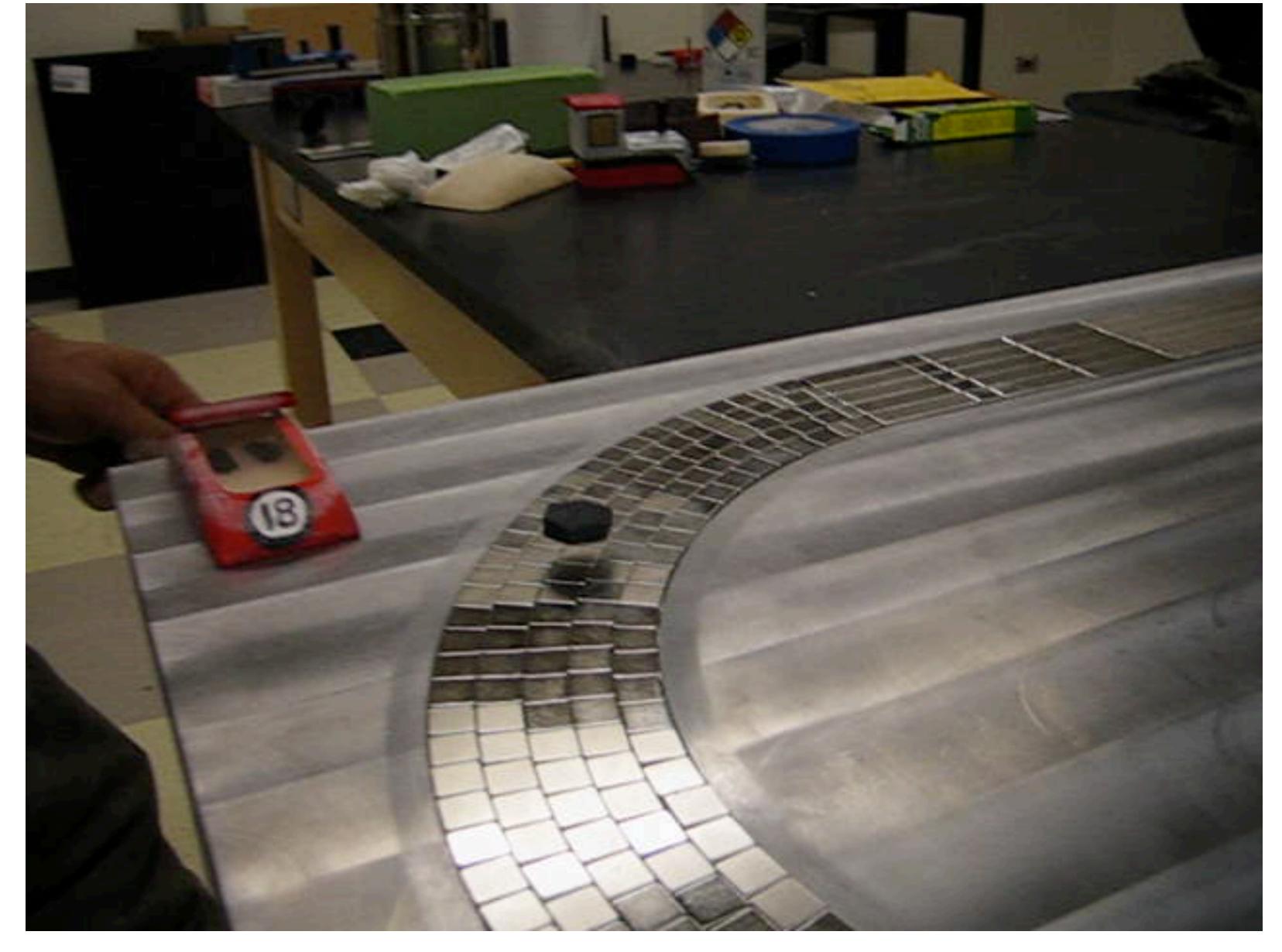
Kamerlingh Onnes 1911: Mercury is a superconductor below -269 $^{\circ}\mathrm{C}$

Cuprate high temperature superconductors







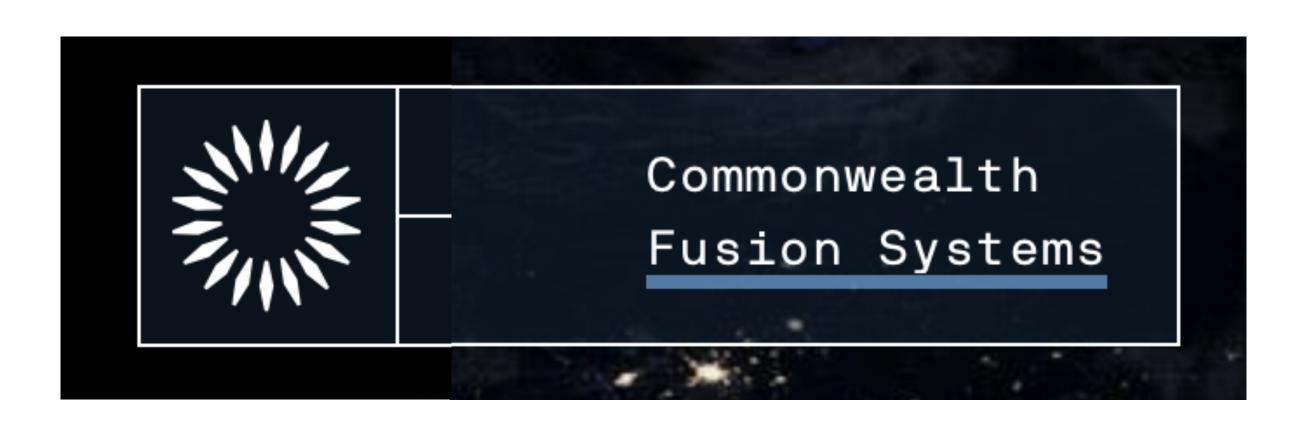


Nd-Fe-B magnets, YBaCuO superconductor

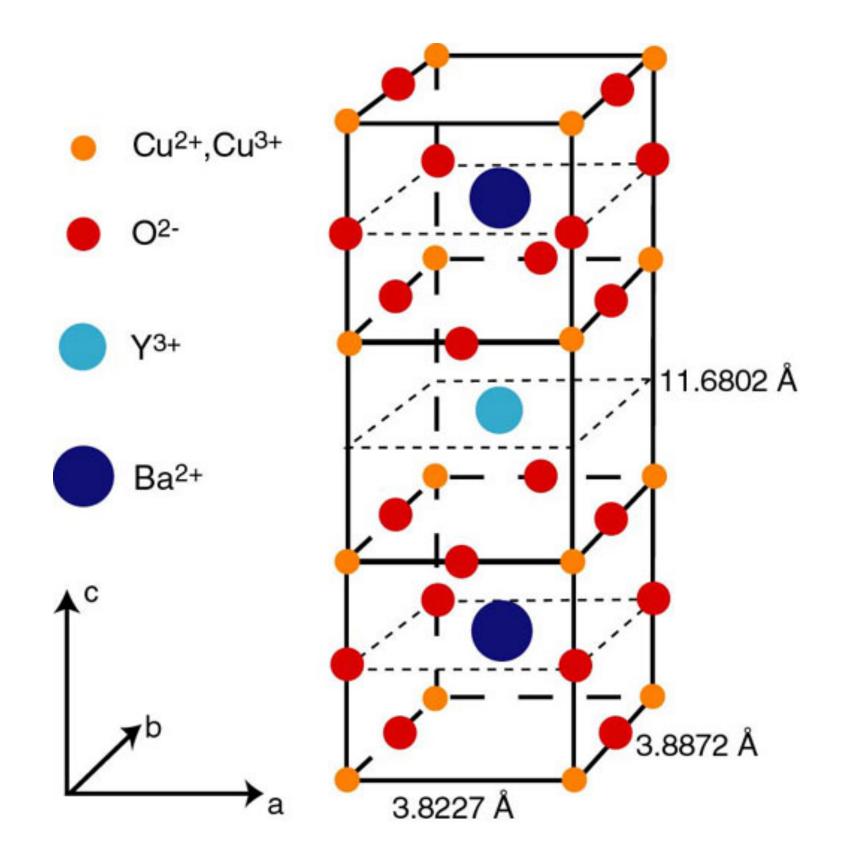
HTS Magnets: Enabling Technology

The surest path to limitless, clean, fusion energy

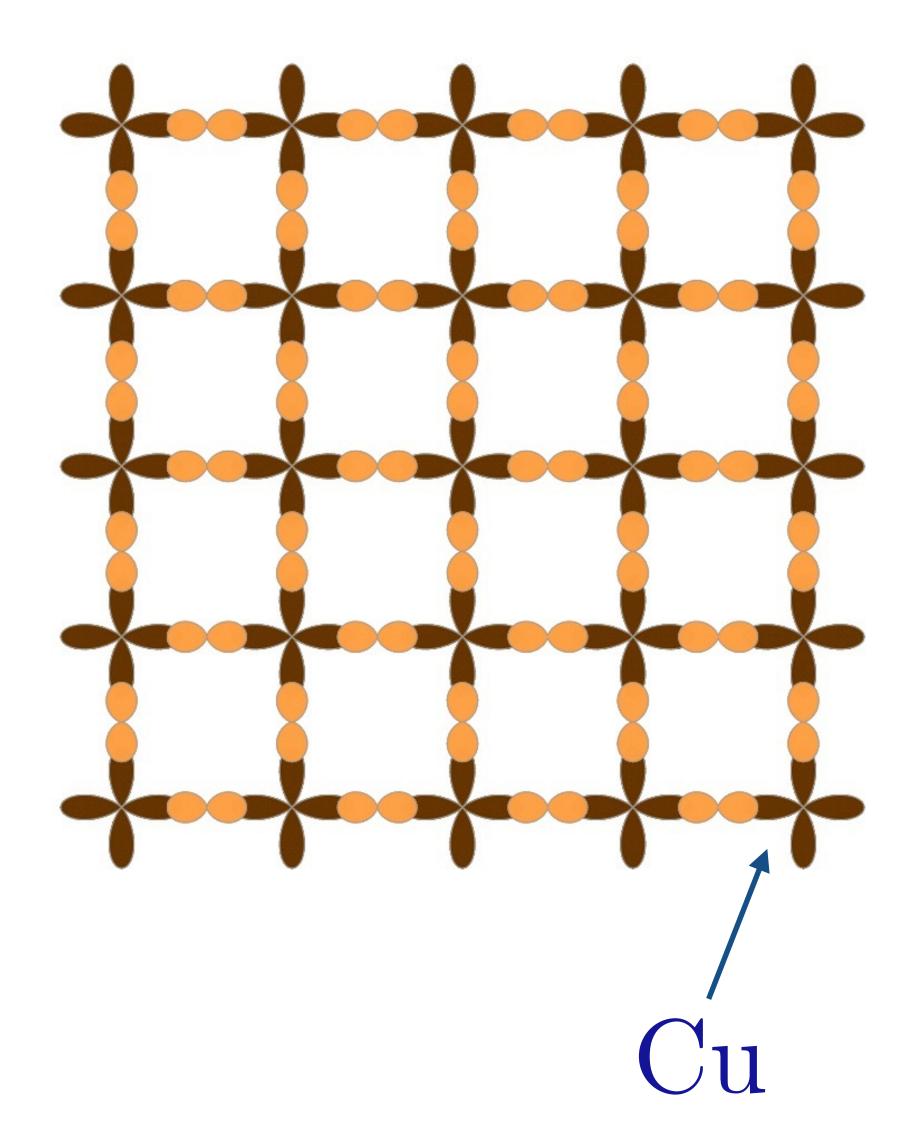
YBCO magnets allow for smaller, faster, and less expensive tokamaks for plasma fusion

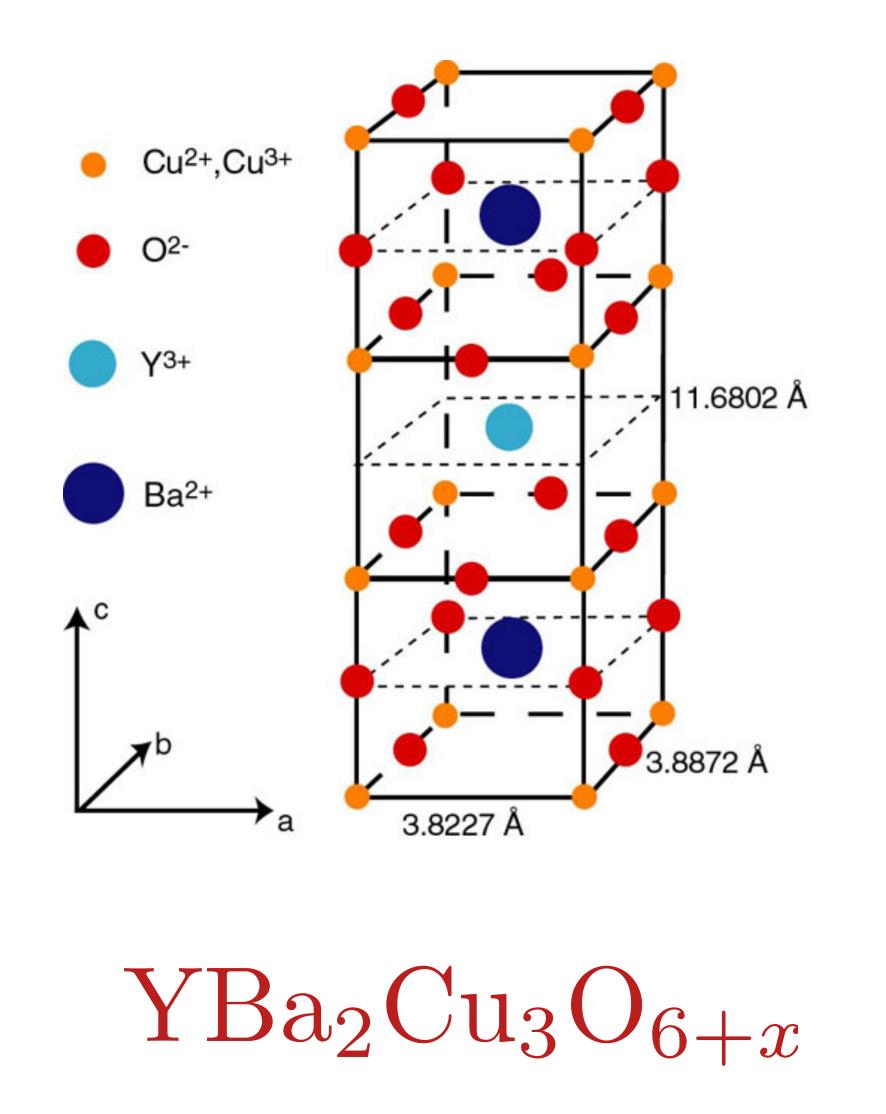


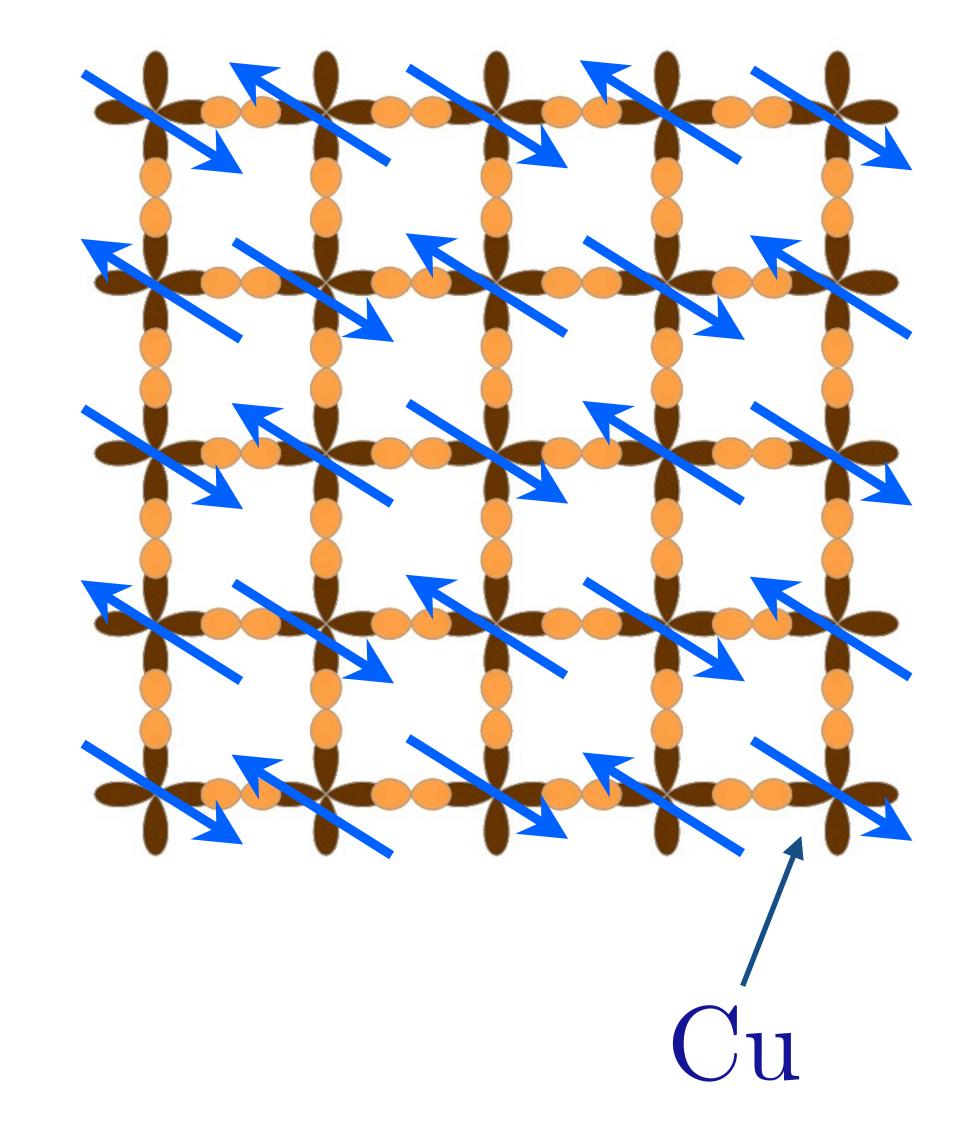




 $YBa_2Cu_3O_{6+x}$



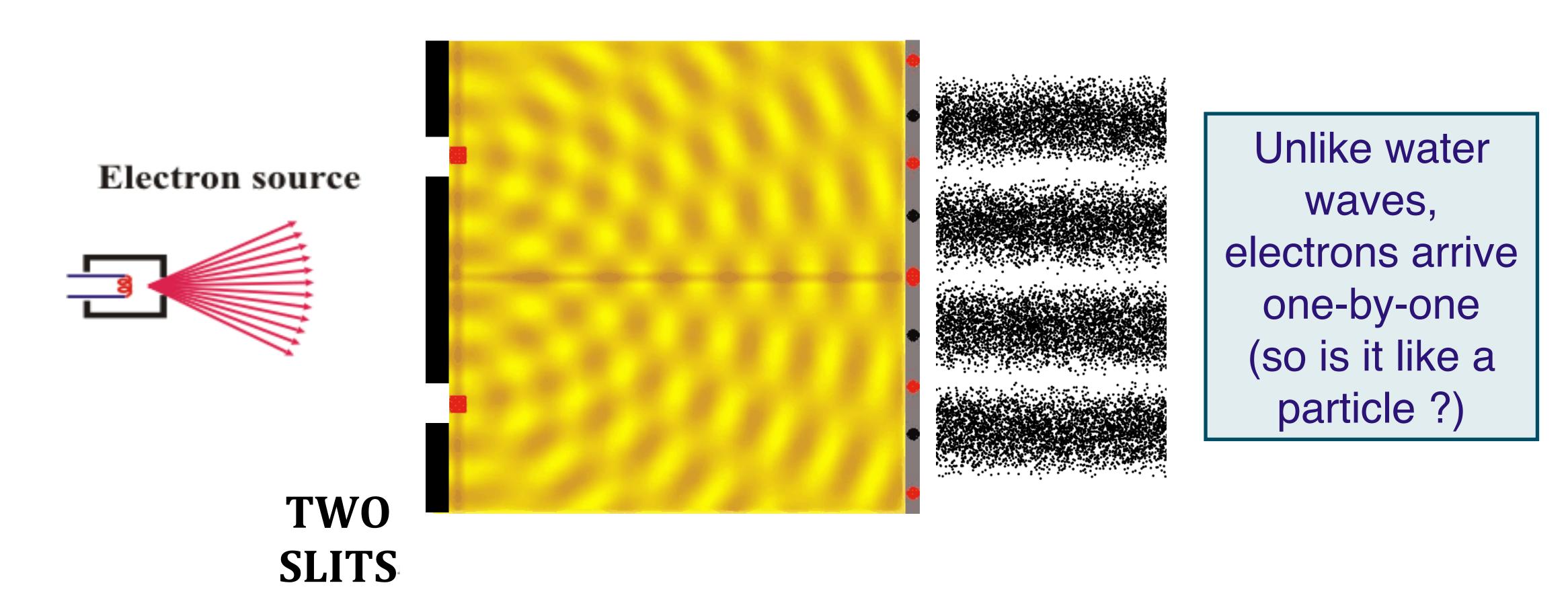




P.W. Anderson and G. Baskaran (1988): The key to high temperature superconductivity is the formation of a "resonating valence bond state" (a type of **quantum spin liquid**) which entangles the electrons on Cu

Principles of Quantum Mechanics: I. Quantum Superposition

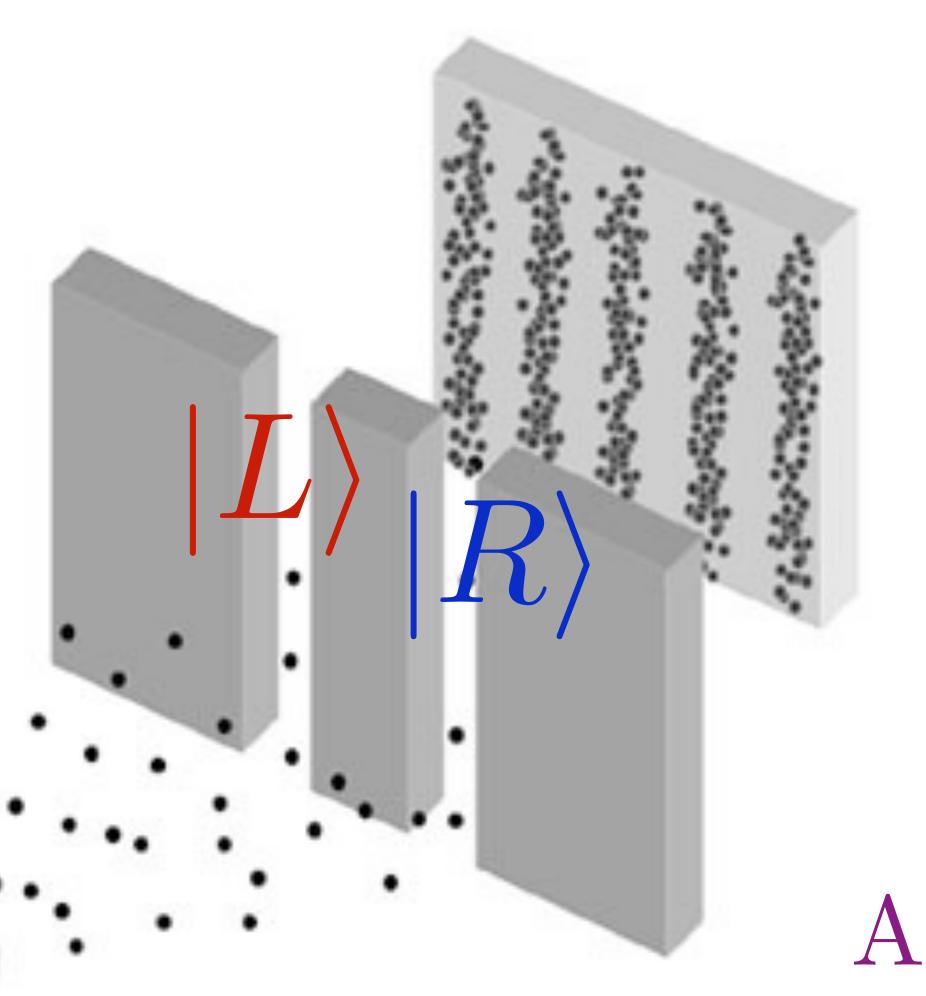
The double slit experiment



Interference of electrons

Principles of Quantum Mechanics 101: Quantum Superposition

The double slit experiment



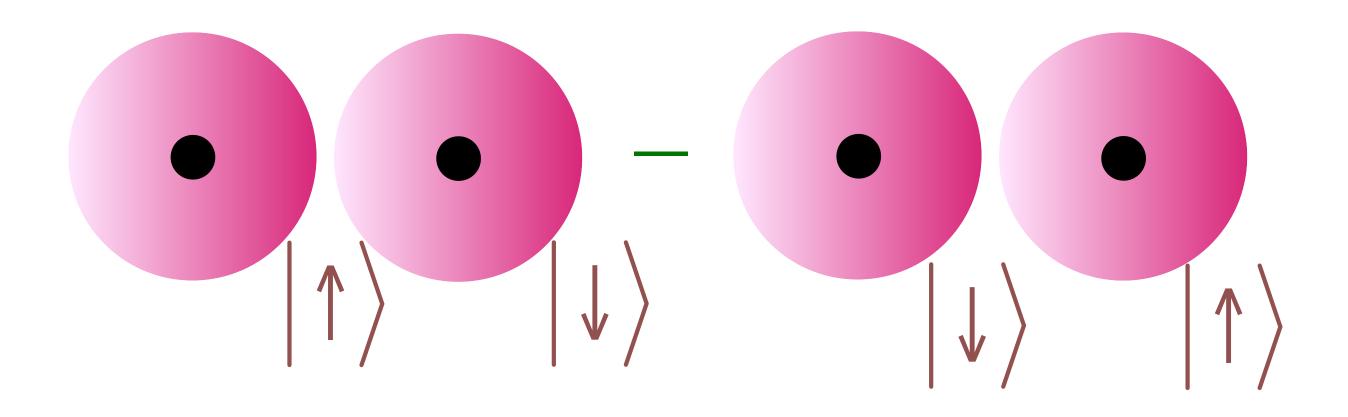
Let $|L\rangle$ represent the state with the electron in the left slit

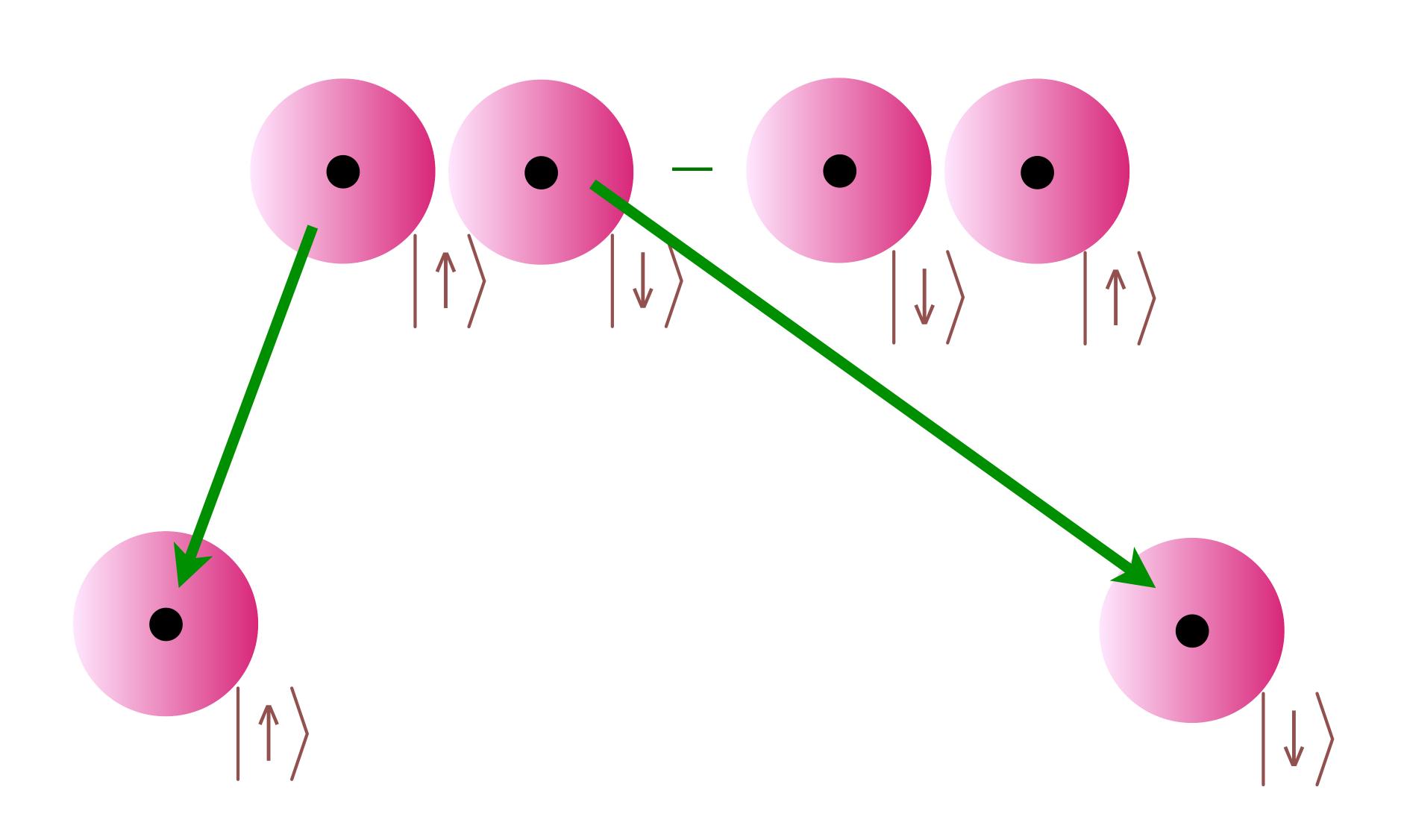
And $|R\rangle$ represents the state with the electron in the right slit

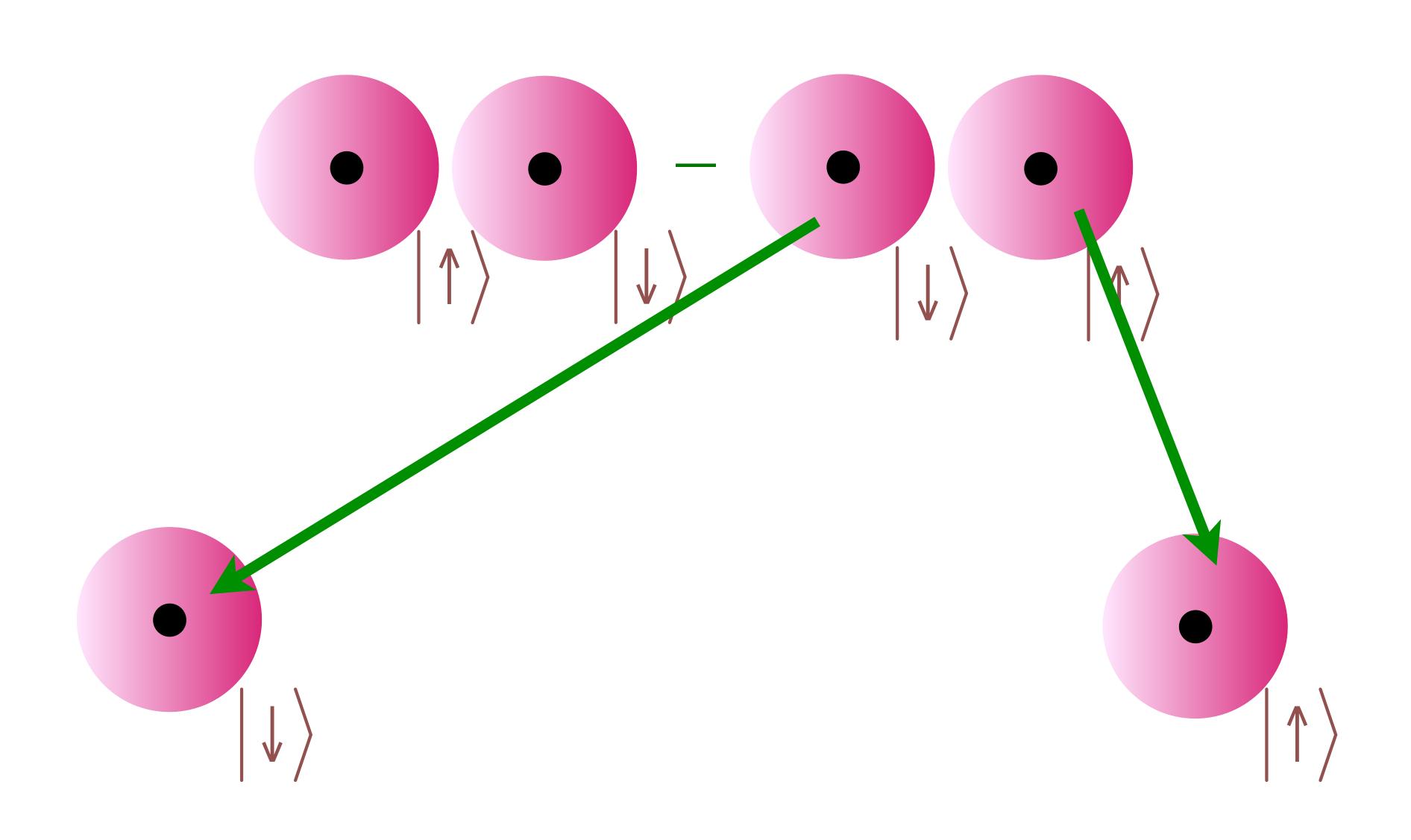
Actual state of each electron is $|L\rangle + |R\rangle$

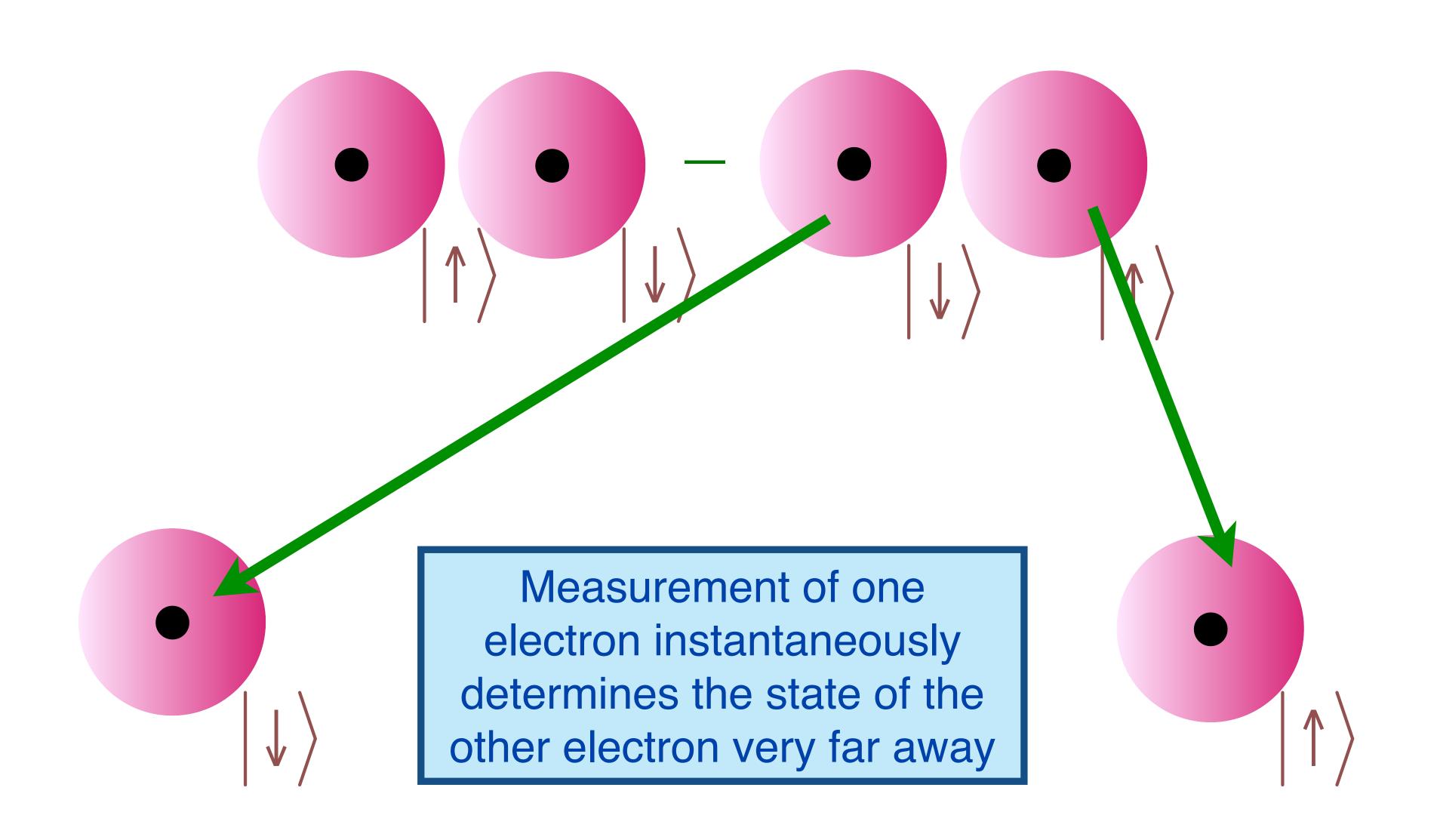
Can Quantum-Mechanical Description of Physical Reality Be Considered Complete?

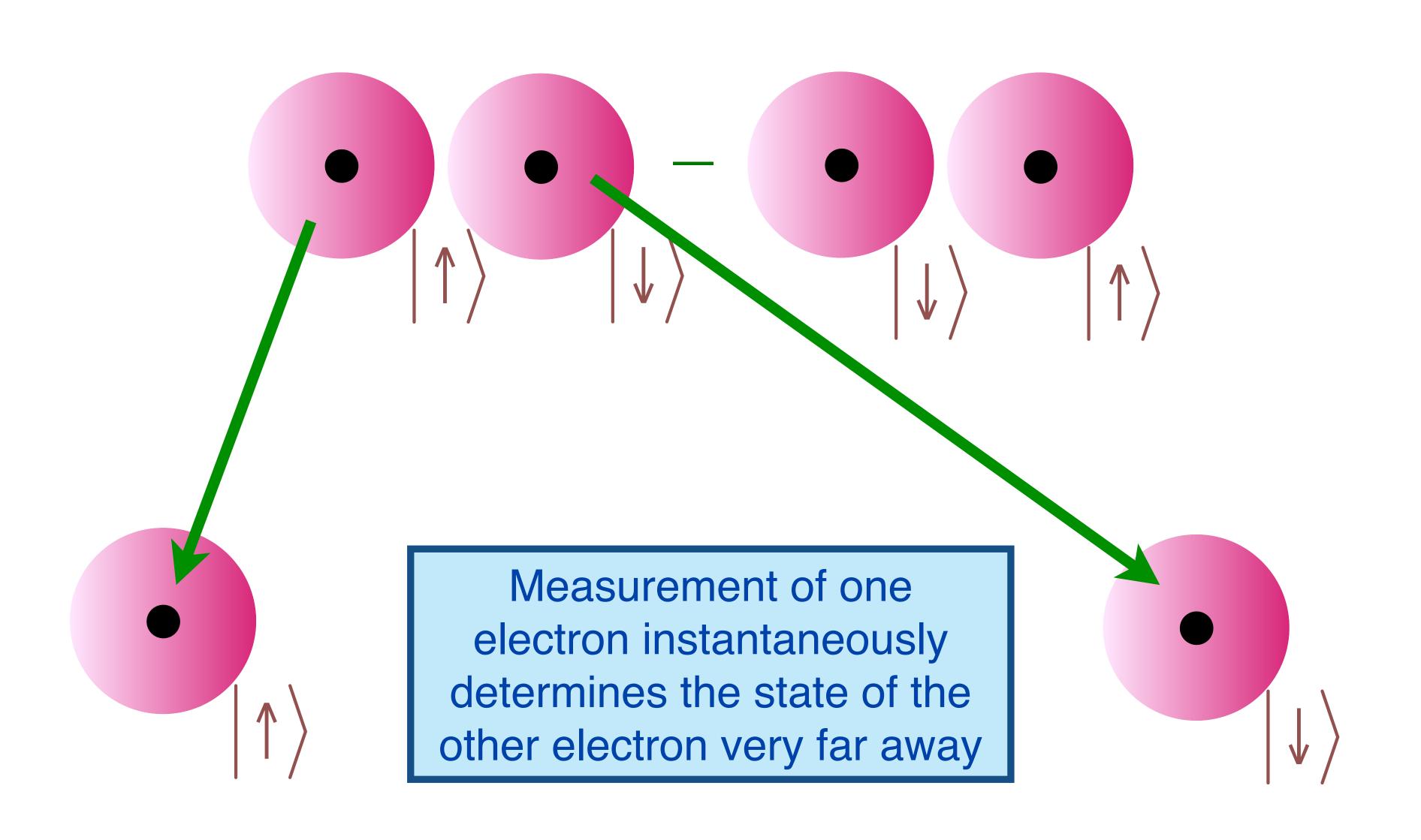
A. EINSTEIN, B. Podolsky and N. Rosen, Institute for Advanced Study, Princeton, New Jersey (Received March 25, 1935)

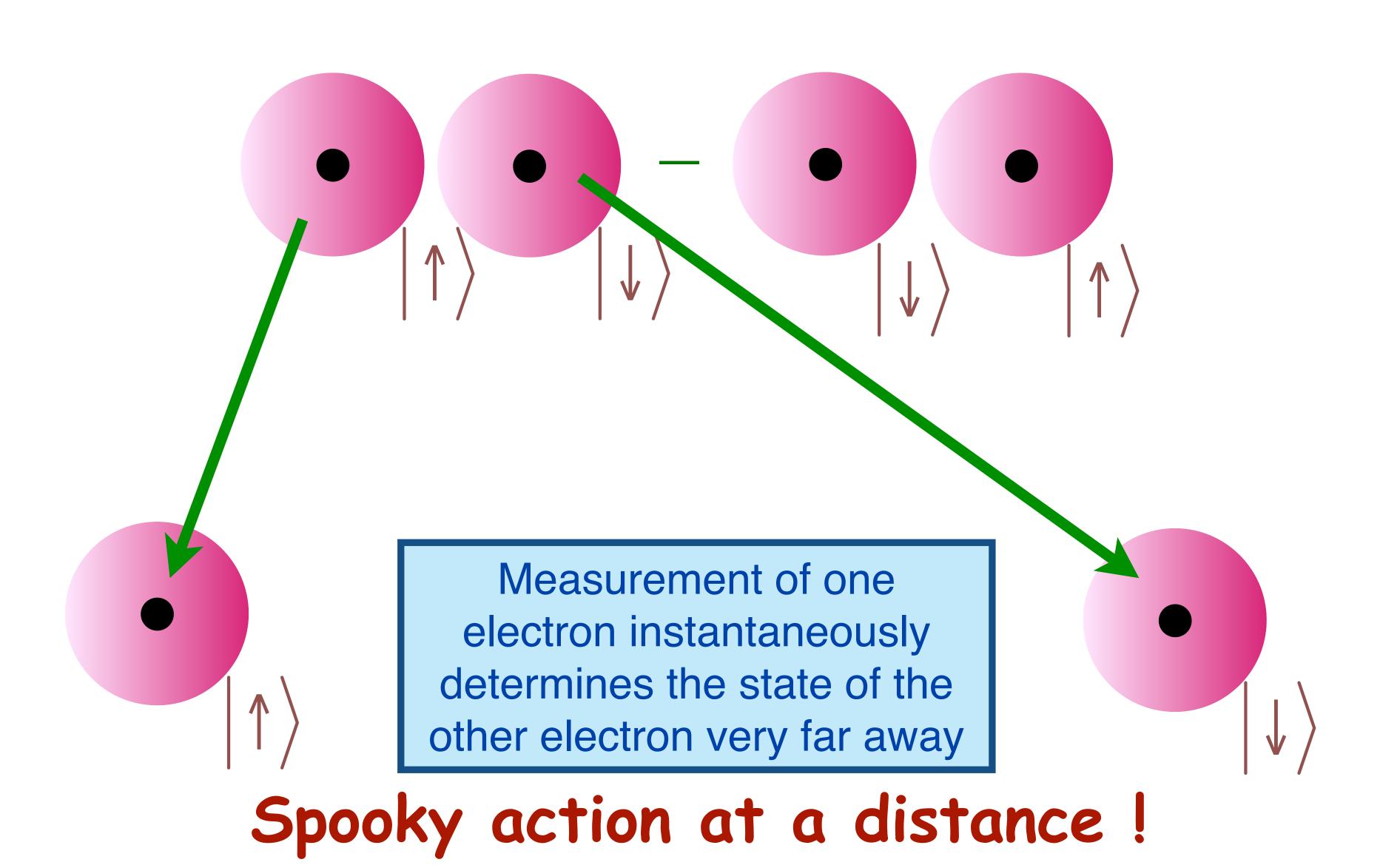












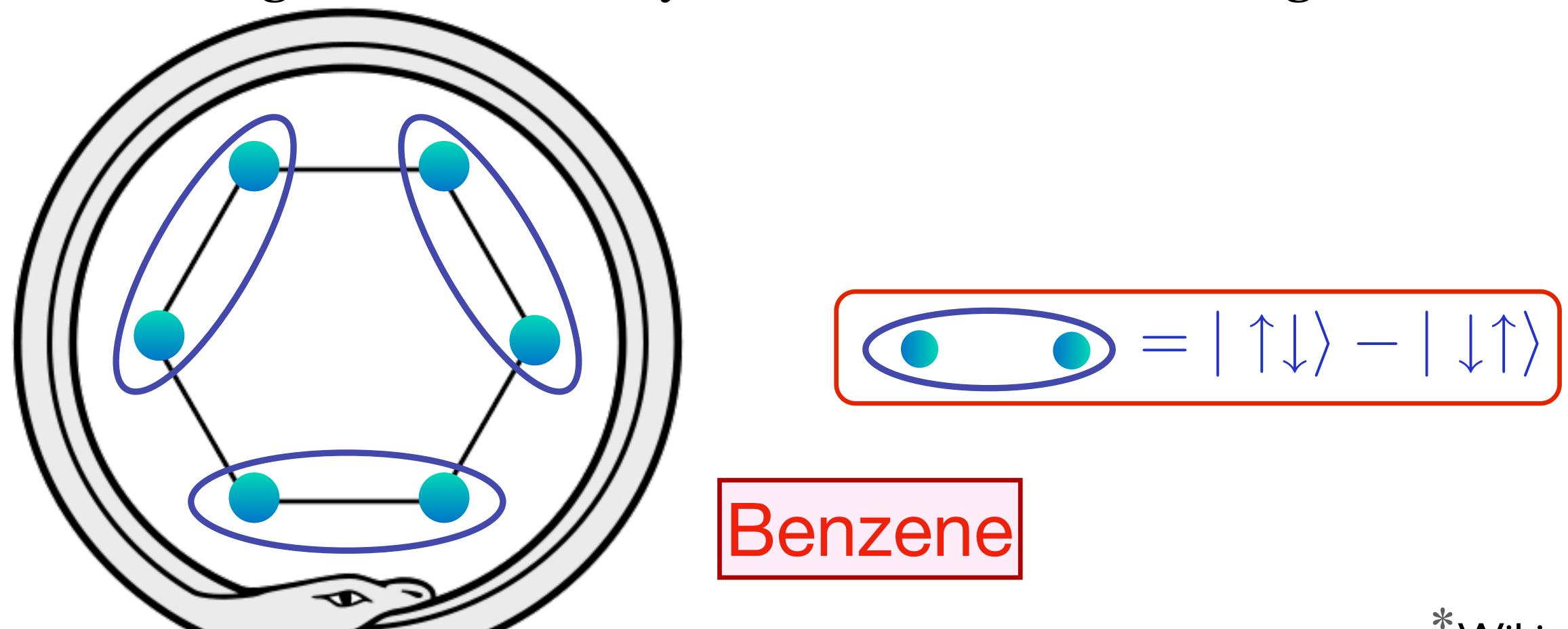
deren Notwendigkeit im Rus deren Notwendigkeit im Rus ja zuerst von Dir klar erkannt wurde, einen bedeute mus ja zuerst von Dir klar erkannt wurde, einen Bedeute mus ja zuerst von Dir klar erkannt wurde, einen Bedeute mus ja zuerst von Dir klar erkannt wurde, einen bedeute mus ja zuerst von Dir klar erkannt wurde, einen Bedeute mus ja zuerst von Dir klar erkannt wurde, einen Bedeute mus ja zuerst von Dir klar erkannt wurde, einen Bedeute mus ja zuerst von Dir klar erkannt wurde, einen Bedeute mus ja zuerst von Dir klar erkannt wurde, einen Bedeute mus ja zuerst von Dir klar erkannt wurde, einen Bedeute mus ja zuerst von Dir klar erkannt w

I cannot seriously believe in it because the theory cannot be reconciled with the idea that physics should represent a reality in time and space, free from spooky actions at distance

Albert Einstein to Max Born, 3 March 1947

Kekule's spooky dream (1865)

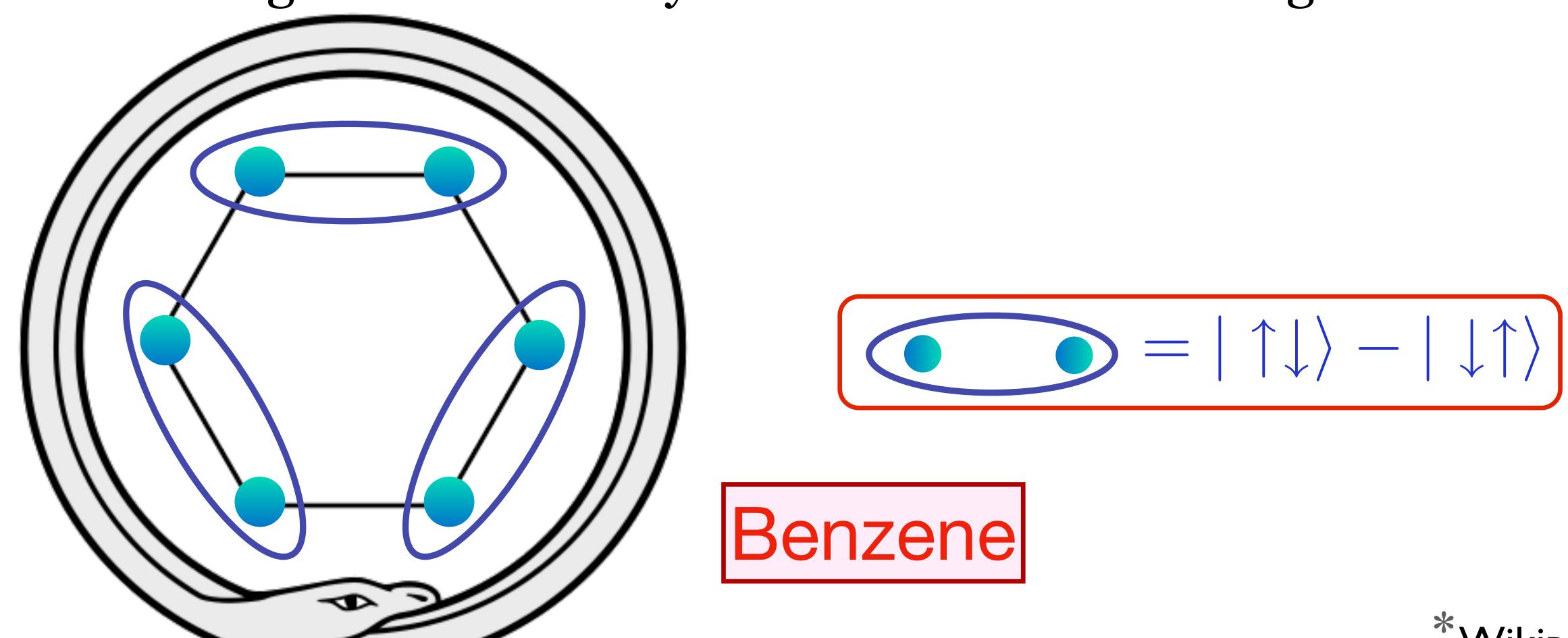
Kekulé spoke of the creation of the theory. He said that he had discovered the ring shape of the benzene molecule after having a reverie or day-dream of a snake seizing its own tail*



*Wikipedia

Kekule's spooky dream (1865)

Kekulé spoke of the creation of the theory. He said that he had discovered the ring shape of the benzene molecule after having a reverie or day-dream of a snake seizing its own tail*



*Wikipedia

Quantum spin liquids and quantum error correction

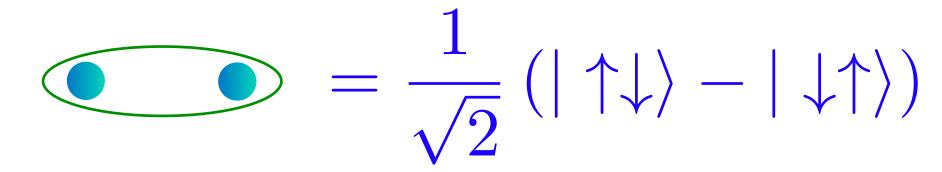
Triangular lattice antiferromagnet

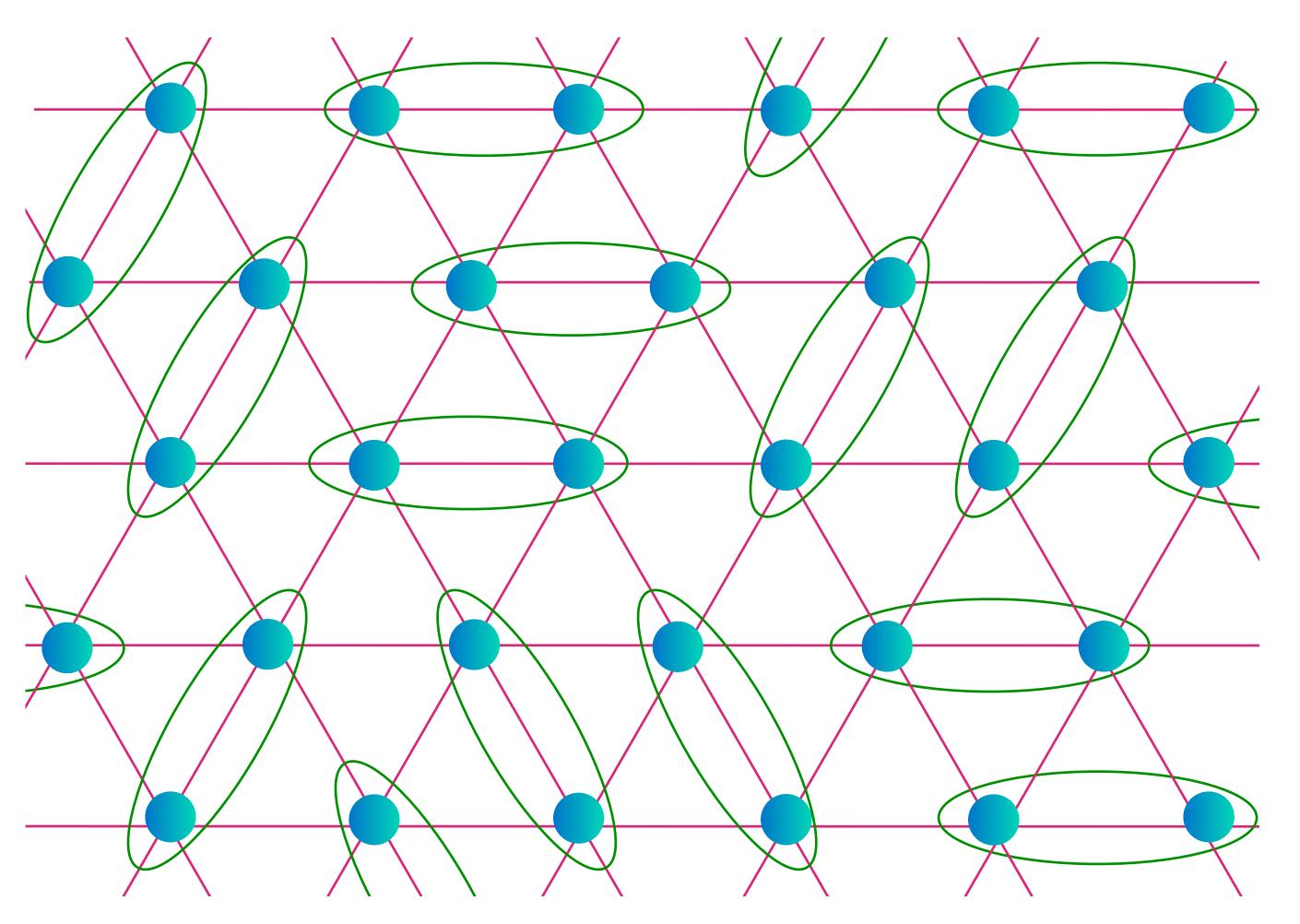
$KYbSe_2$ Yb Se

Nearest-neighbor model has ordered spins



Patrik Fazekas Hungarian Academy of Sciences

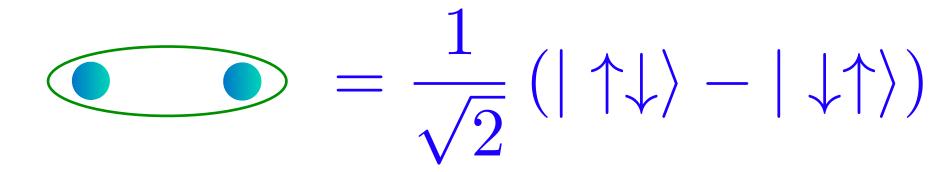


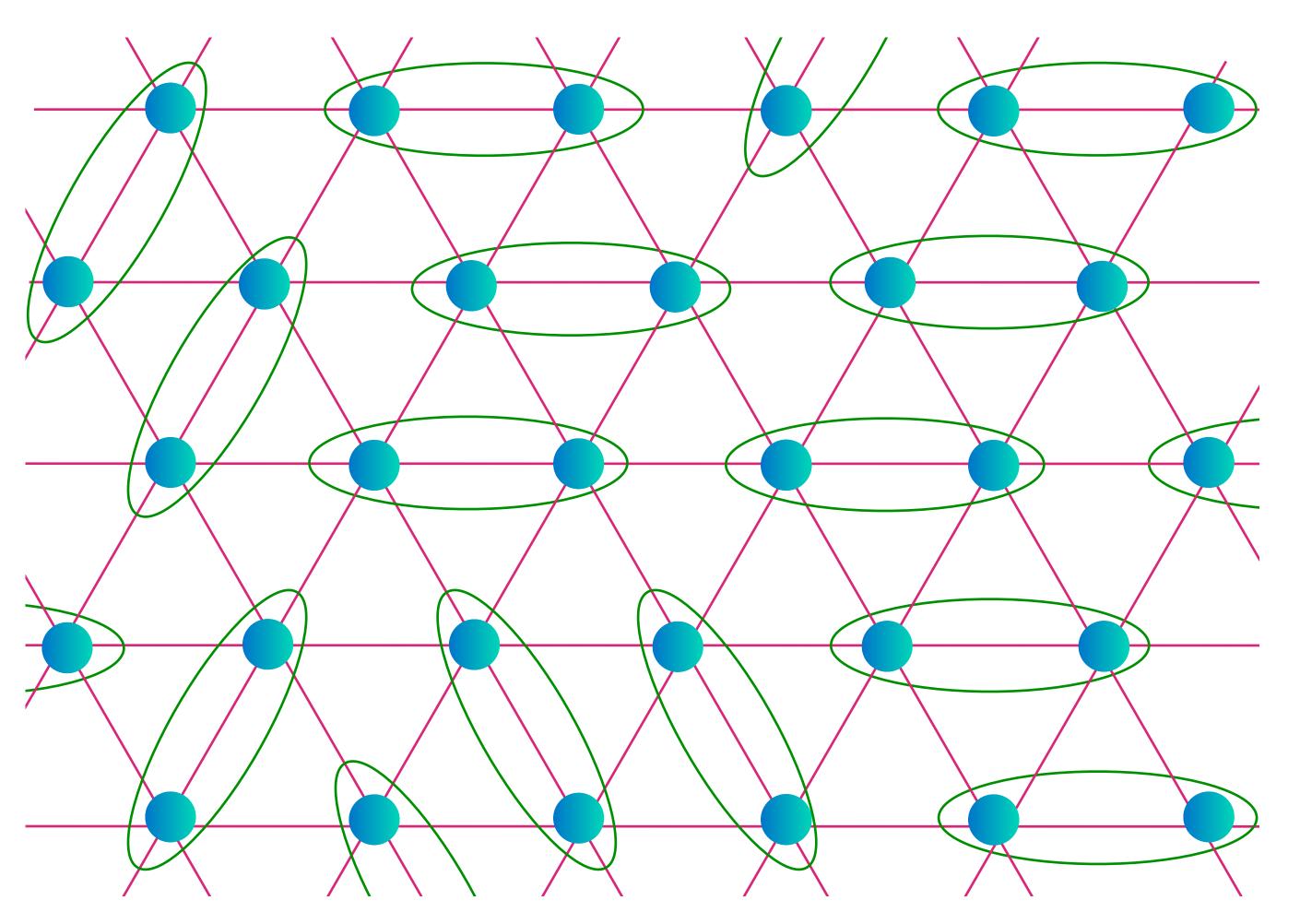


$$|G\rangle = \sum_{\mathcal{D}} c_{\mathcal{D}} |\mathcal{D}\rangle$$



Patrik Fazekas Hungarian Academy of Sciences

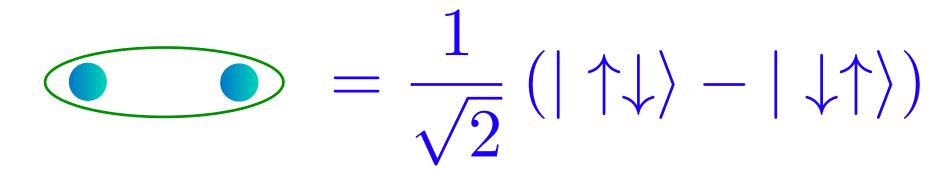


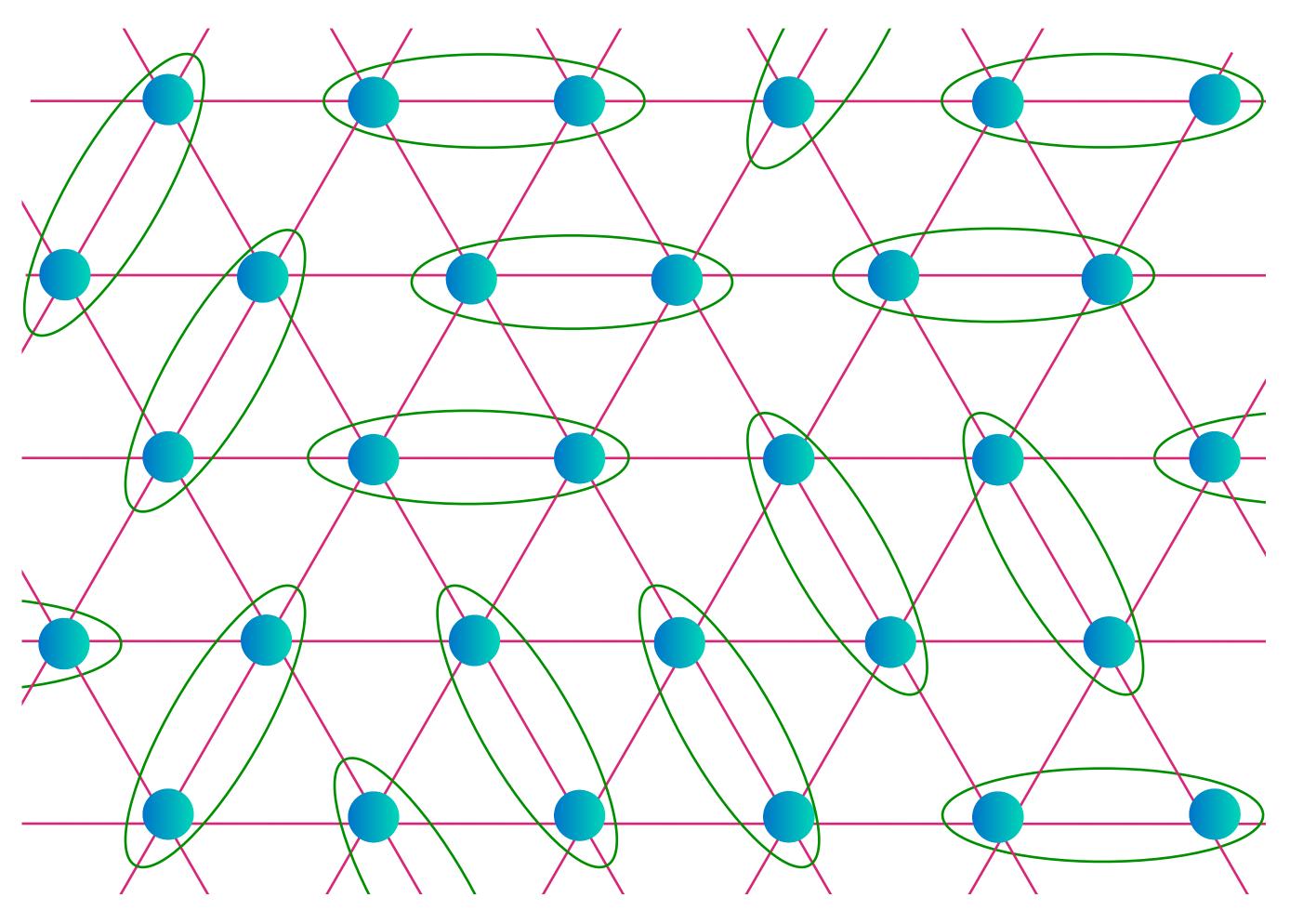


$$|G\rangle = \sum_{\mathcal{D}} c_{\mathcal{D}} |\mathcal{D}\rangle$$



Patrik Fazekas Hungarian Academy of Sciences

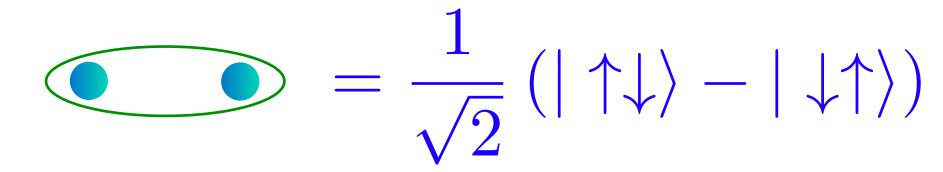


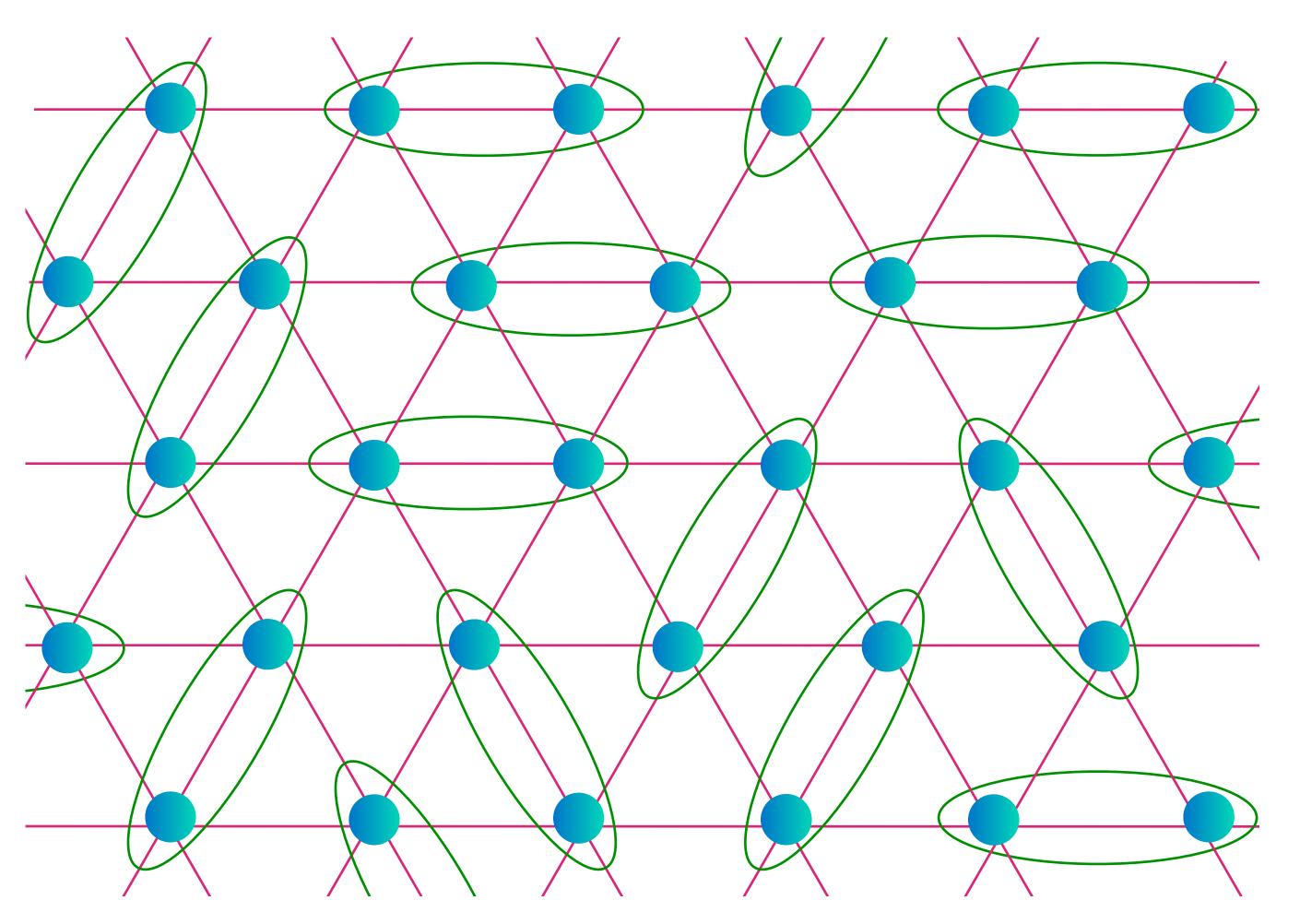


$$|G\rangle = \sum_{\mathcal{D}} c_{\mathcal{D}} |\mathcal{D}\rangle$$



Patrik Fazekas Hungarian Academy of Sciences

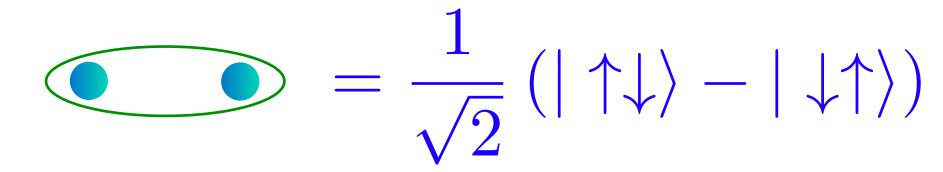


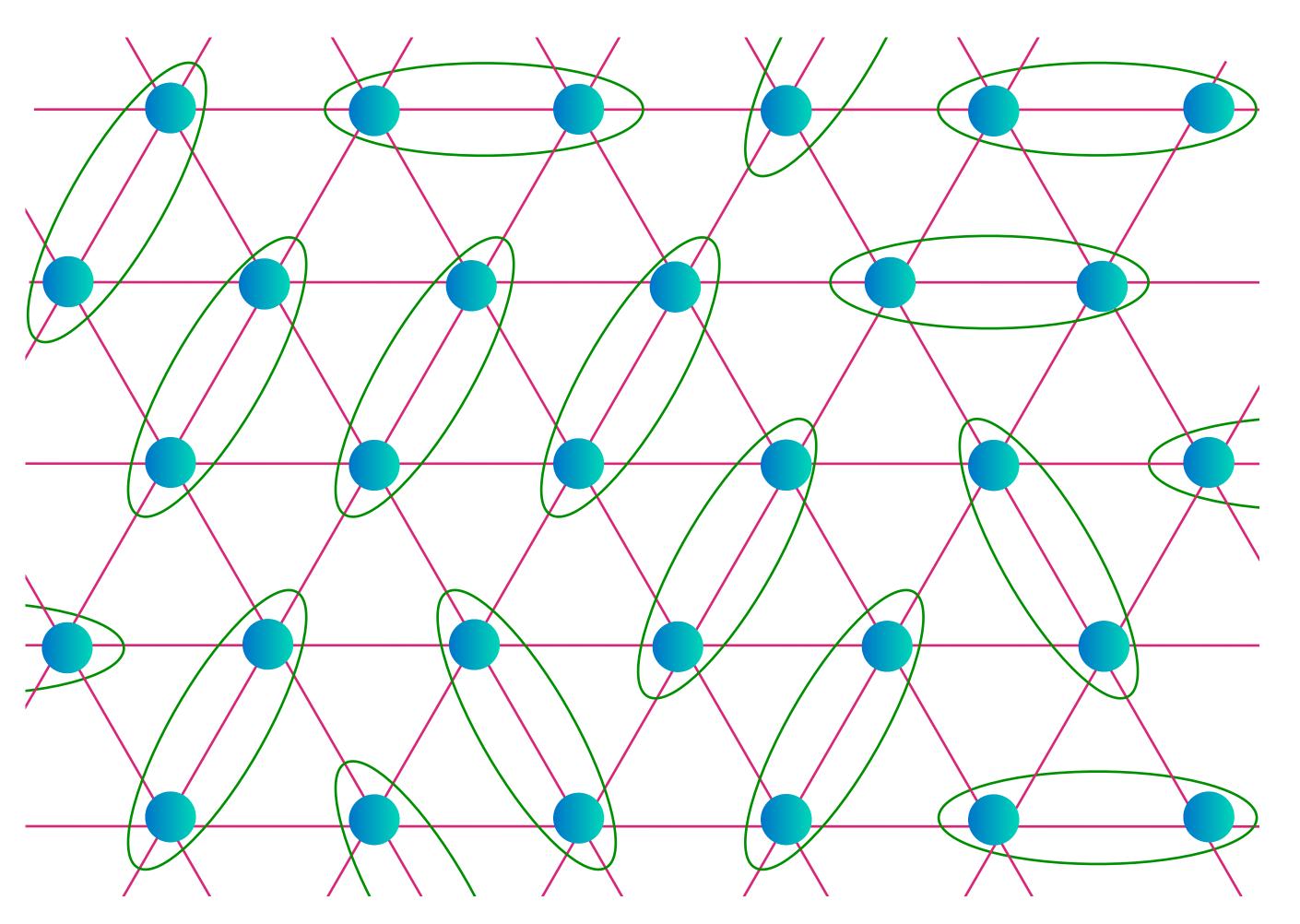


$$|G\rangle = \sum_{\mathcal{D}} c_{\mathcal{D}} |\mathcal{D}\rangle$$



Patrik Fazekas Hungarian Academy of Sciences

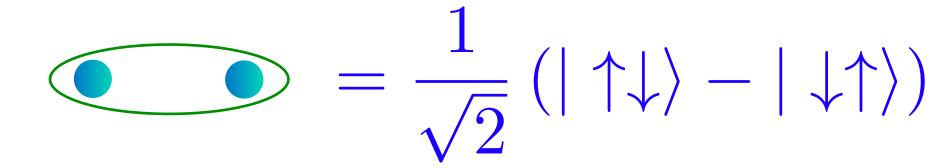


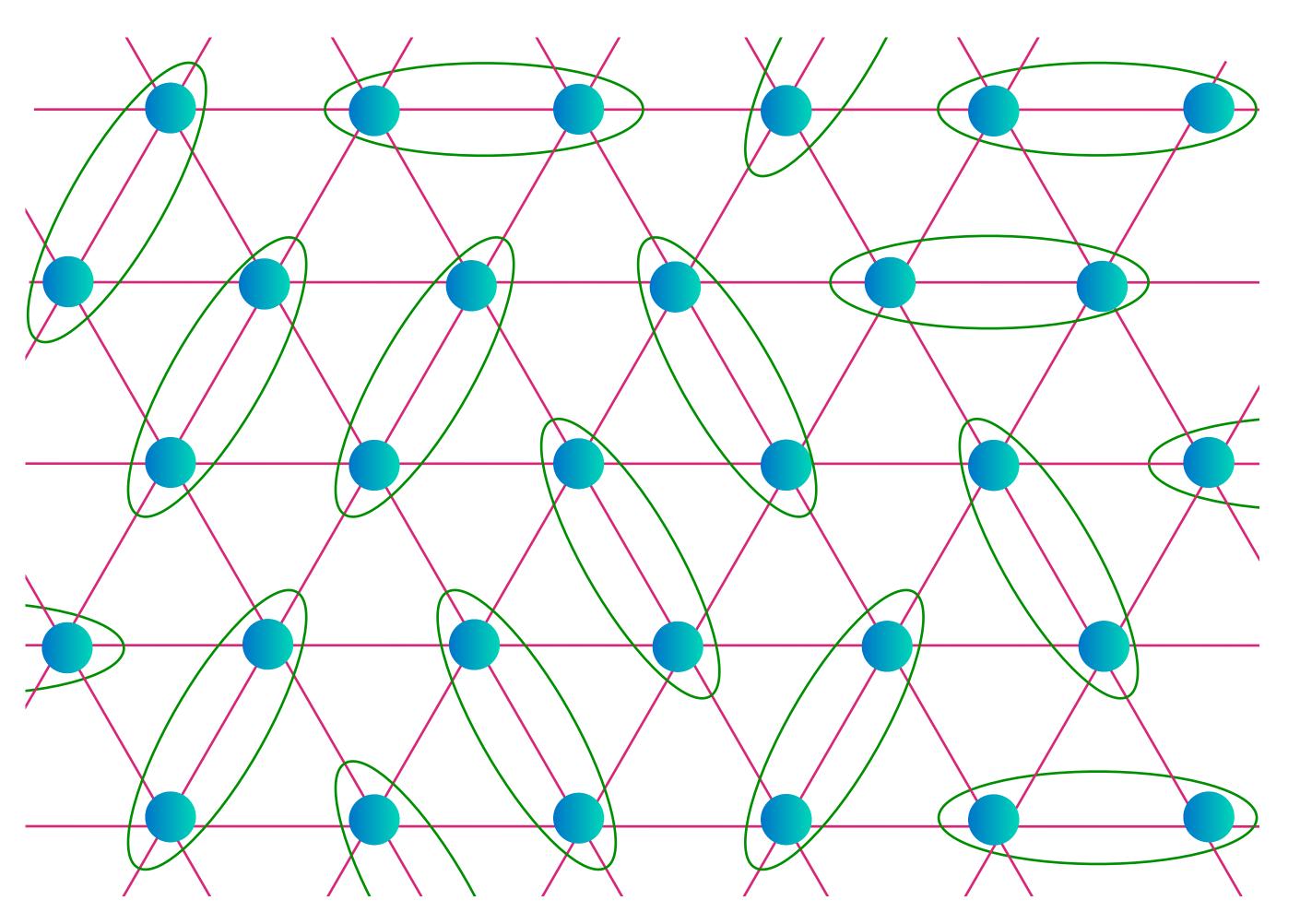


$$|G\rangle = \sum_{\mathcal{D}} c_{\mathcal{D}} |\mathcal{D}\rangle$$



Patrik Fazekas Hungarian Academy of Sciences

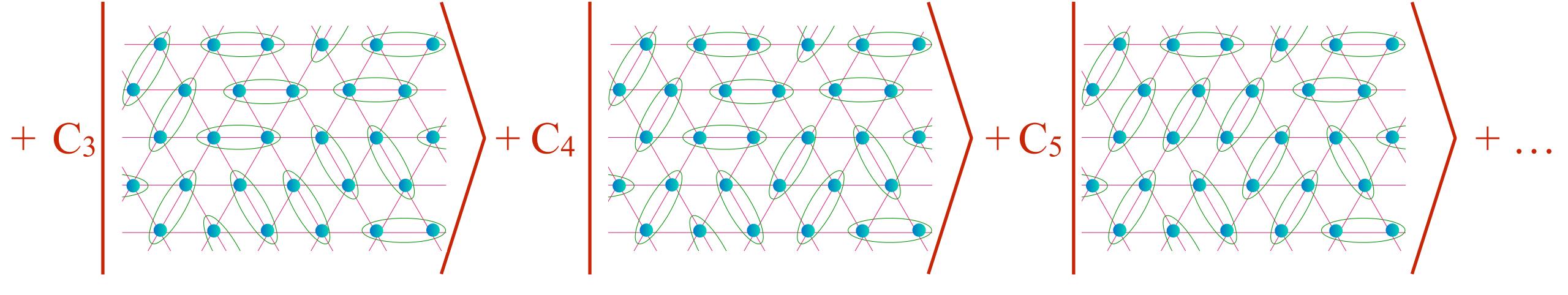


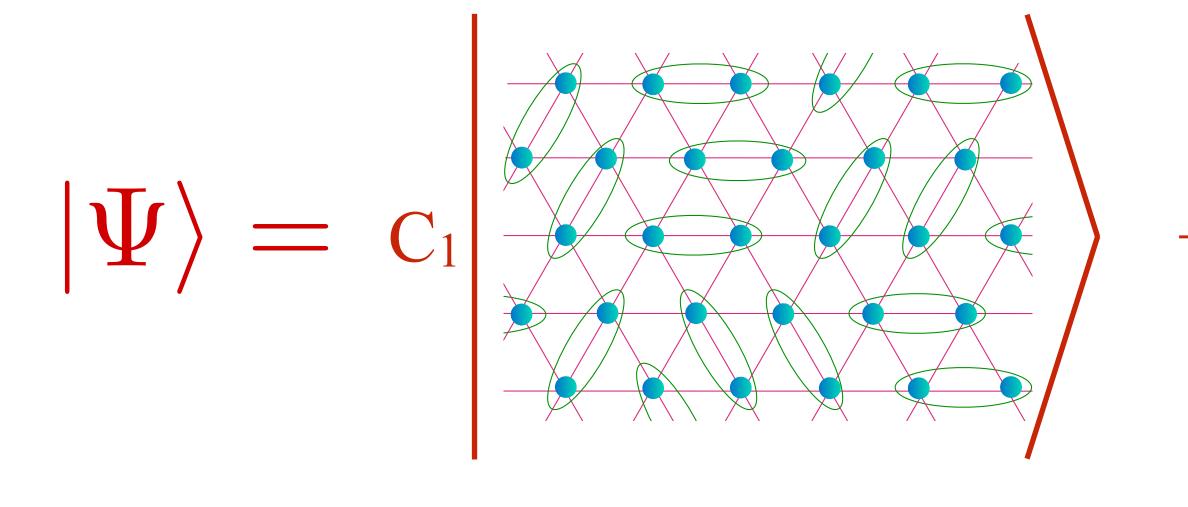


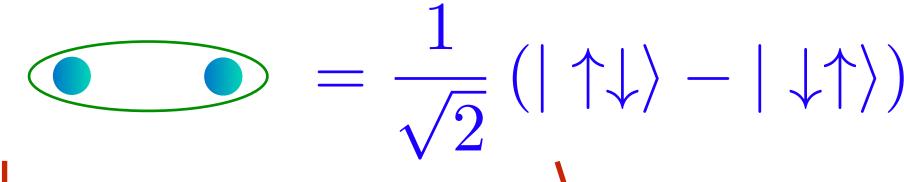
$$|G\rangle = \sum_{\mathcal{D}} c_{\mathcal{D}} |\mathcal{D}\rangle$$

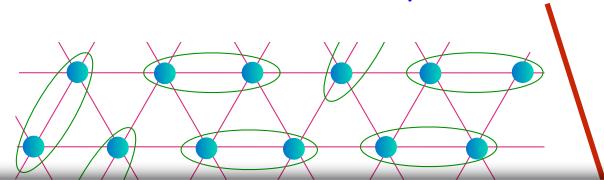
 $\mathcal{D} \to \mathrm{dimer\ covering}$ of lattice

$$|\Psi
angle = c_1$$
 $|\Psi
angle = c_1$ $|\Psi
angle = c_1$





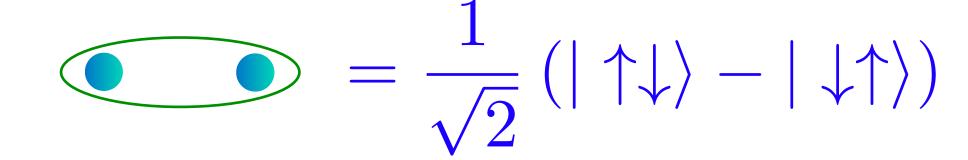


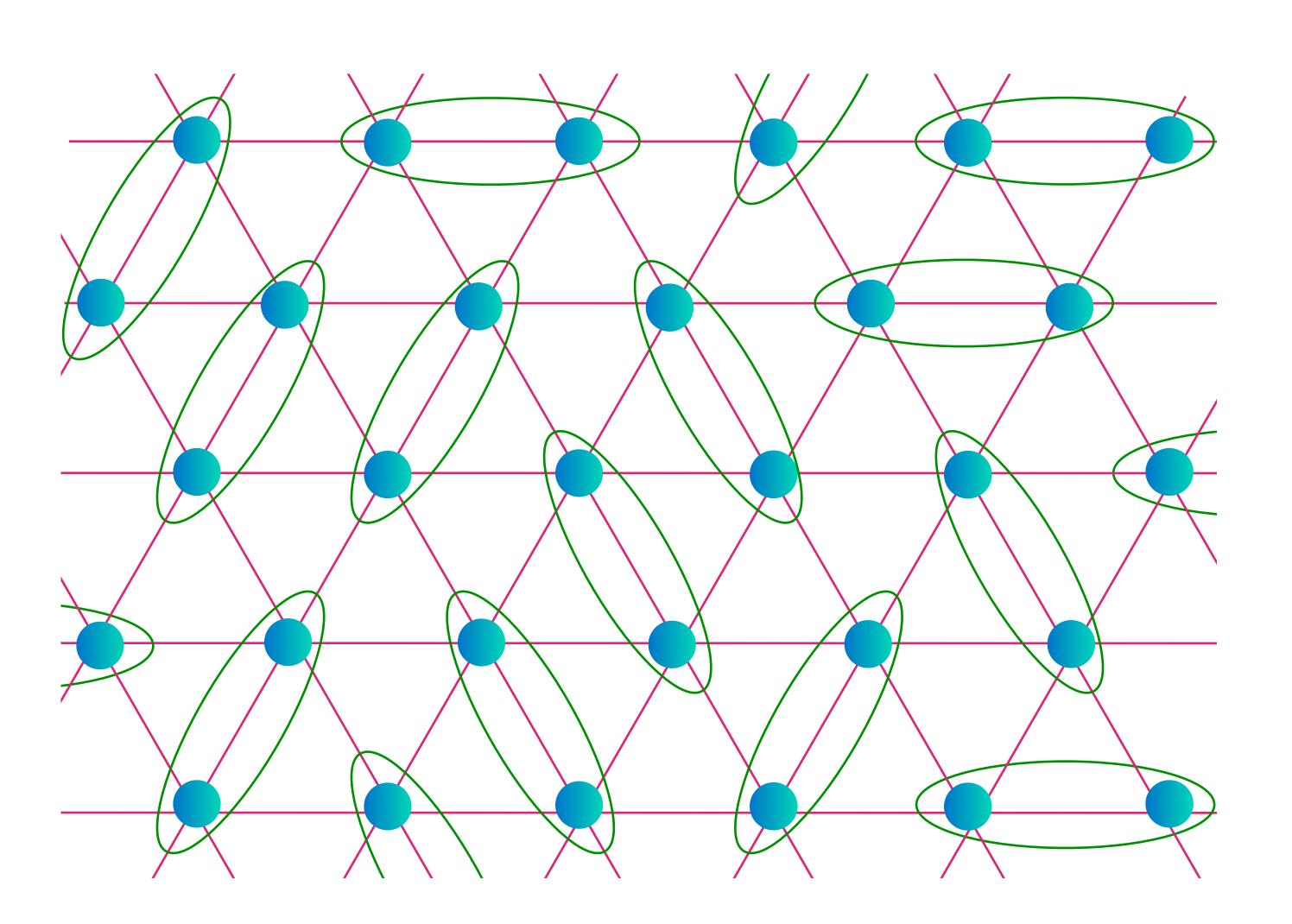


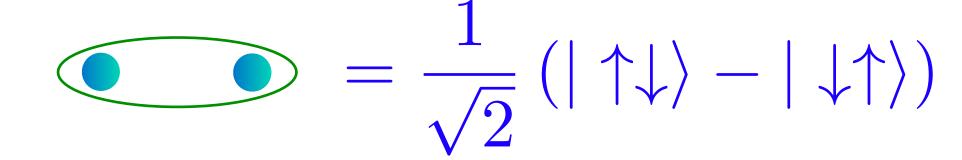
Key feature: fractionalization.

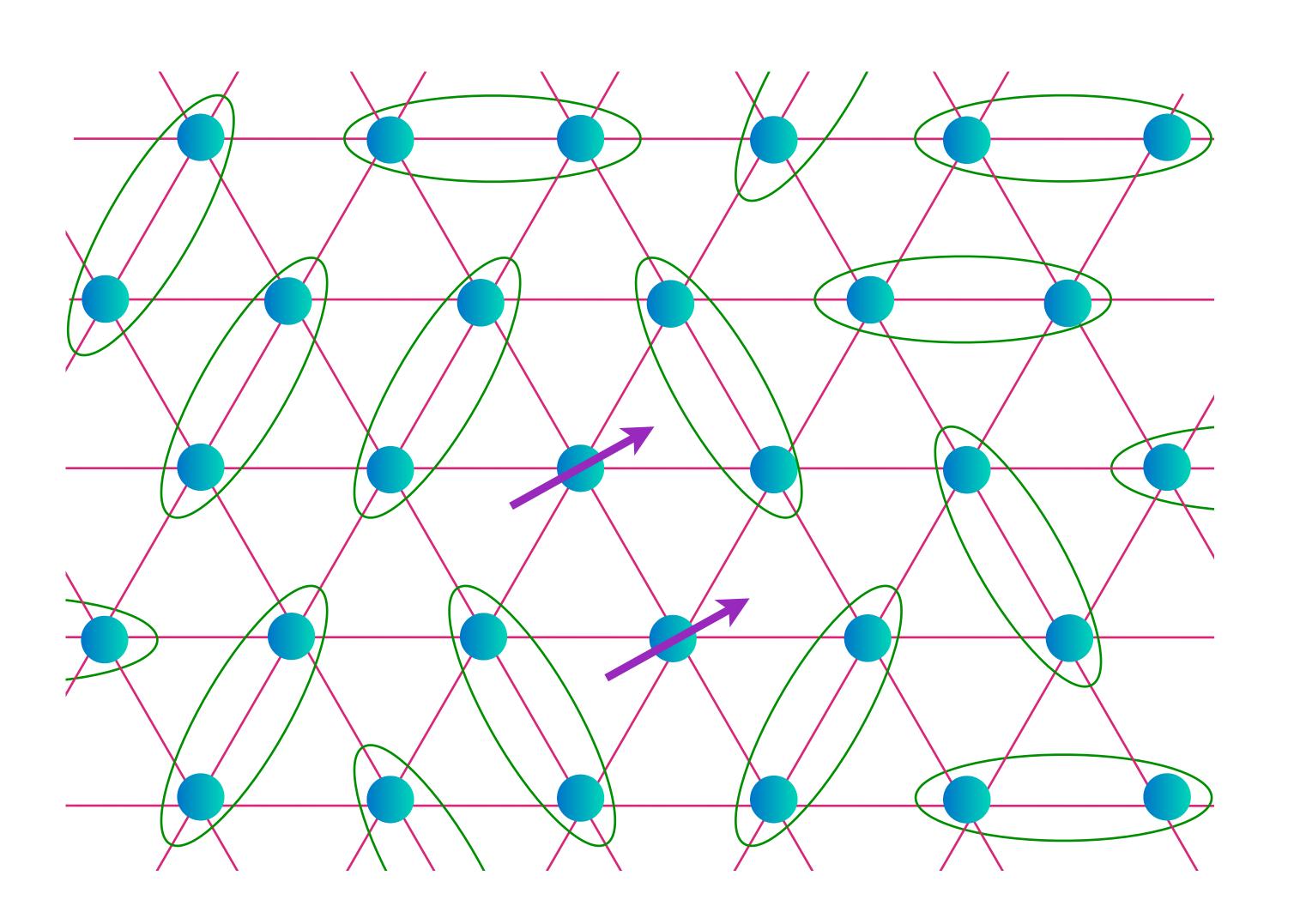
Excitations are particle-like, but cannot be created by local operators.

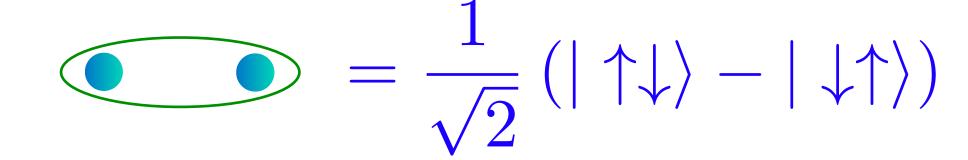
The excitations are classified under distinct anyon sectors.

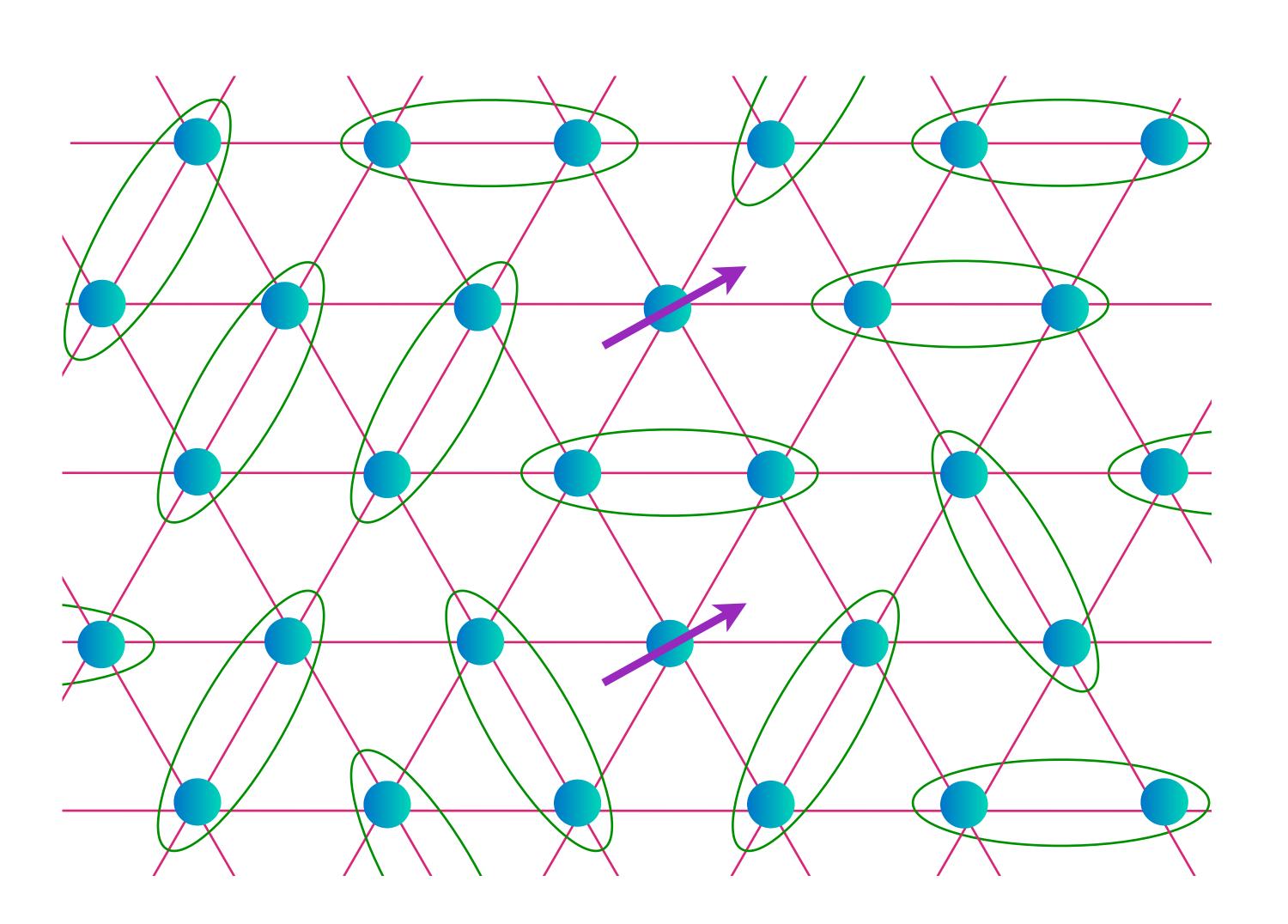


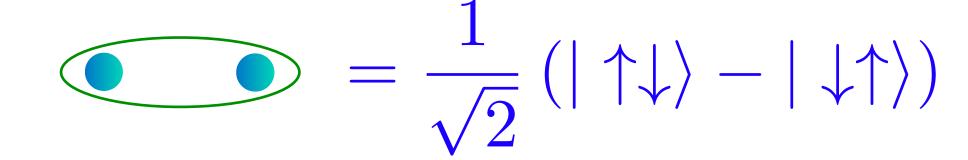


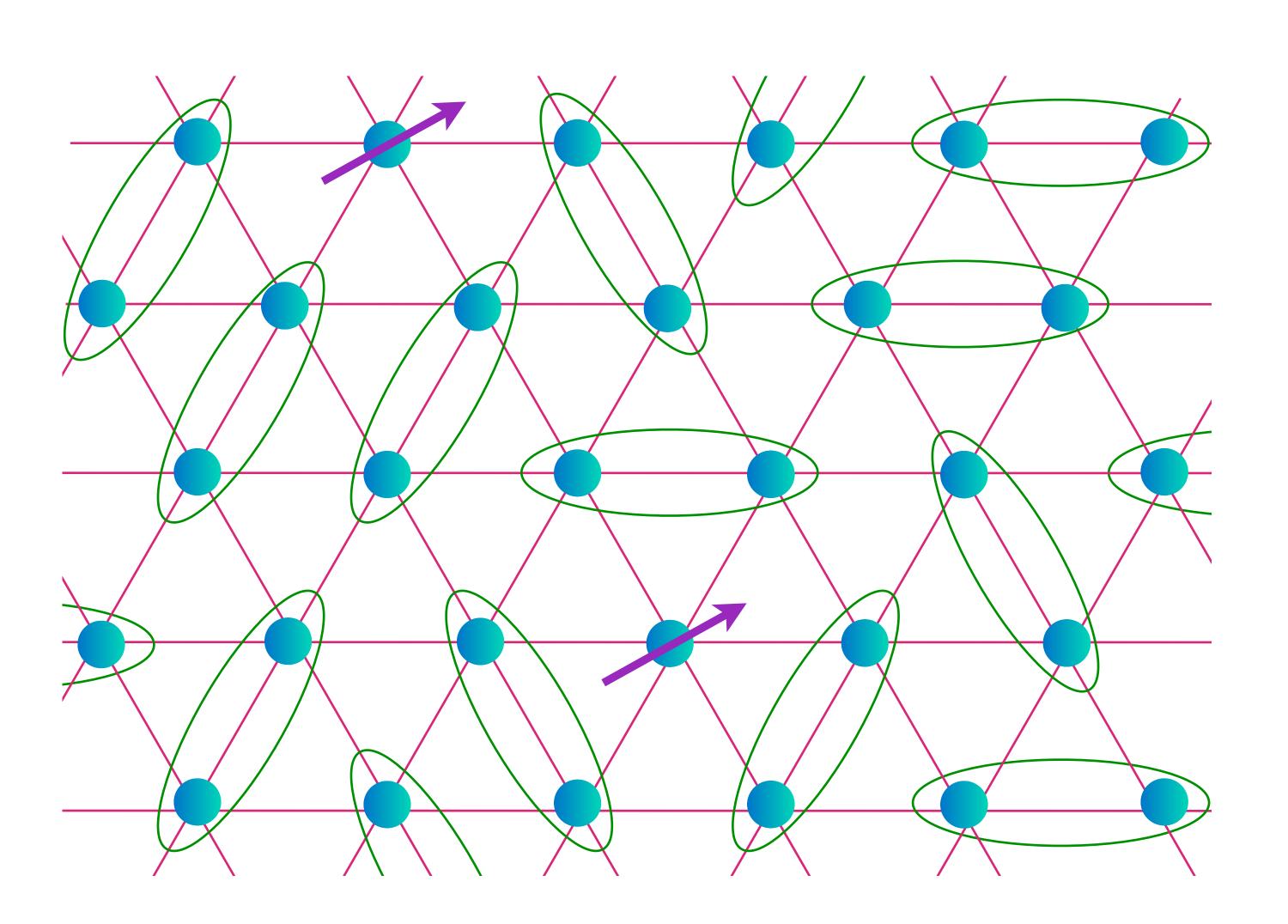


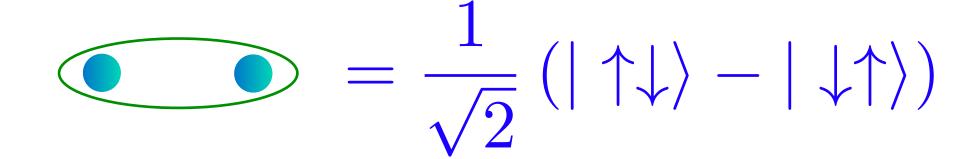


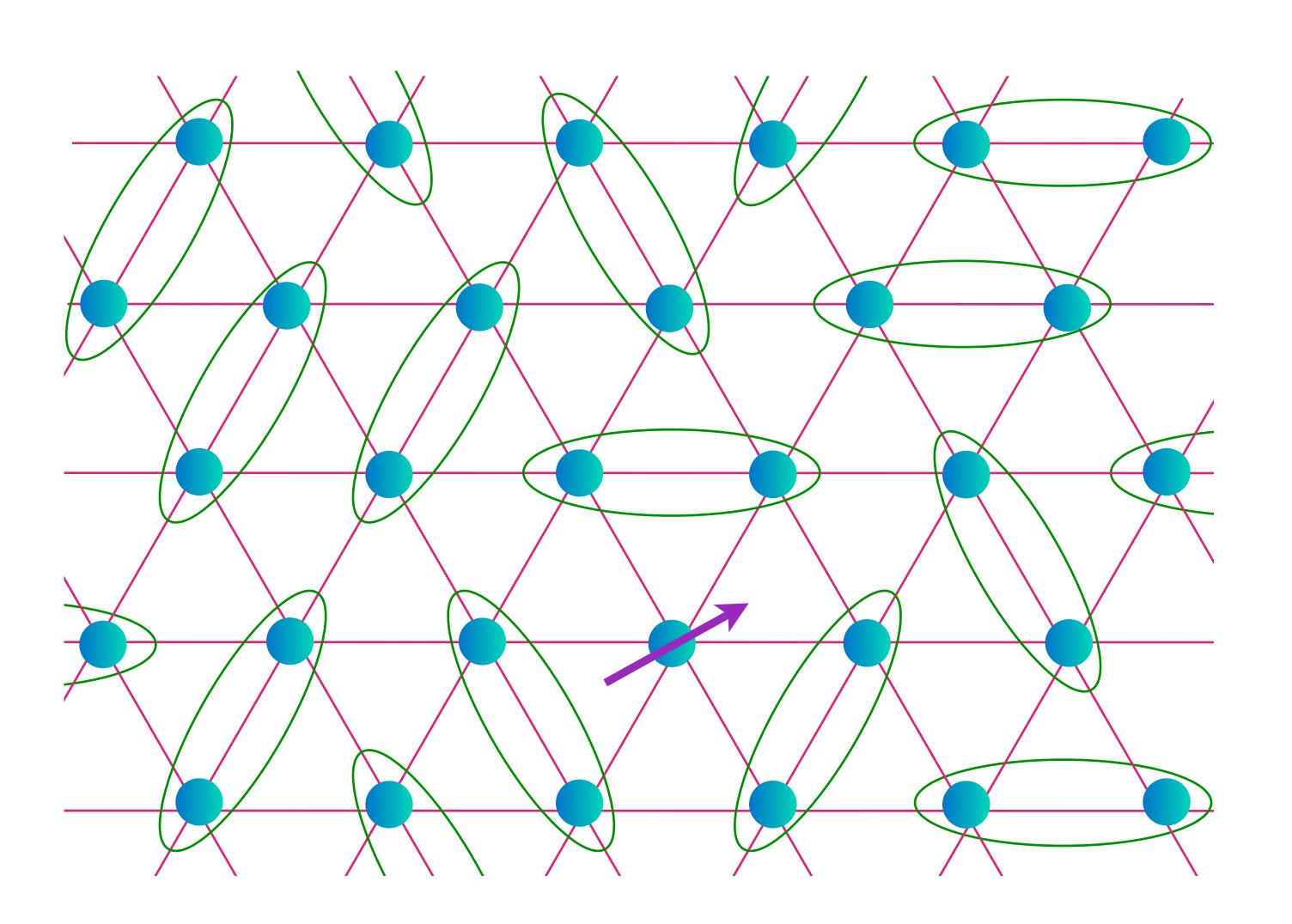


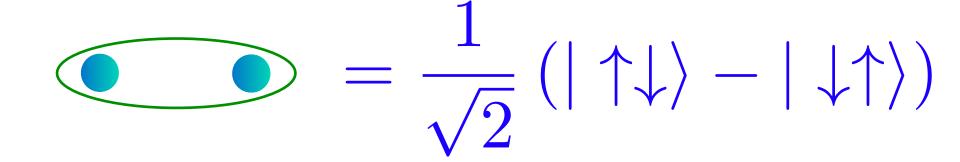


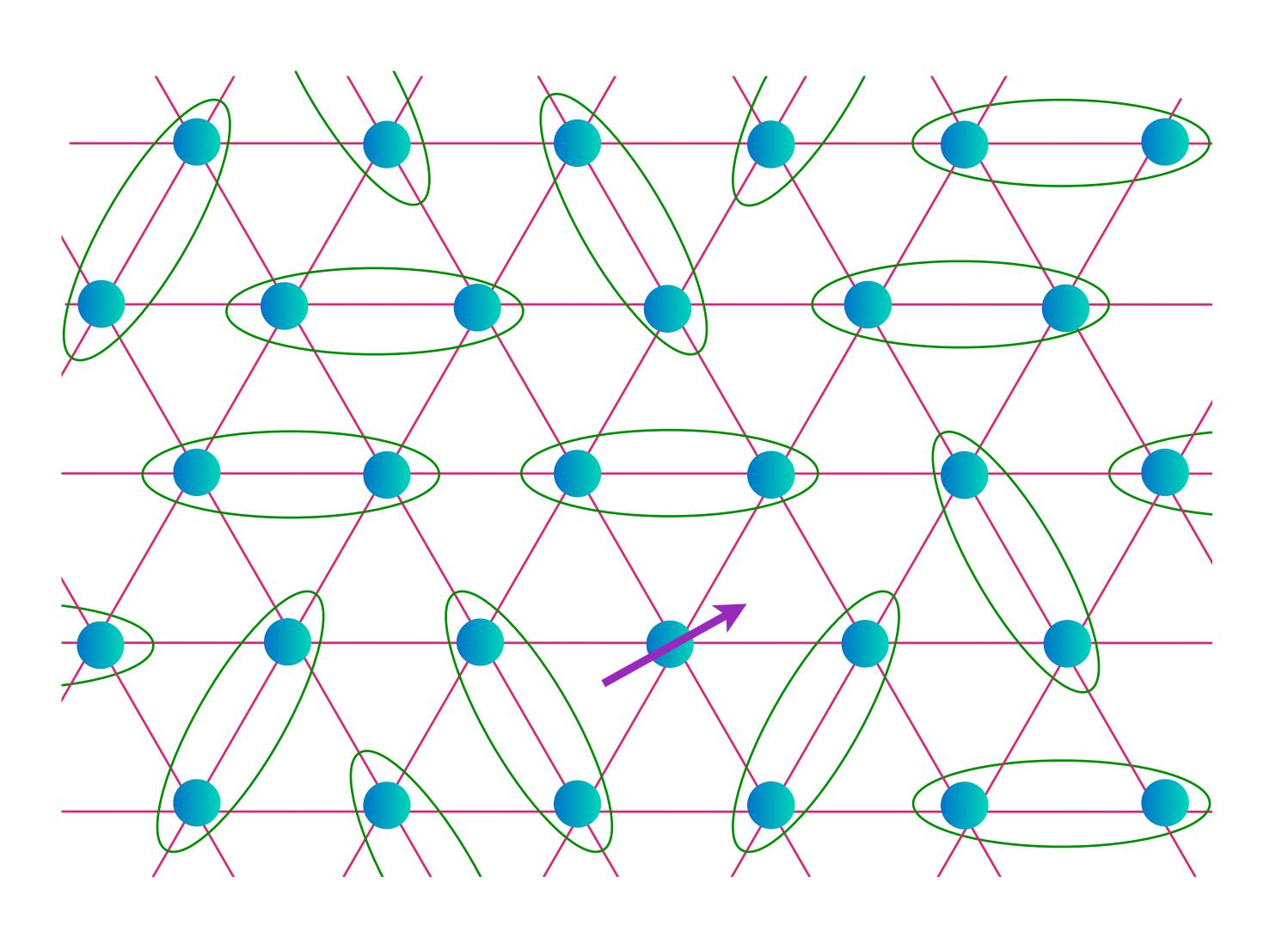


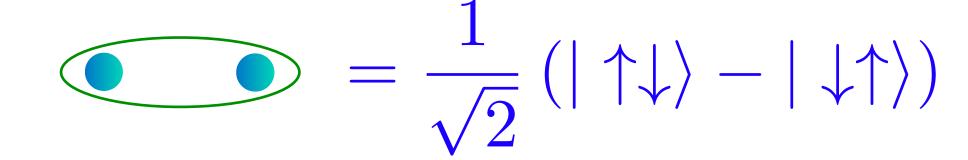


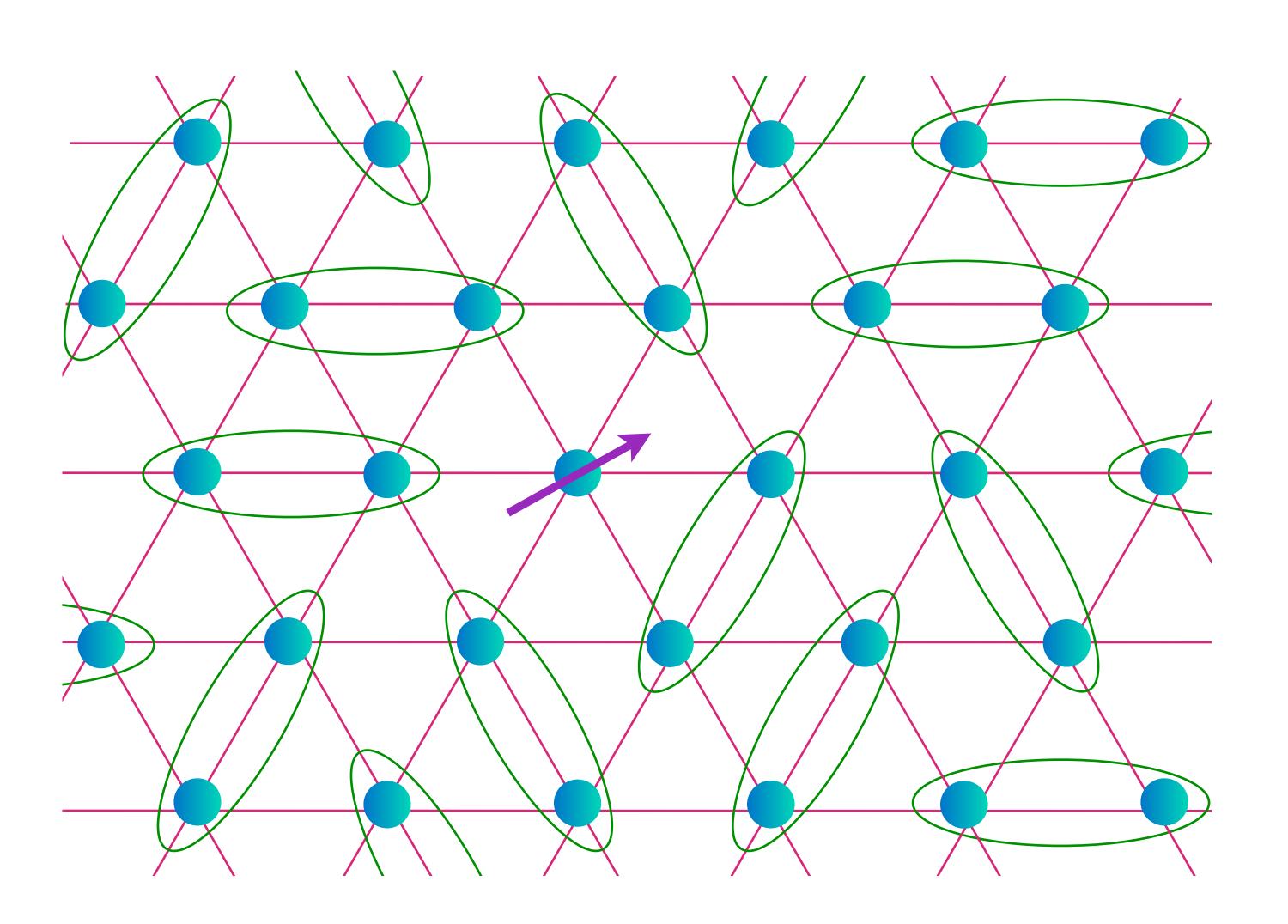


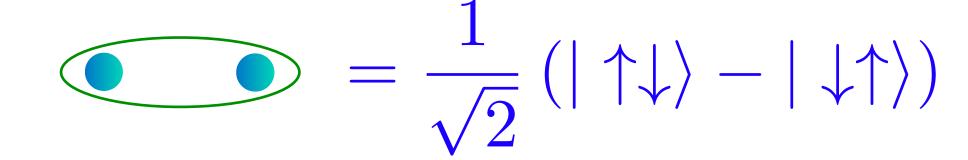


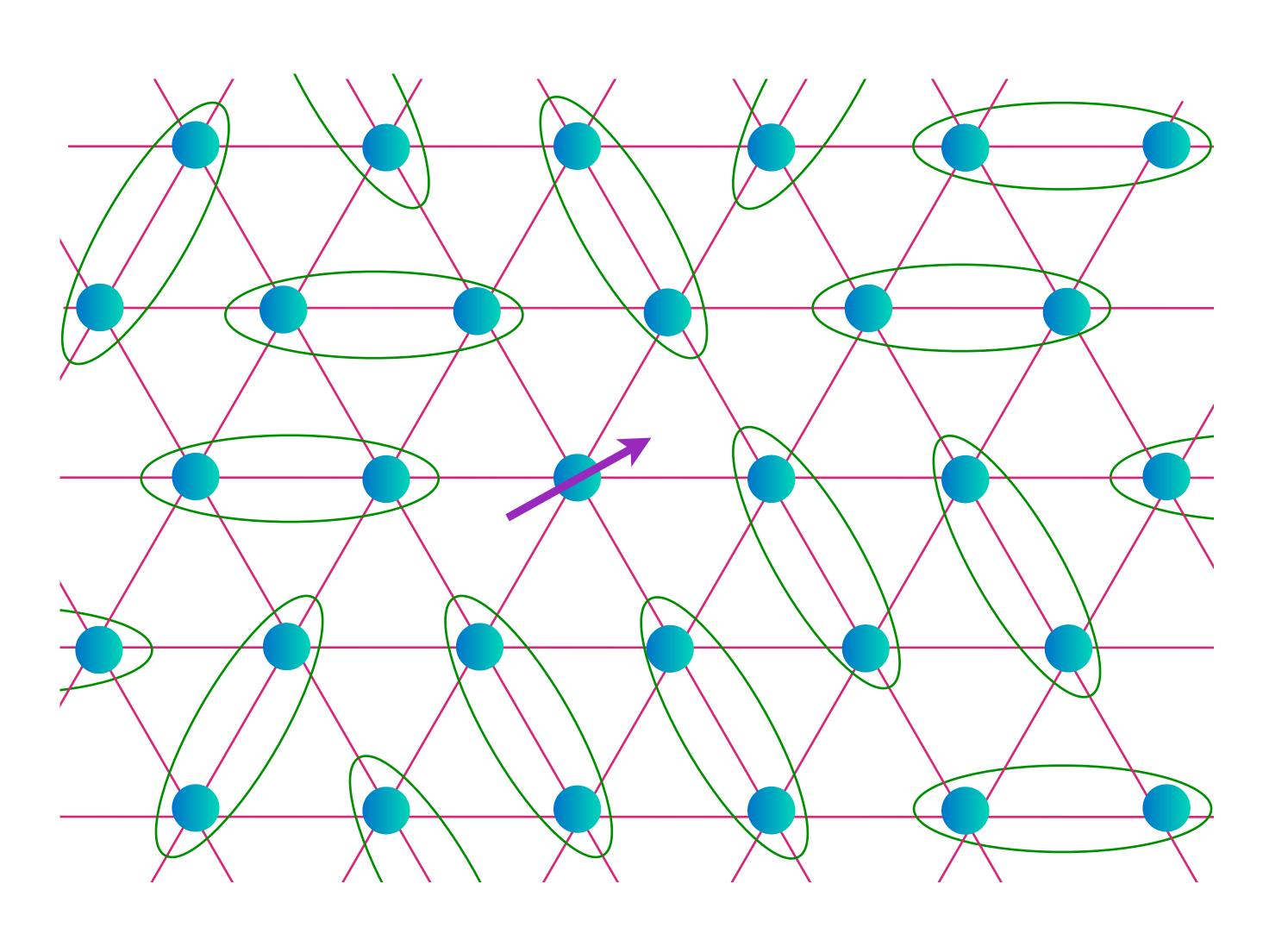


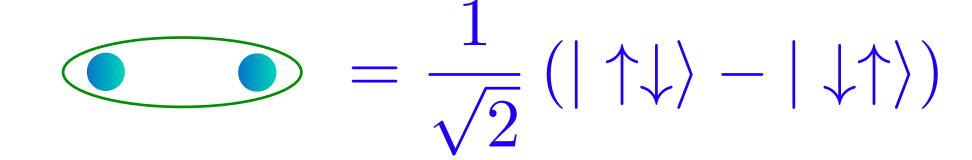


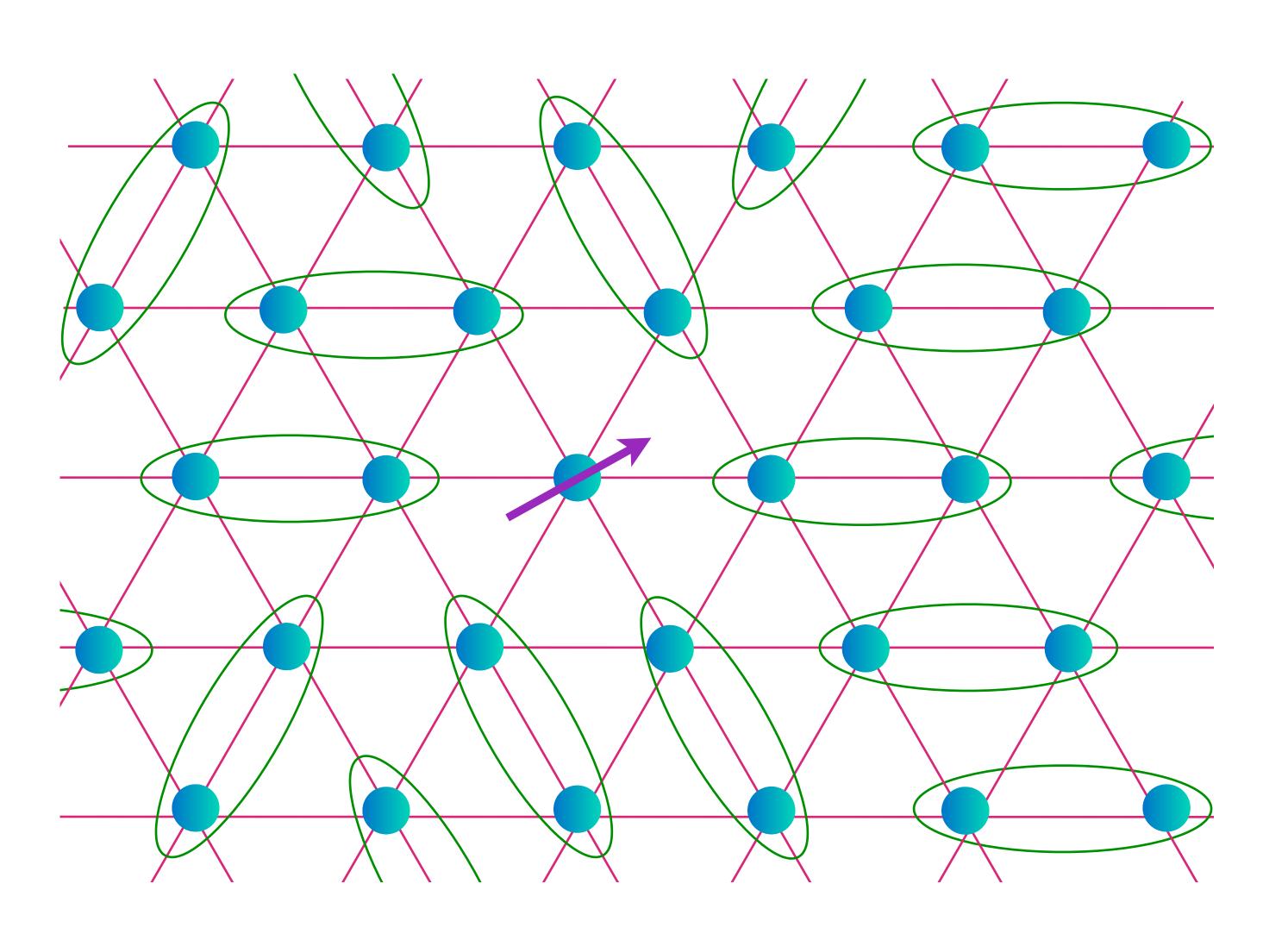




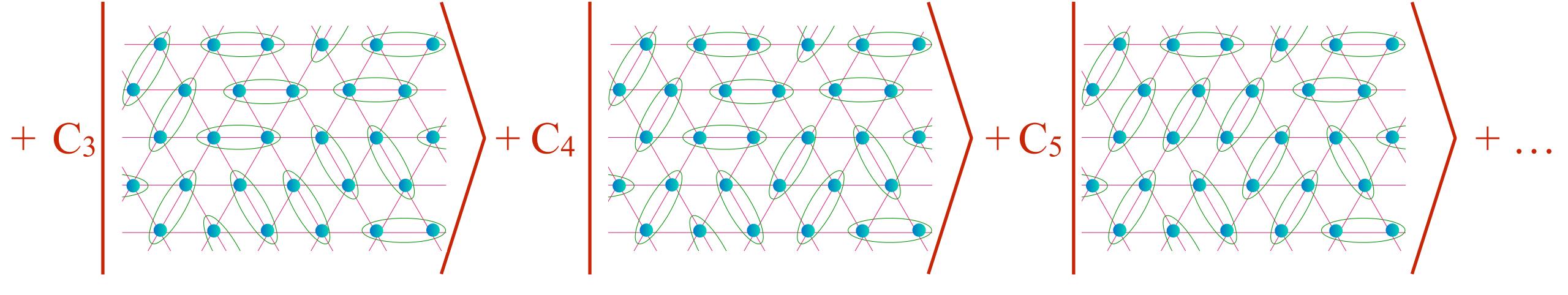




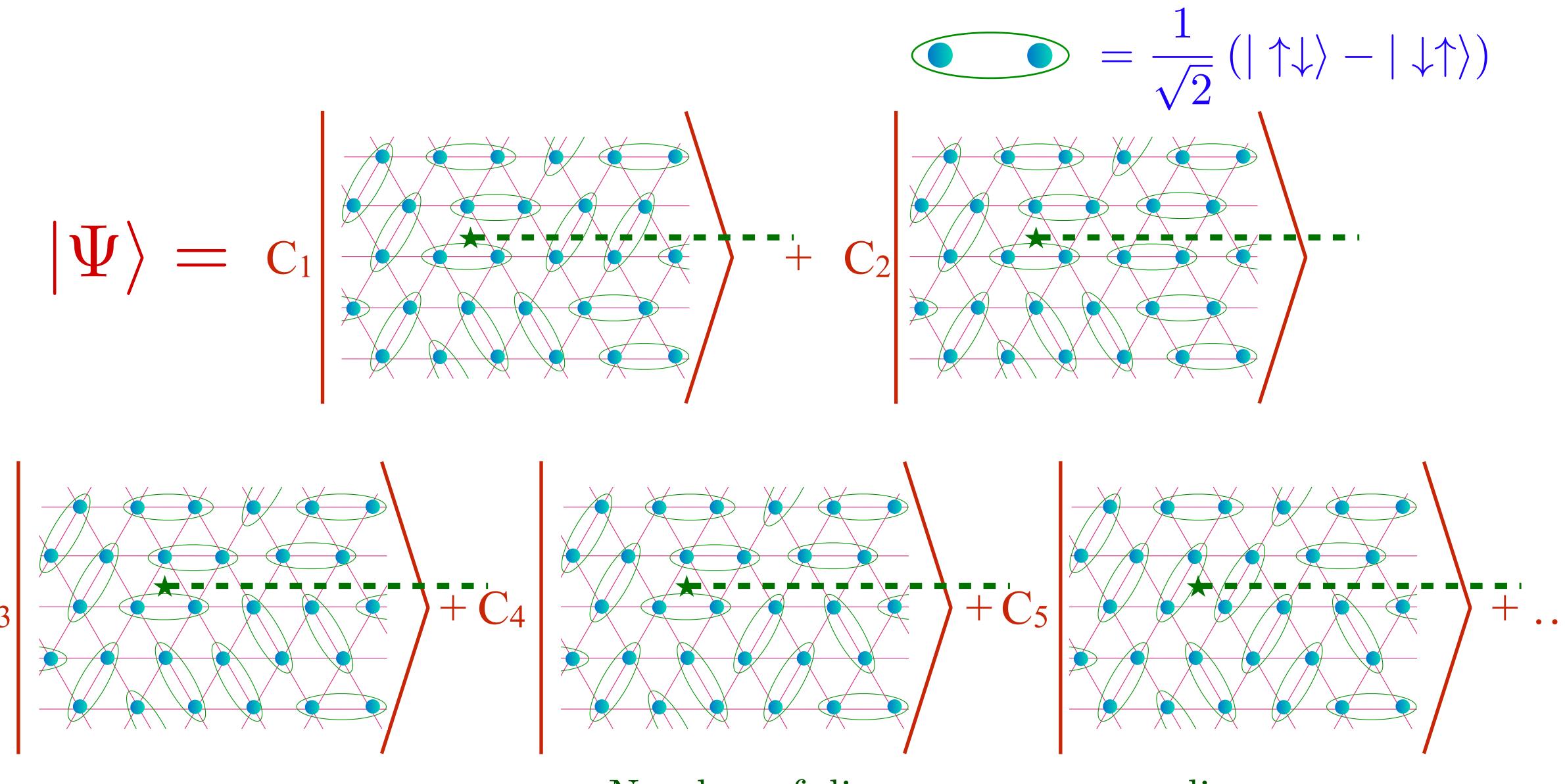




$$|\Psi
angle = c_1$$
 $|\Psi
angle = c_1$ $|\Psi
angle = c_1$



Another anyon—involves subtle changes in sign of superposition



$$C_n \Rightarrow C_n (-1)^{\text{Number of dimers across green line}}$$

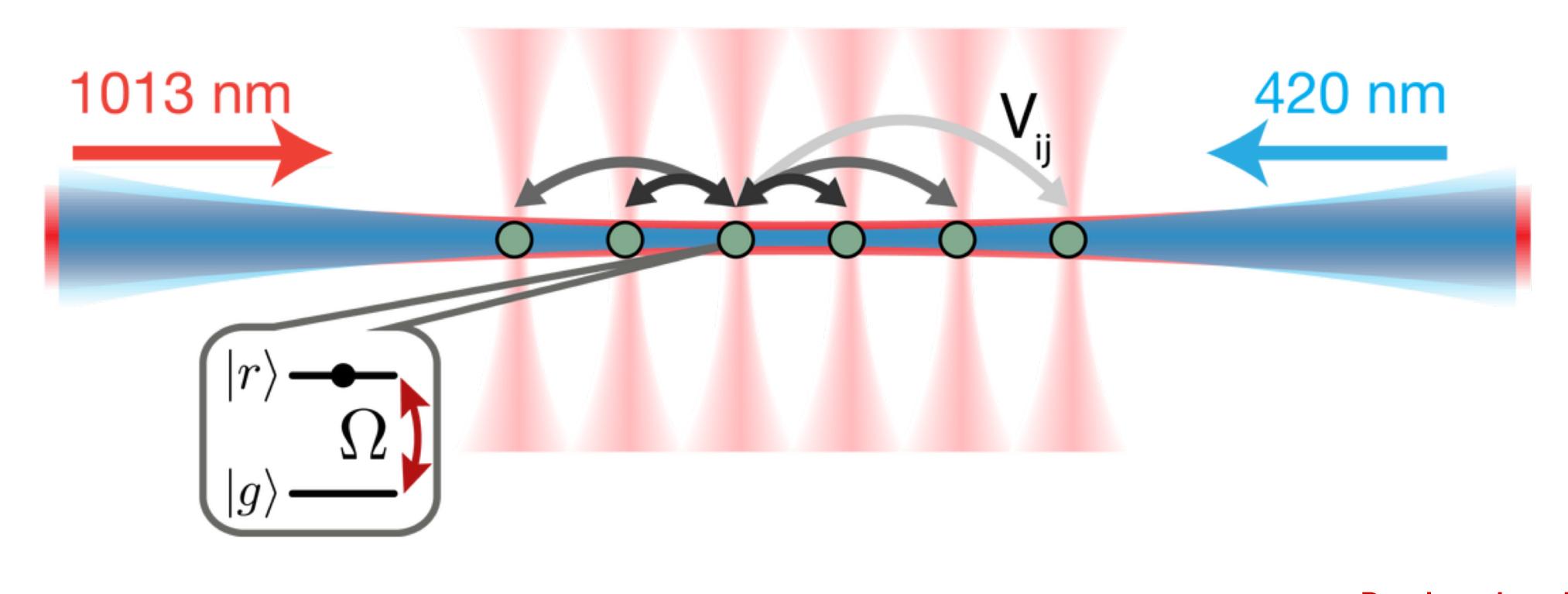
Read and Sachdev (1990):

Determined the anyon structure of the resonating valence bond spin liquid.

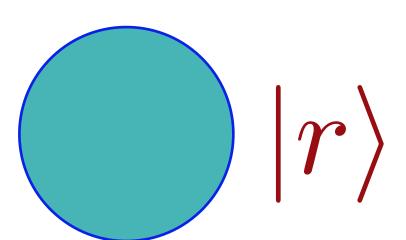
The anyon structure of this spin liquid is the same as Kitaev's $toric\ code\ (1997)$.

Kitaev (1997): Place the quantum information in a superposition of anyon sectors for fault-tolerant quantum computation.

Qubits using Rydberg atoms in optical tweezers



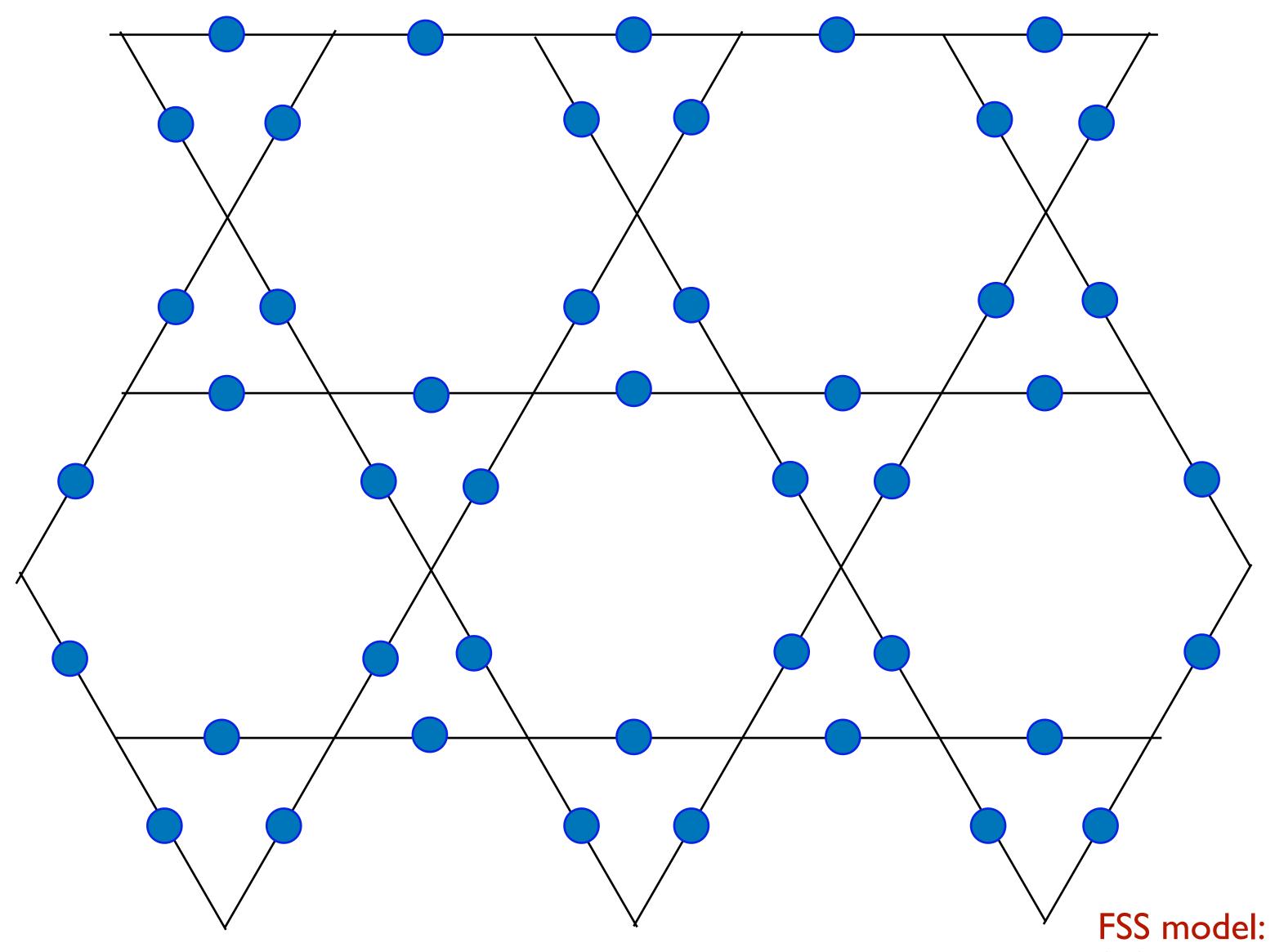
 \bullet $|g\rangle$



Realized at Raman Research Institute by Prof. Sanjukta Roy

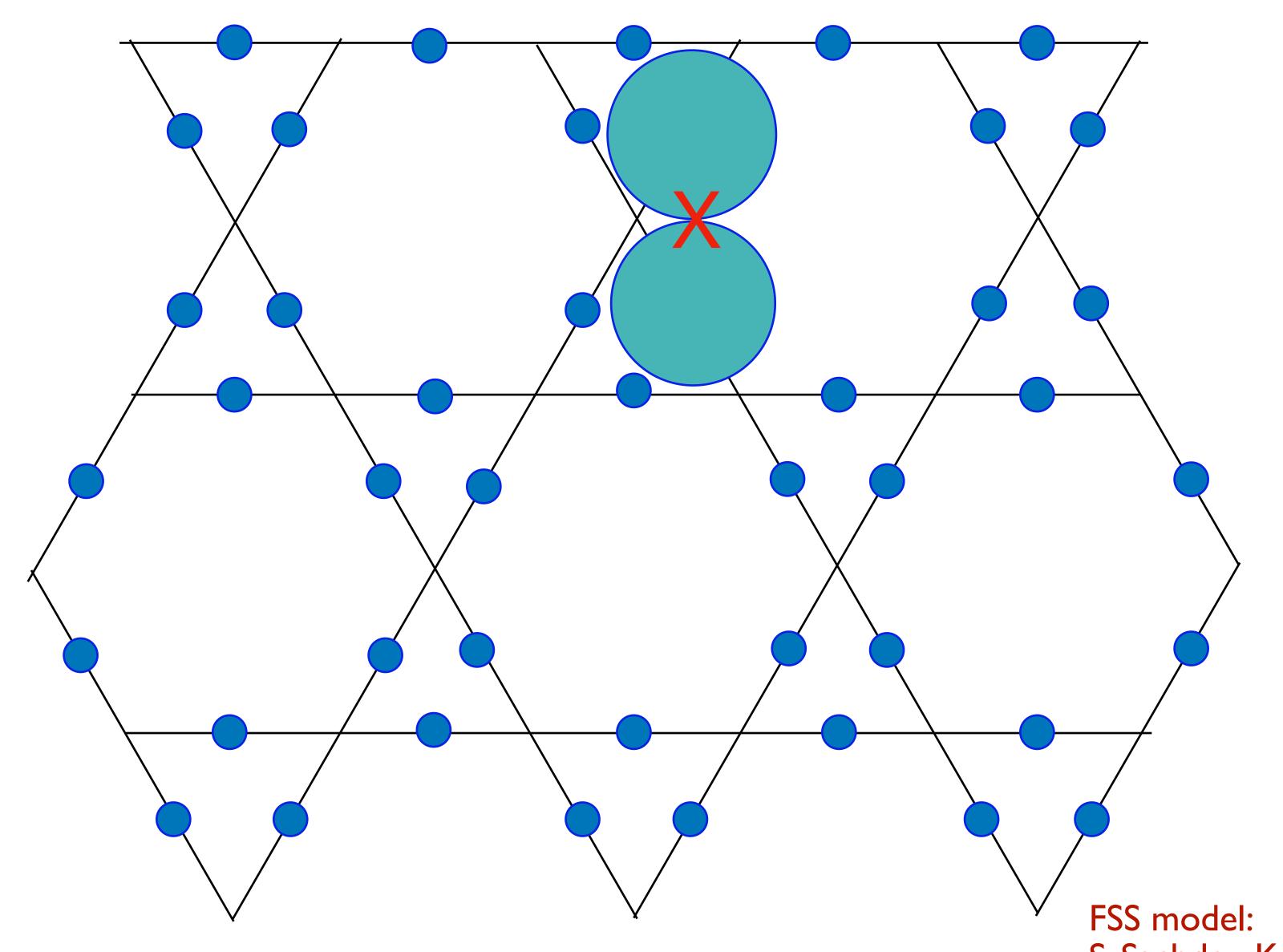
S. Ebadi, Tout T. Wang, H. Levine, A. Keesling, G. Semeghini, A. Omran, D. Bluvstein, R. Samajdar, H. Pichler, Wen Wei Ho, Soonwon Choi, S. Sachdev, M. Greiner, V. Vuletić, and M. D. Lukin, Nature **595**, 227 (2021)

Entangling Rydberg atom qubits



S. Sachdev, K. Sengupta, and S.M. Girvin, PRB **66**, 075128 (2002) P. Fendley, K. Sengupta, S. Sachdev, PRB **69**, 075106 (2004)

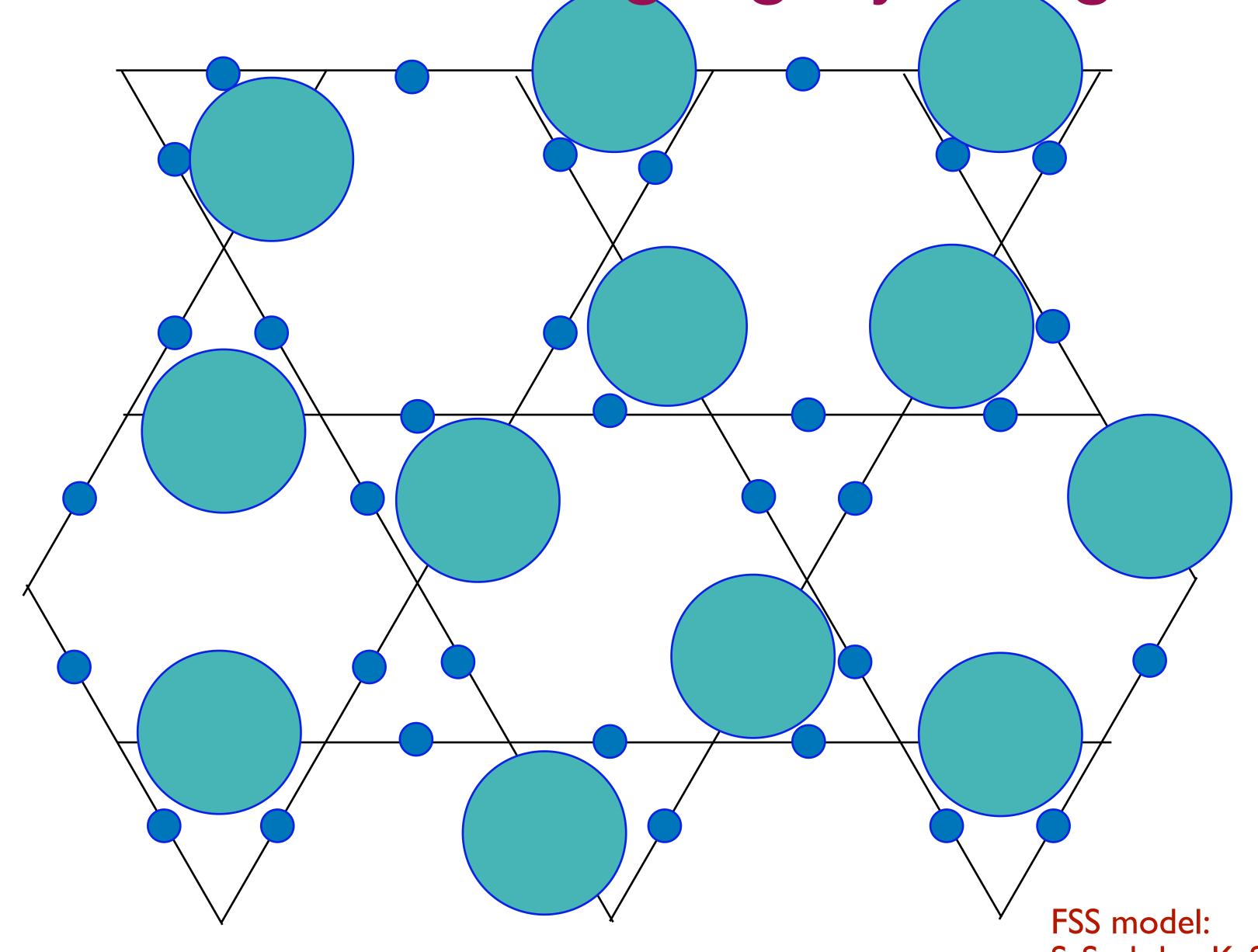
Entangling Rydberg atom qubits



NOT ALLOWED

S. Sachdev, K. Sengupta, and S.M. Girvin, PRB **66**, 075128 (2002) P. Fendley, K. Sengupta, S. Sachdev, PRB **69**, 075106 (2004)

Entangling Rydberg atom qubits

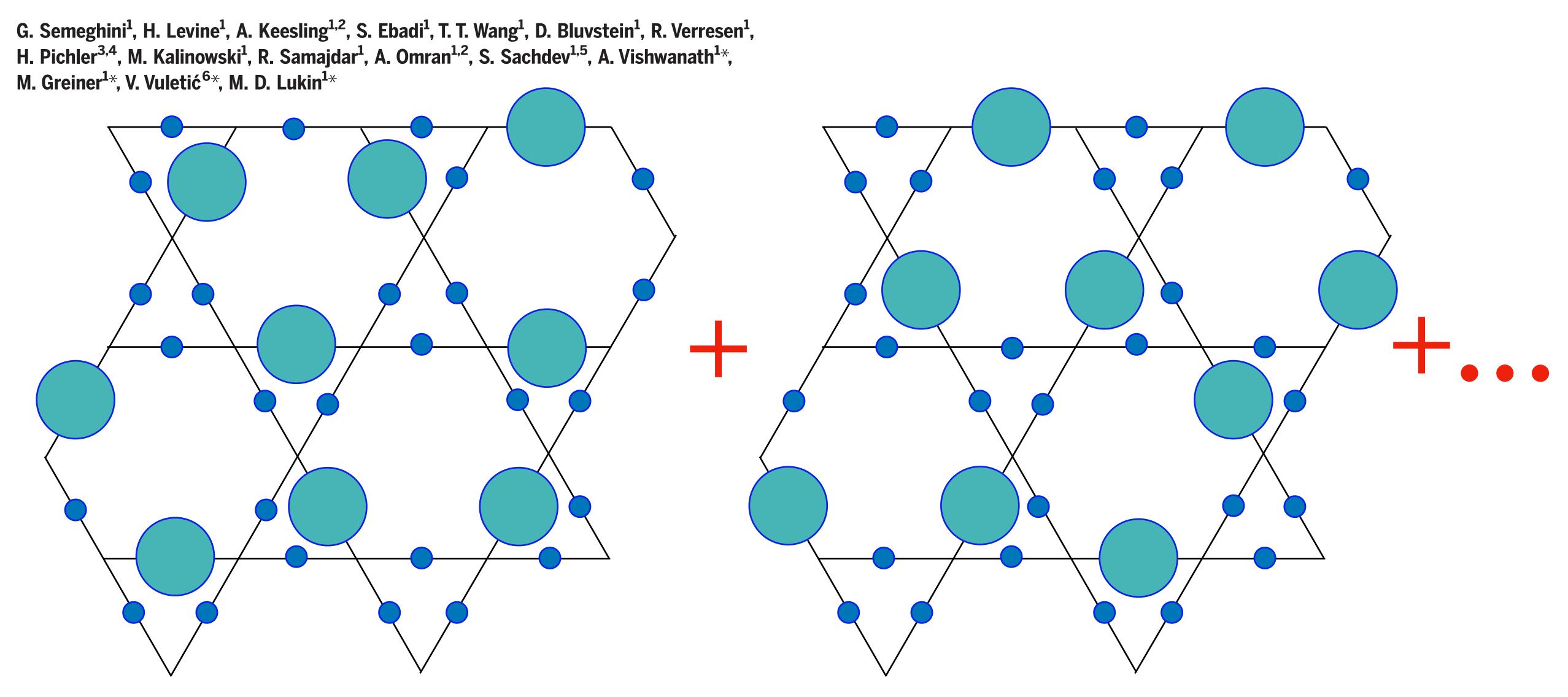


ALLOWED

S. Sachdev, K. Sengupta, and S.M. Girvin, PRB **66**, 075128 (2002) P. Fendley, K. Sengupta, S. Sachdev, PRB **69**, 075106 (2004)

Probing topological spin liquids on a programmable quantum simulator

Science 374, 1242-1247 (2021)



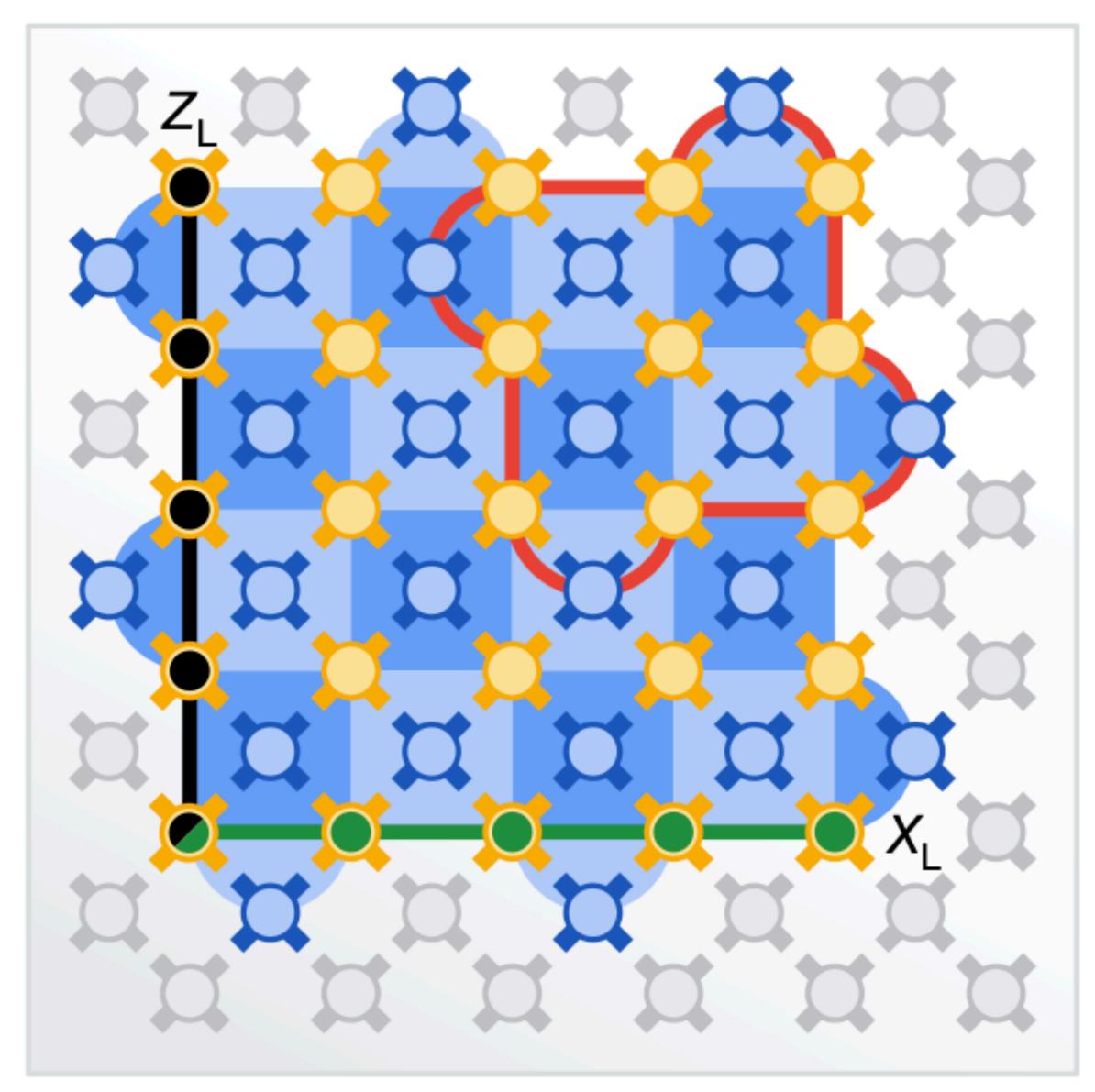
Entanglement similar to that in a RVB spin liquid

Suppressing quantum errors by scaling a surface code logical qubit

Google Quantum AI*

676 | Nature | Vol 614 | 23 February 2023

"Surface code" is closely related to the "toric code"



Suppressing quantum errors by scaling a

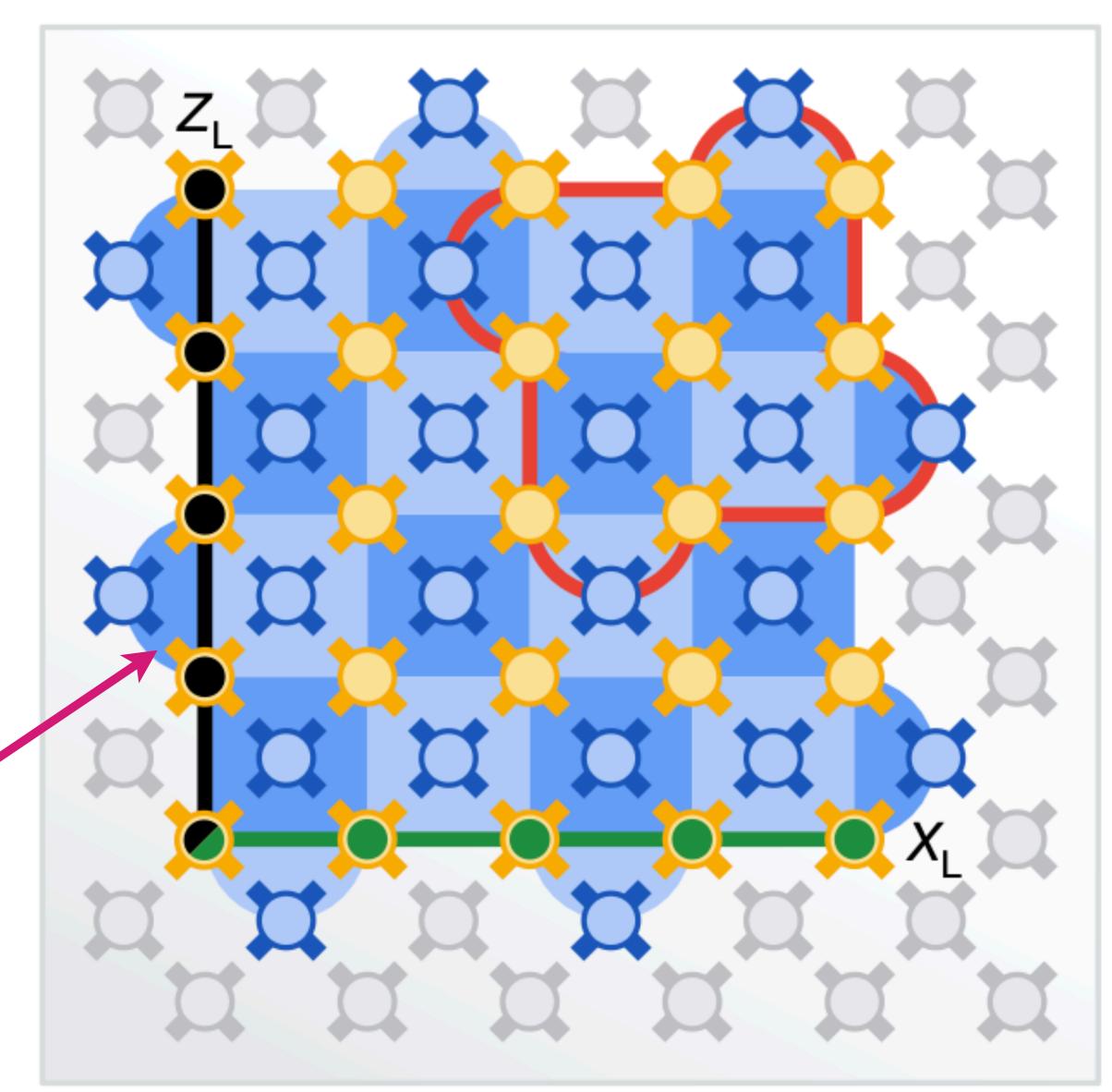
surface code logical qubit

Google Quantum AI*

676 | Nature | Vol 614 | 23 February 2023

"Surface code" is closely related to the "toric code"

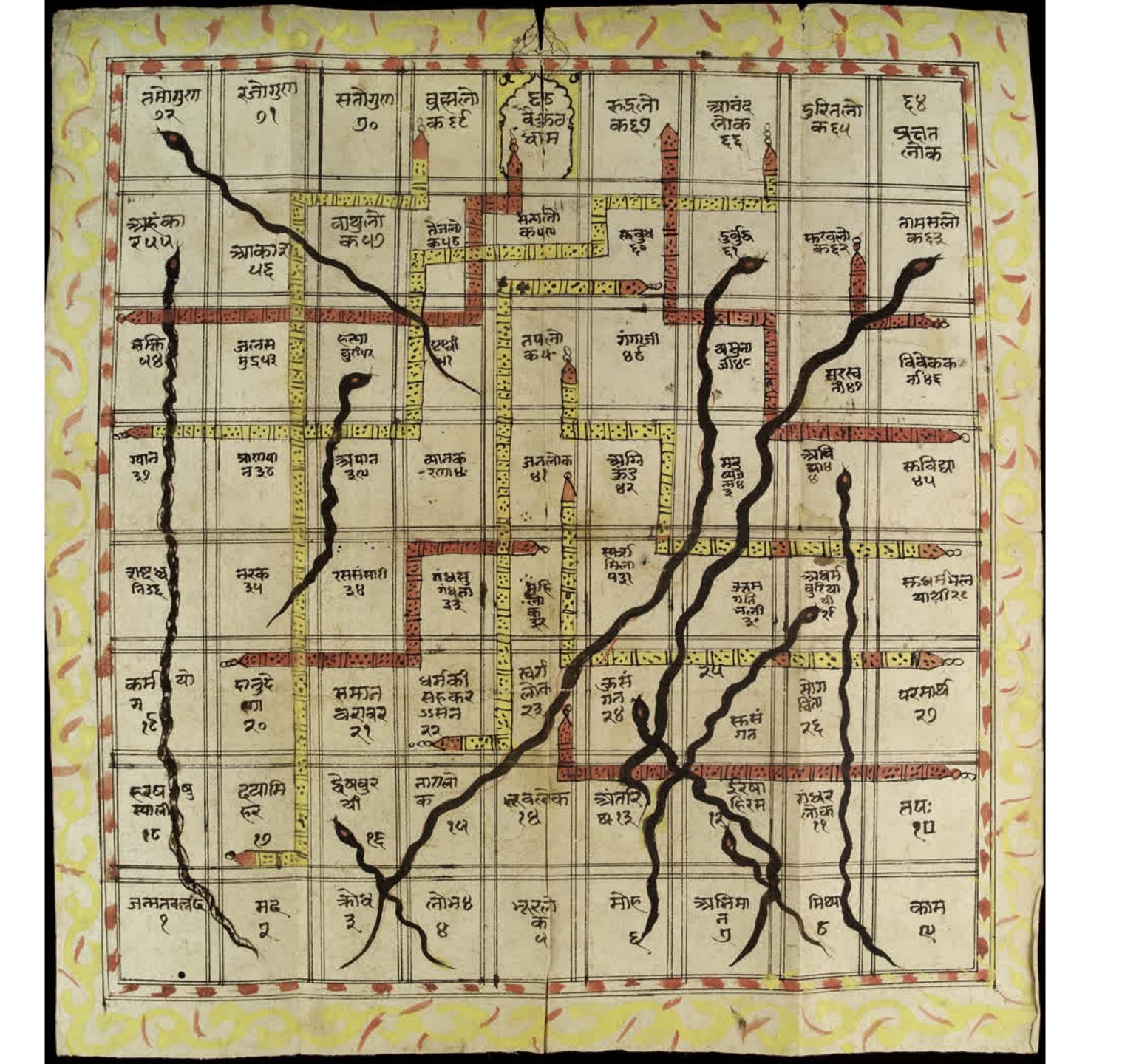
Nobel Prize today for one of these superconducting junctions!



Although it has had a dramatic impact on theory/experiments on fault-tolerant quantum computations,
the theory of spin liquids with well-defined anyons
does not solve the problem of
high temperature superconductivity in the cuprates

Although it has had a dramatic impact on theory/experiments on fault-tolerant quantum computations, the theory of spin liquids with well-defined anyons does not solve the problem of high temperature superconductivity in the cuprates

The Sachdev-Ye-Kitaev model of entanglement of mobile fermions



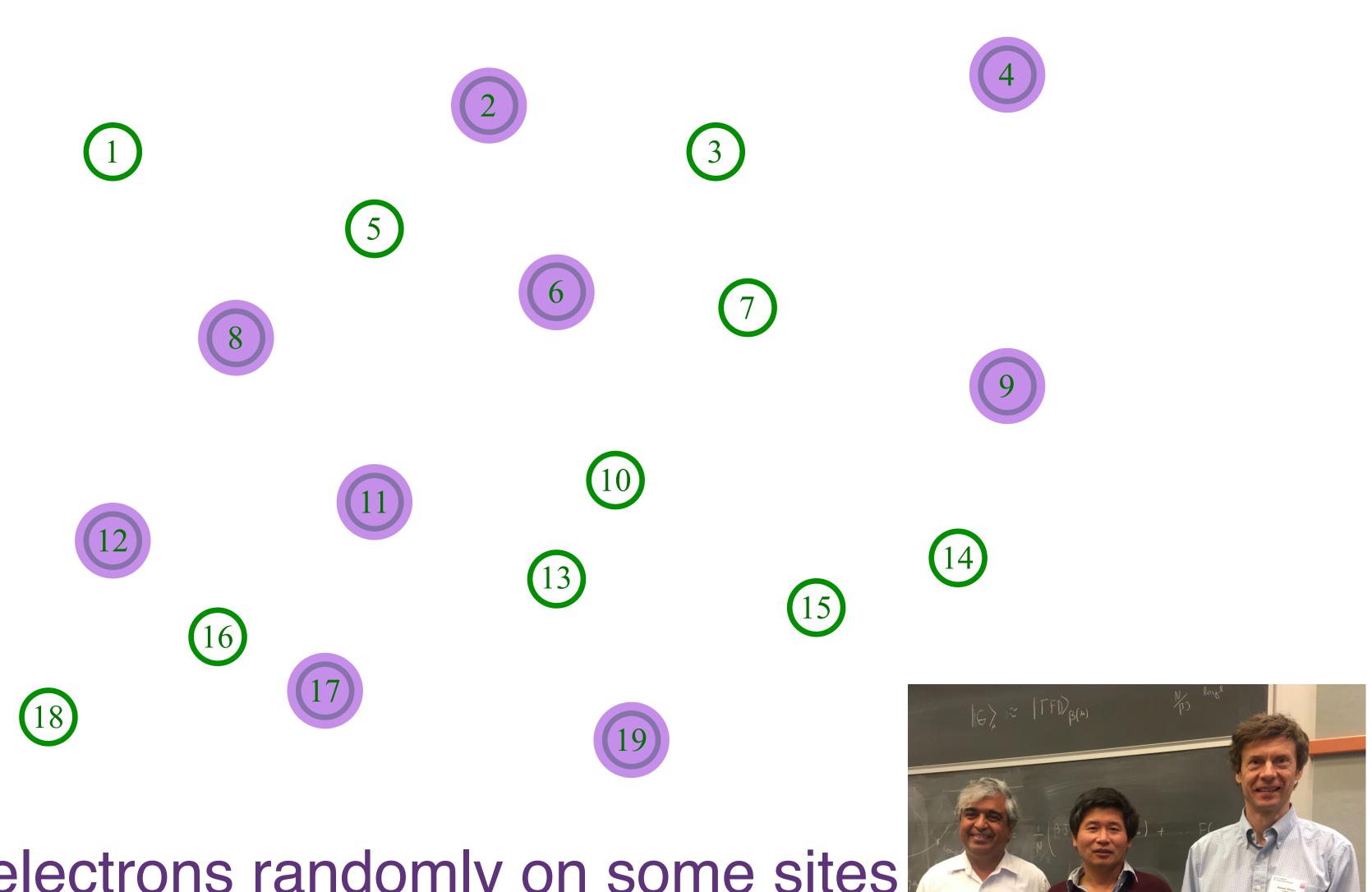
My spooky dream*

Ancient Indian game of Snakes and Ladders

*Not true

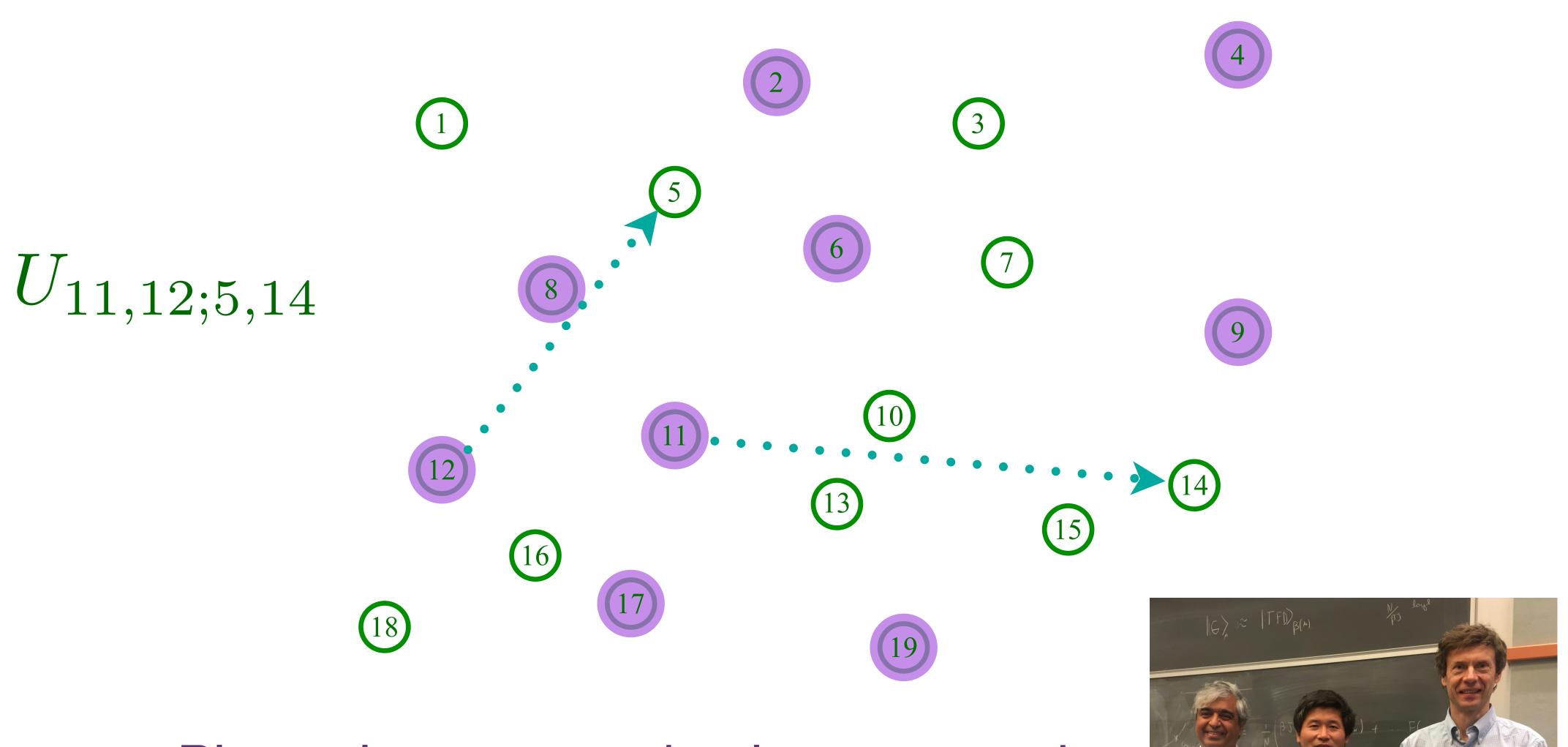


Sachdev, Ye (1993); Kitaev (2015)

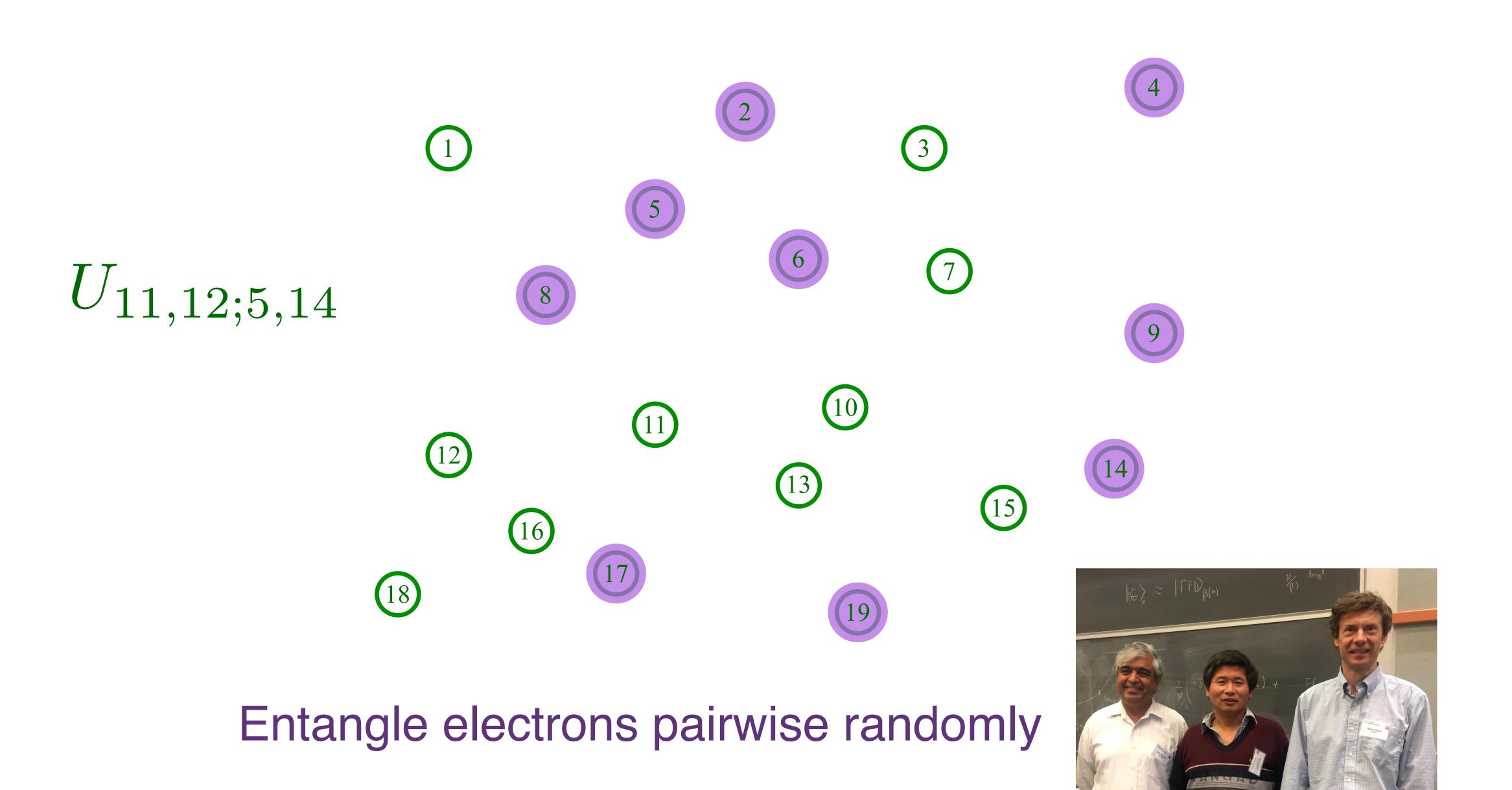


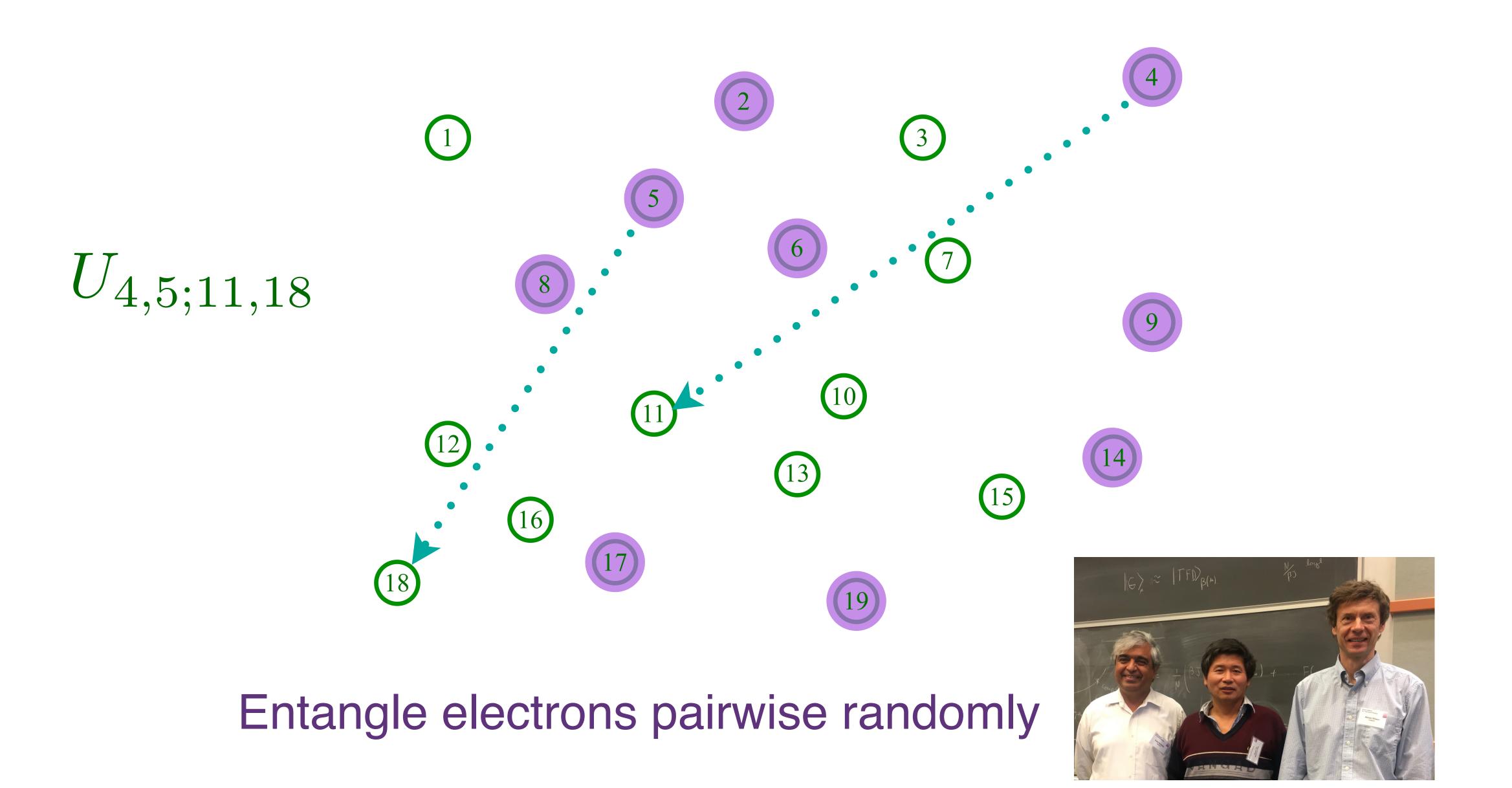
Place electrons randomly on some sites

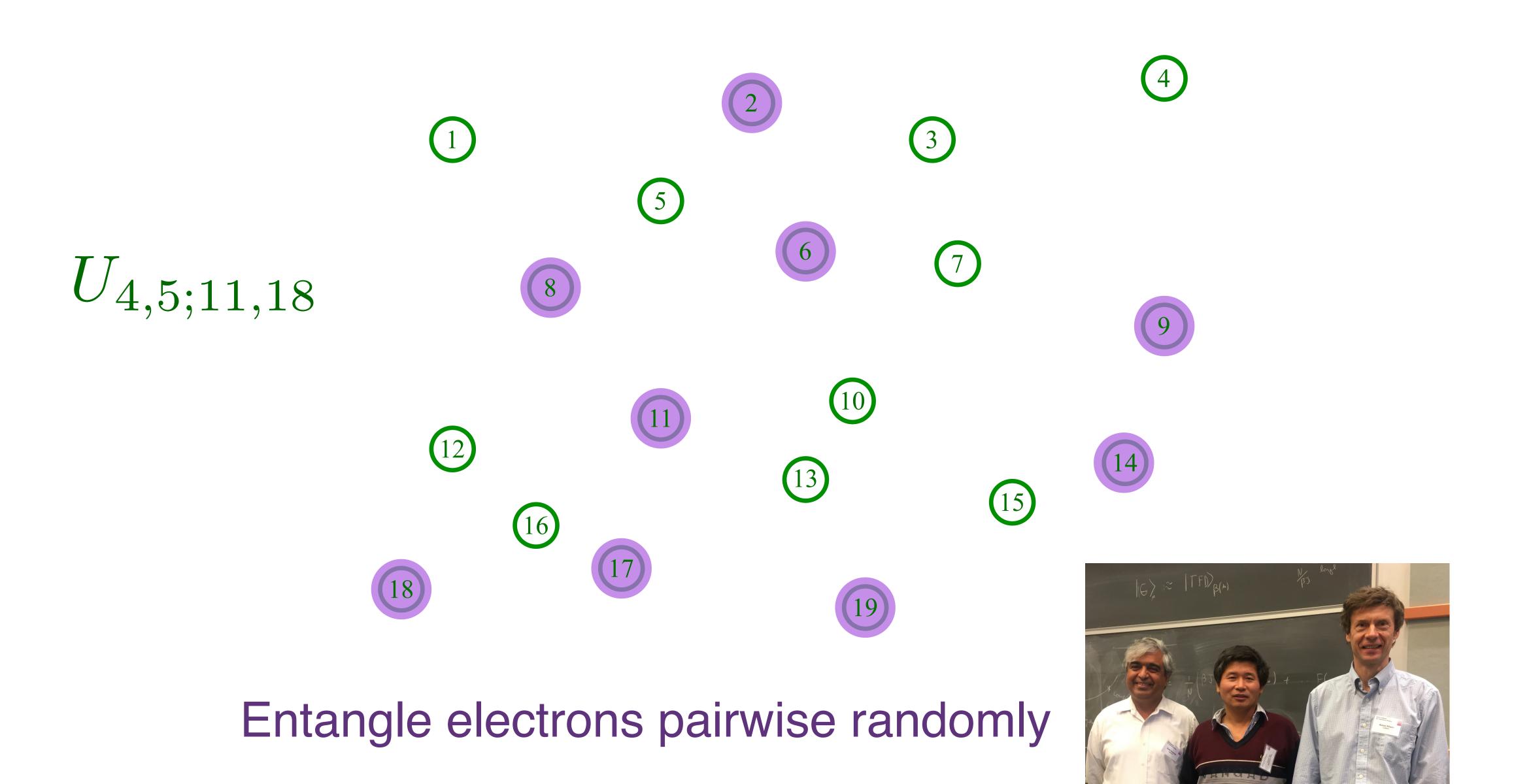
Sachdev, Ye (1993); Kitaev (2015)

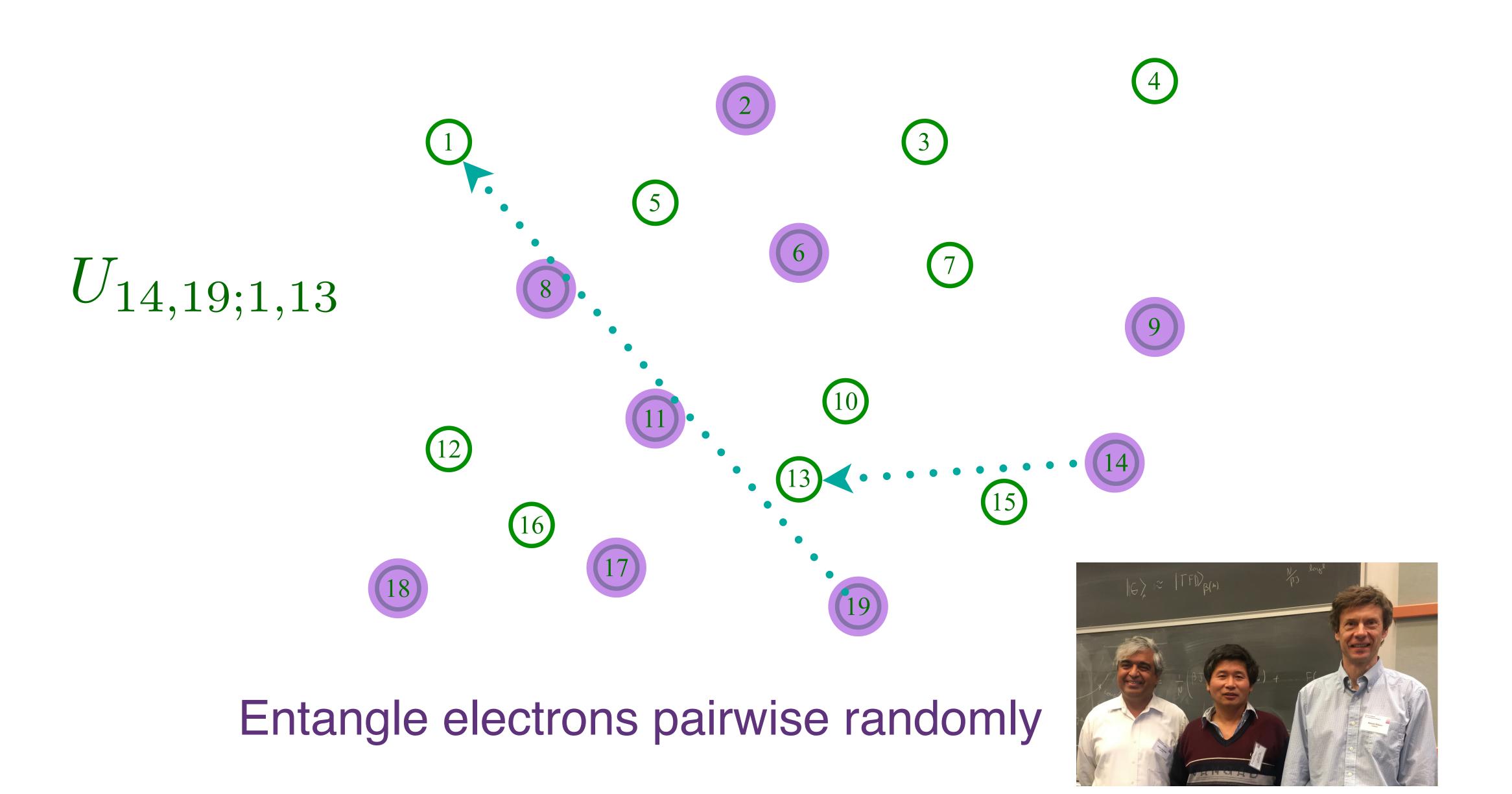


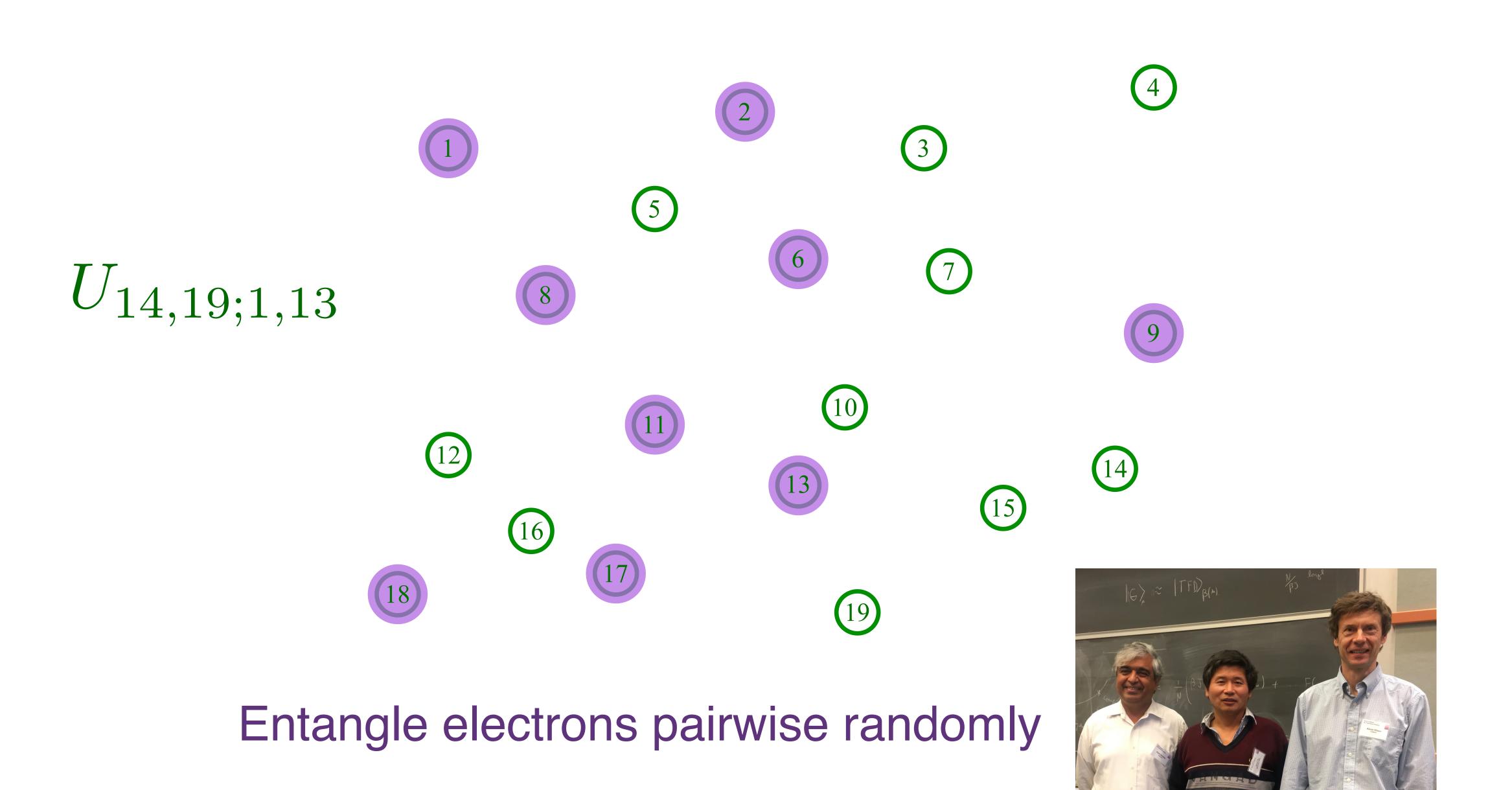
Place electrons randomly on some sites

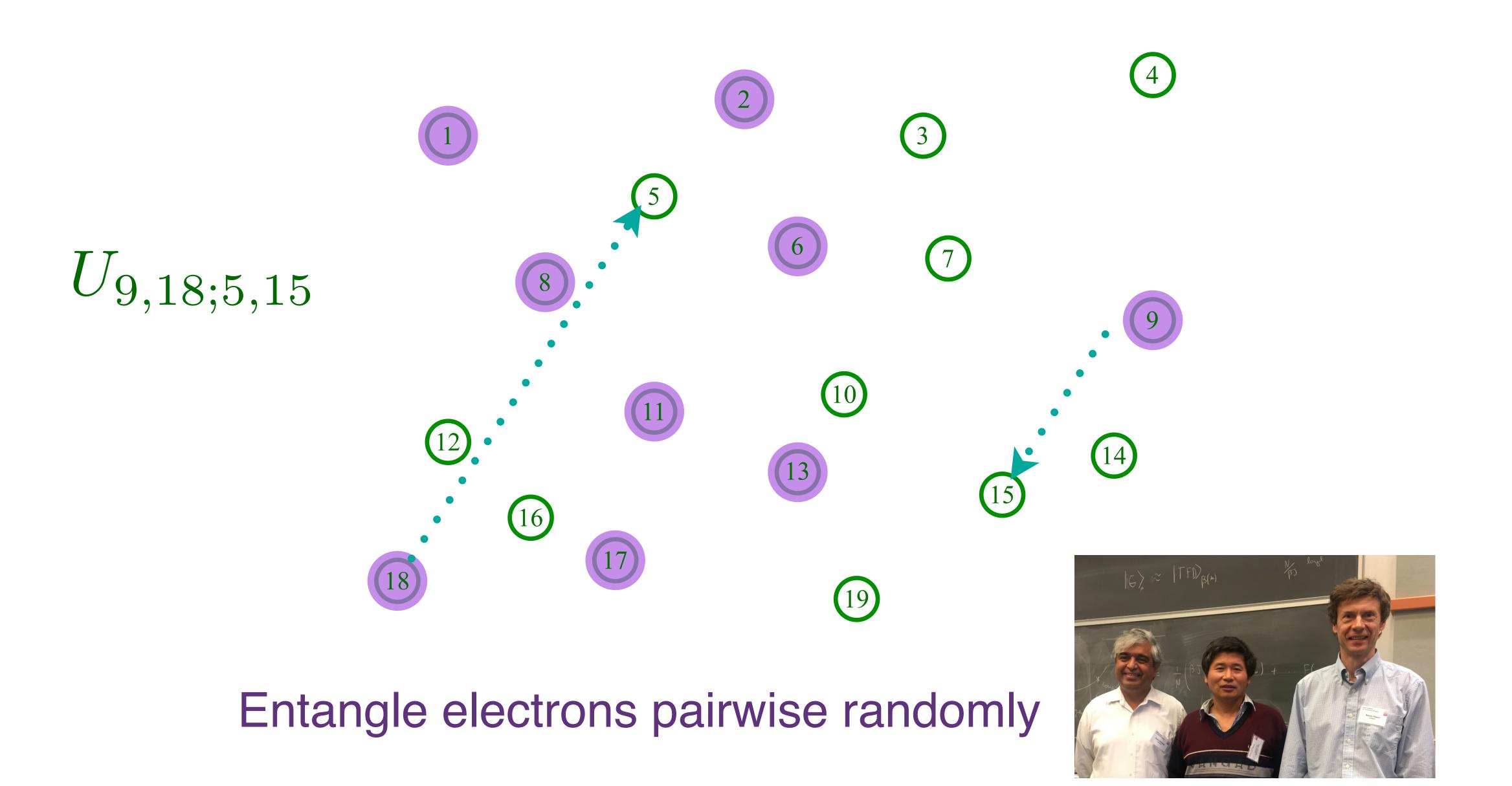


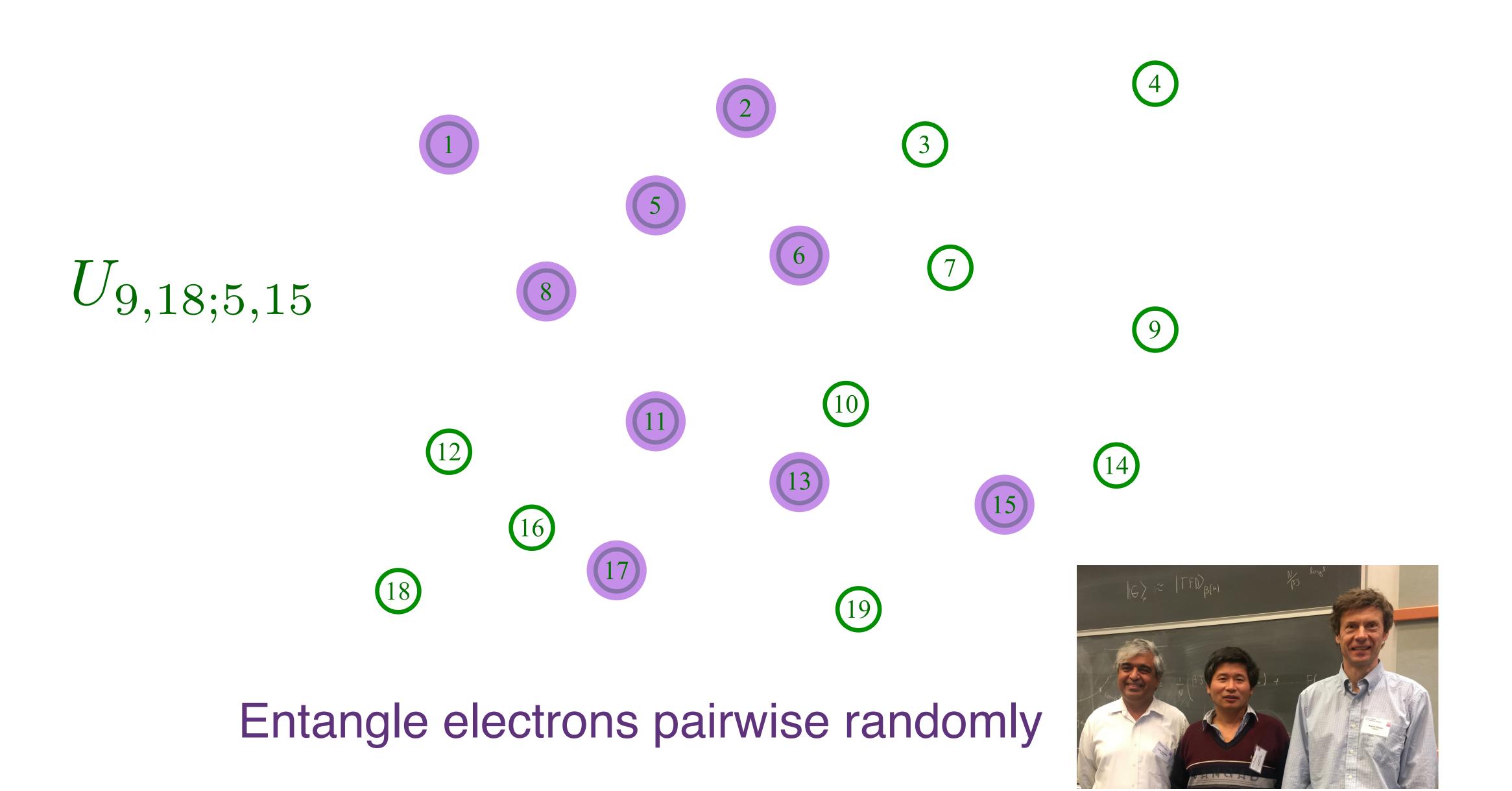


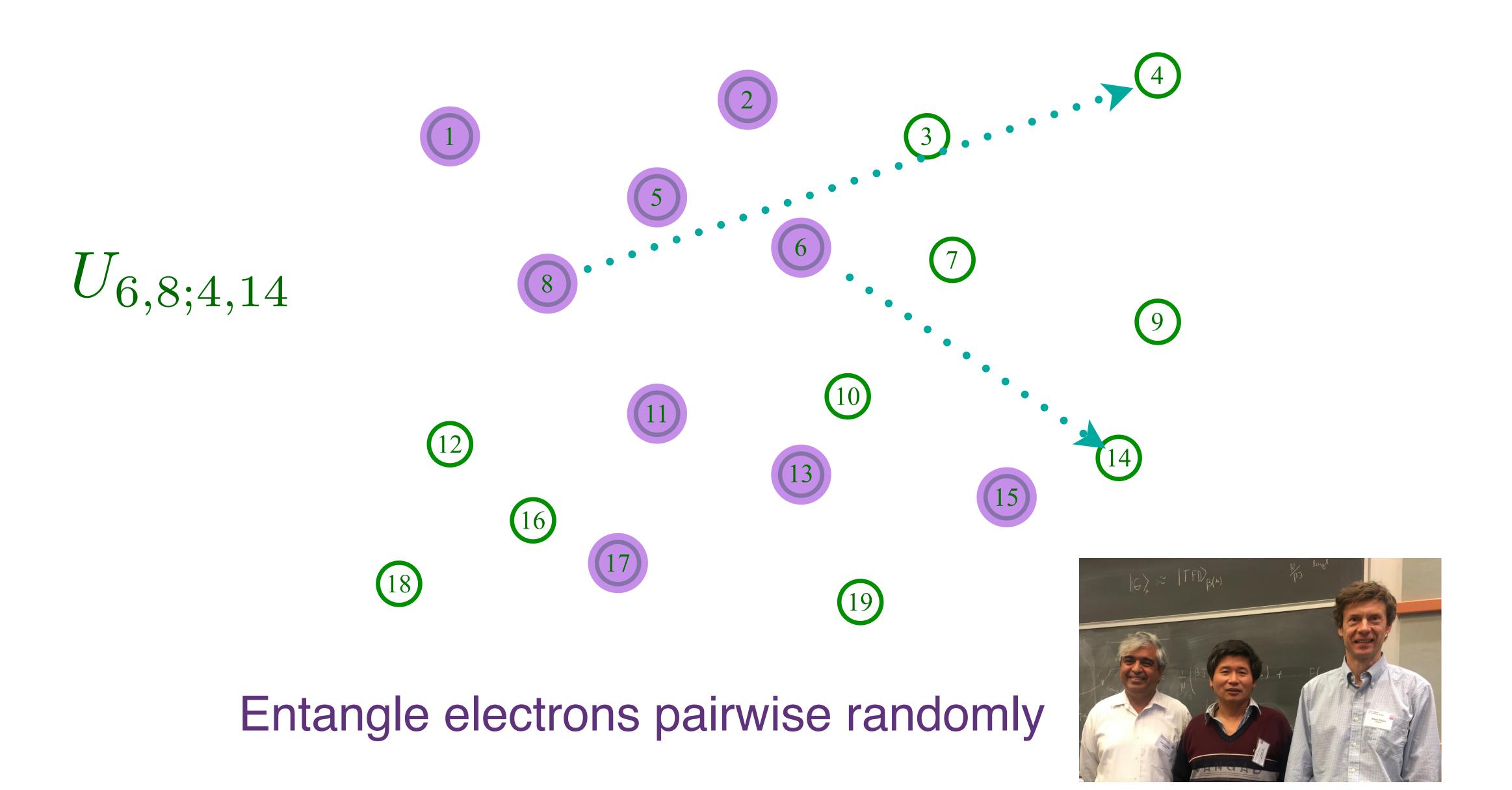




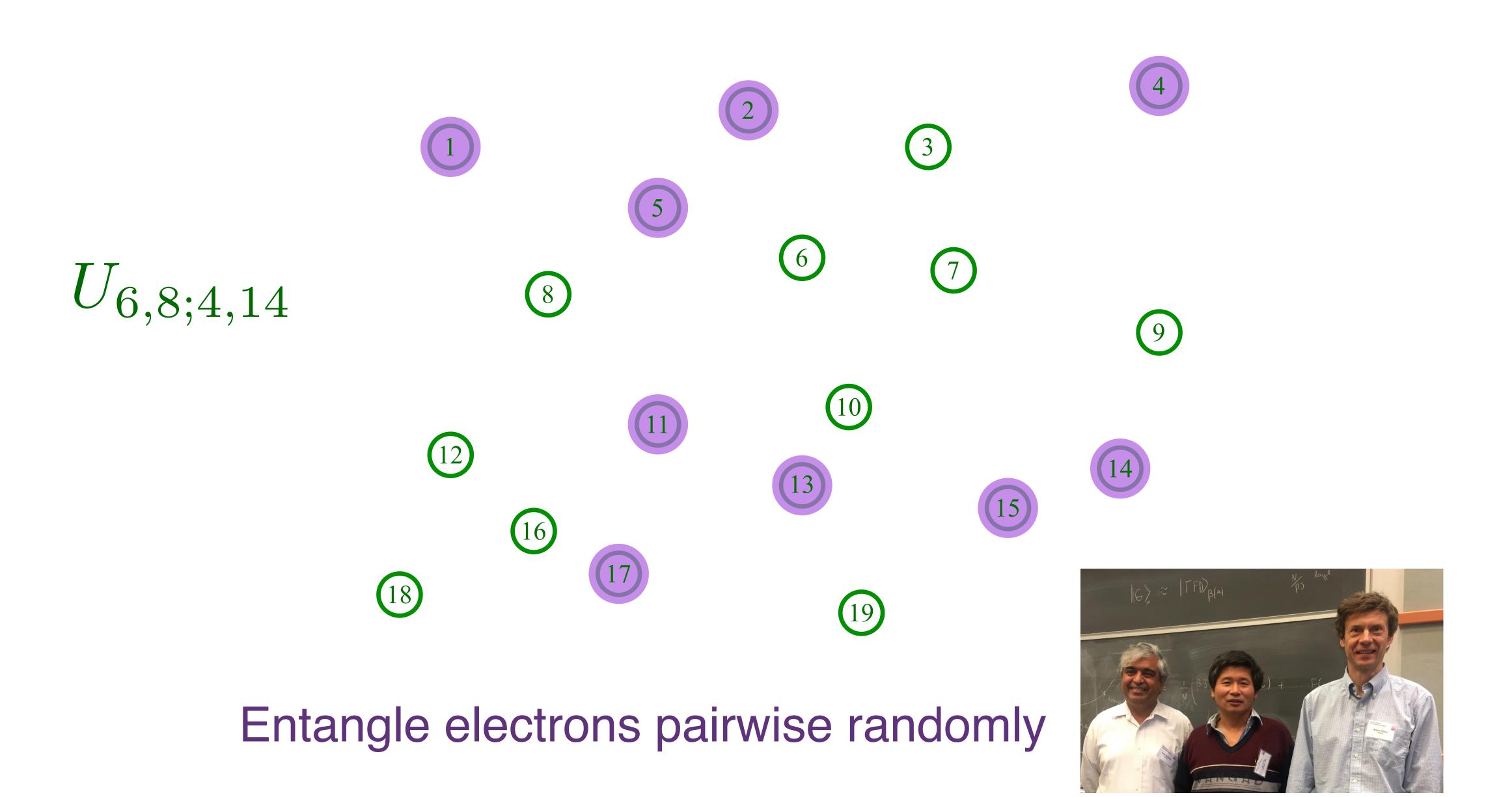








Sachdev, Ye (1993); Kitaev (2015)



Sachdev, Ye (1993); Kitaev (2015)

A solvable model of multi-particle quantum entanglement.

Sachdev, Ye (1993); Kitaev (2015)

Yields a quantum state whose excitations are not particle-like i.e. no bosons, fermions, anyons....

Sachdev, Ye (1993); Kitaev (2015)

Yields a quantum state whose excitations are not particle-like i.e. no bosons, fermions, anyons....

Current is carried by an "entangled quantum soup"

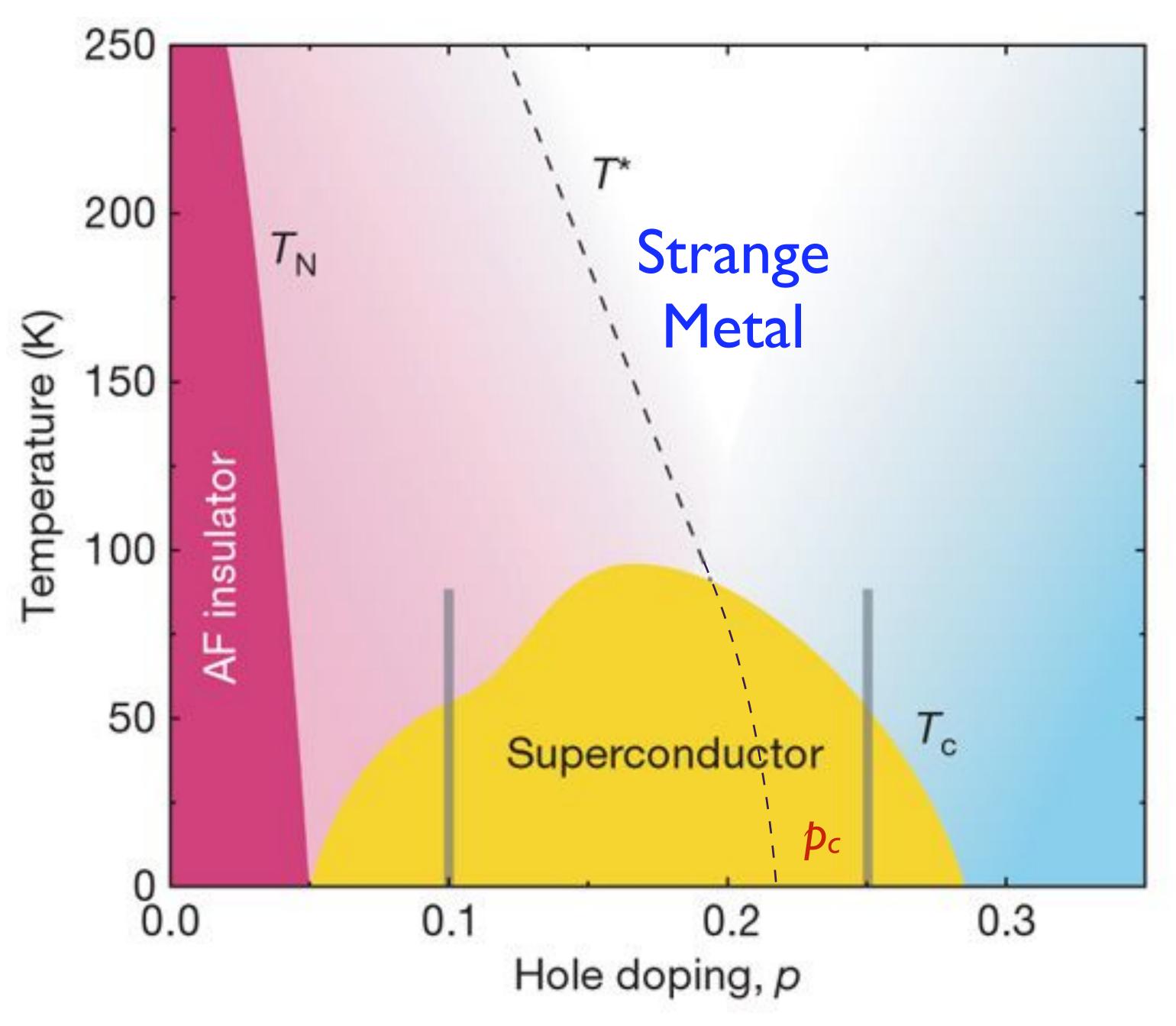
Sachdev, Ye (1993); Kitaev (2015)

Yields a quantum state whose excitations are not particle-like i.e. no bosons, fermions, anyons....

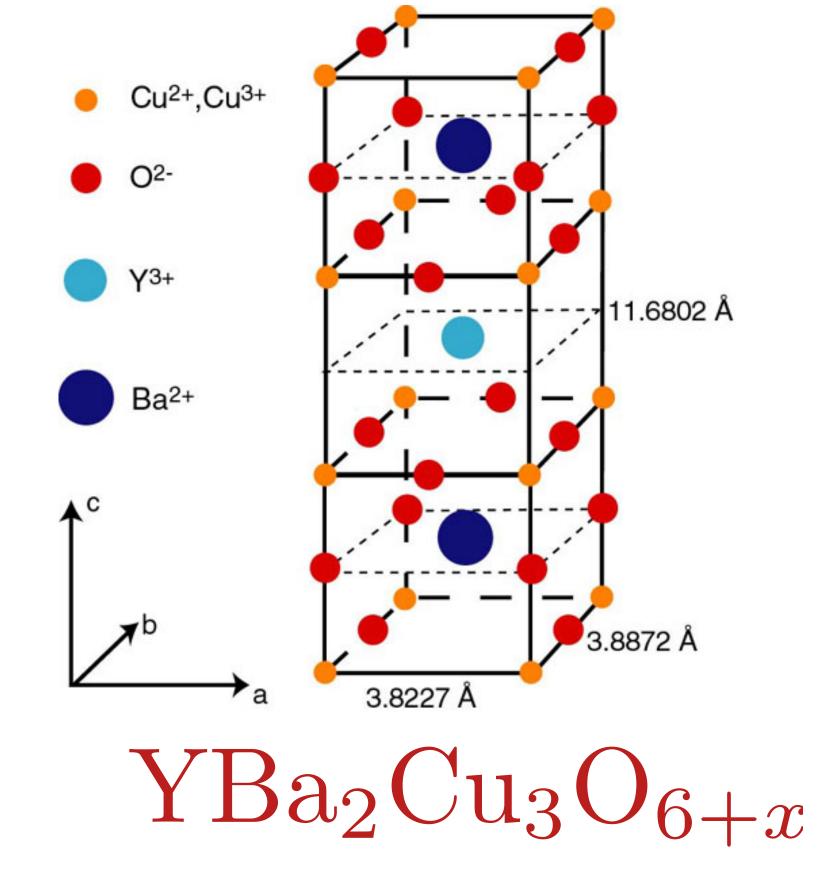
A key consequence of the absence of the particle-like excitations is <u>Universal Planckian Dissipation</u>. The relaxation time, τ , when perturbed at a frequency ω is given by

$$\tau = \frac{\hbar}{k_B T} F \left(\frac{\hbar \omega}{k_B T} \right)$$

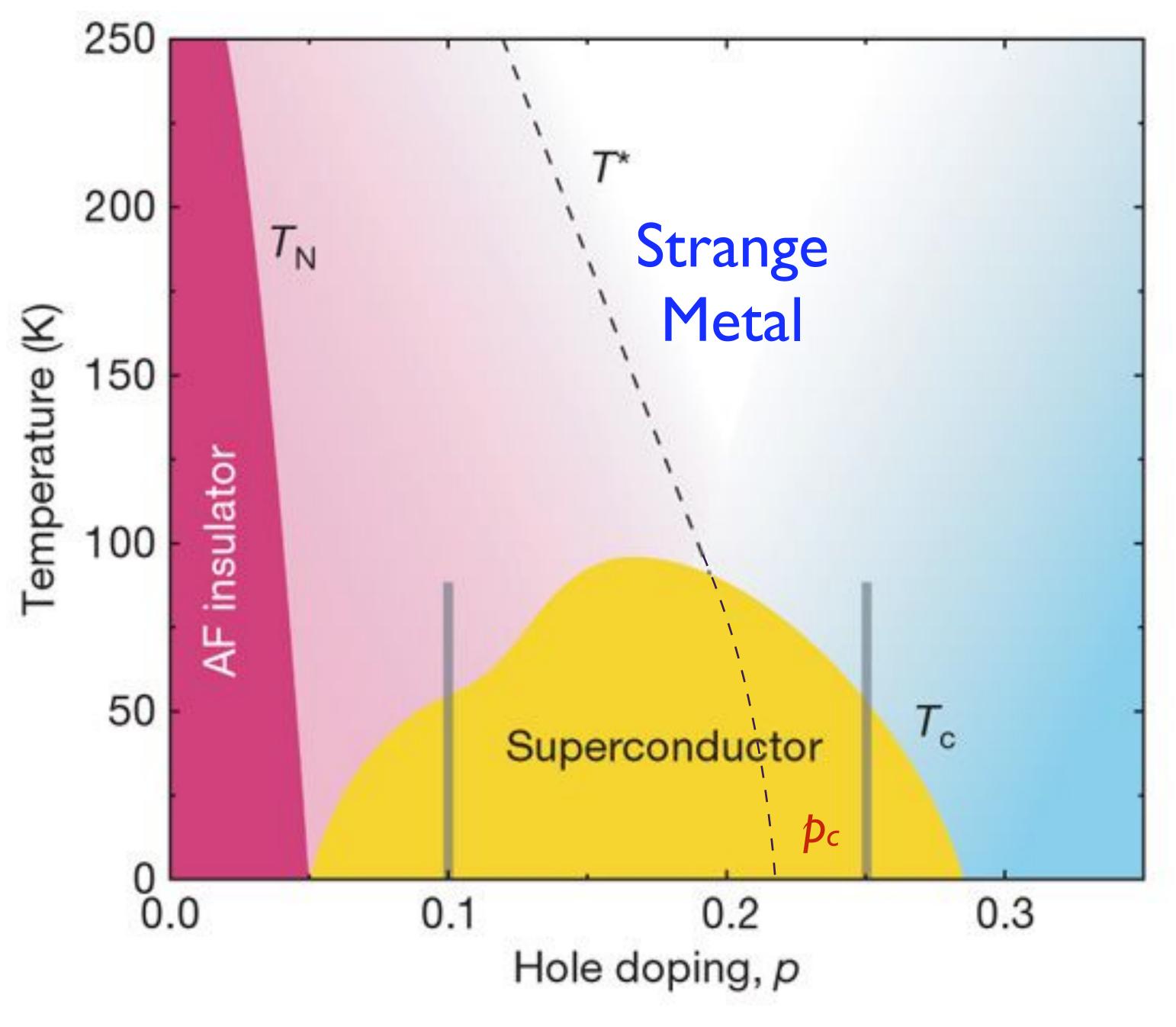
where \hbar is Planck's constant, T is temperature, and the function F is independent of the strength of interaction between the particles.



Aavishkar A. Patel, Haoyu Guo, Ilya Esterlis, S. S., Science 381, 790 (2023)



The "strange metal" has no particle-like/anyon excitations and is described by a SYK-type theory

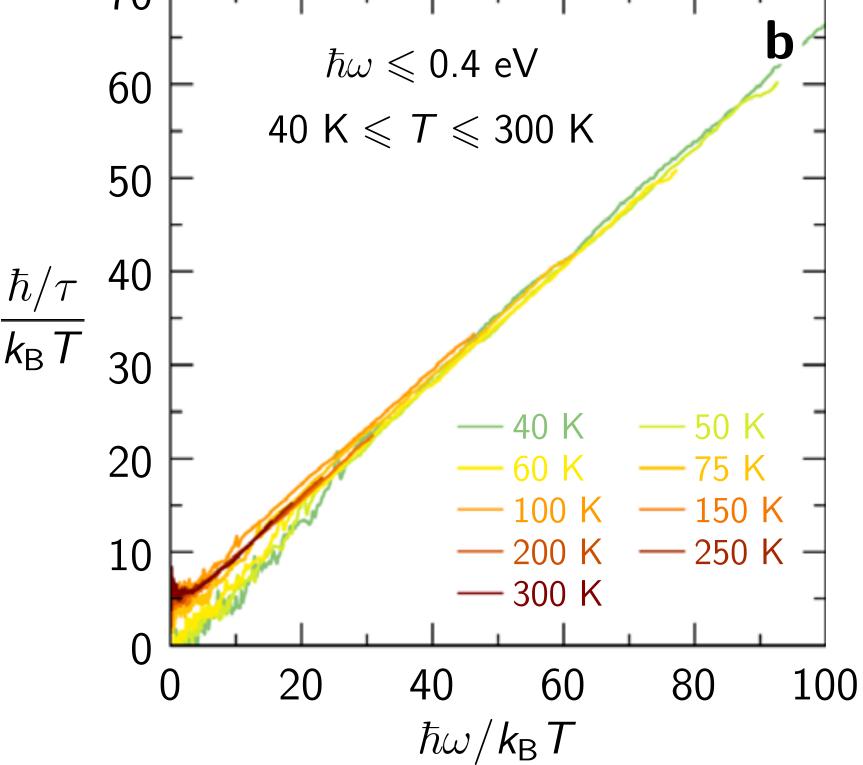


Aavishkar A. Patel, Haoyu Guo, Ilya Esterlis, S. S., Science 381, 790 (2023)

Planckian dynamics!

Electron scattering time τ from optical conductivity

$$\tau(\omega) = \frac{\hbar}{k_B T} F\left(\frac{\hbar\omega}{k_B T}\right)^{3}$$



B. Michon, C. Berthod, C.W. Rischau, A. Ataei, L. Chen, S. Komiya, S. Ono, L. Taillefer, D. van der Marel, A. Georges, Nature Comm. 14, 3033 (2023)

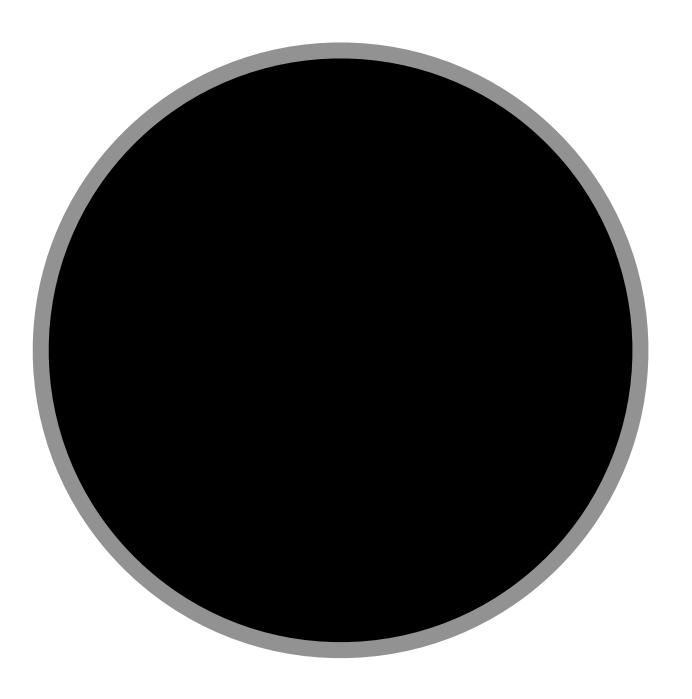
Quantum entanglement, the SYK model, and black holes

Black Holes

Objects so dense that light is gravitationally bound to them.

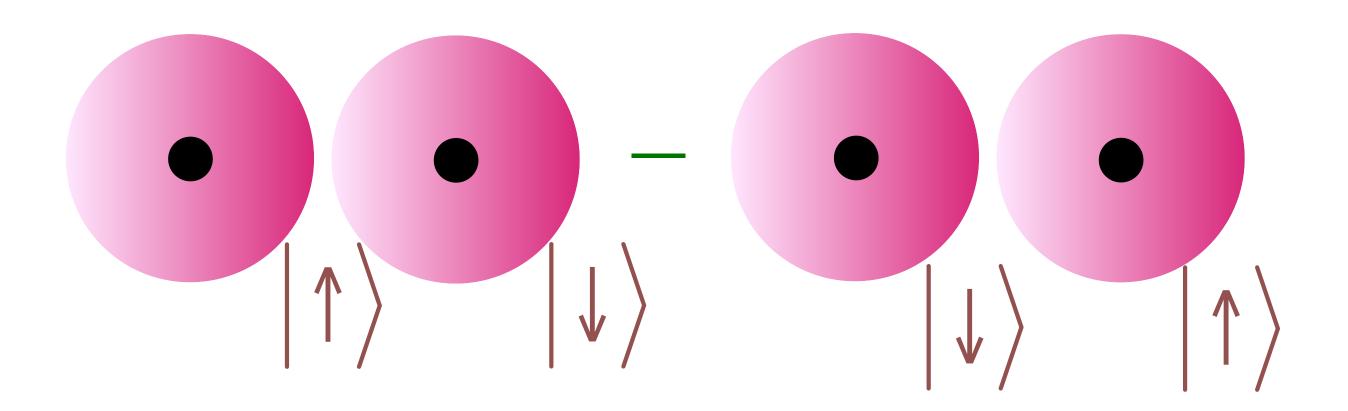


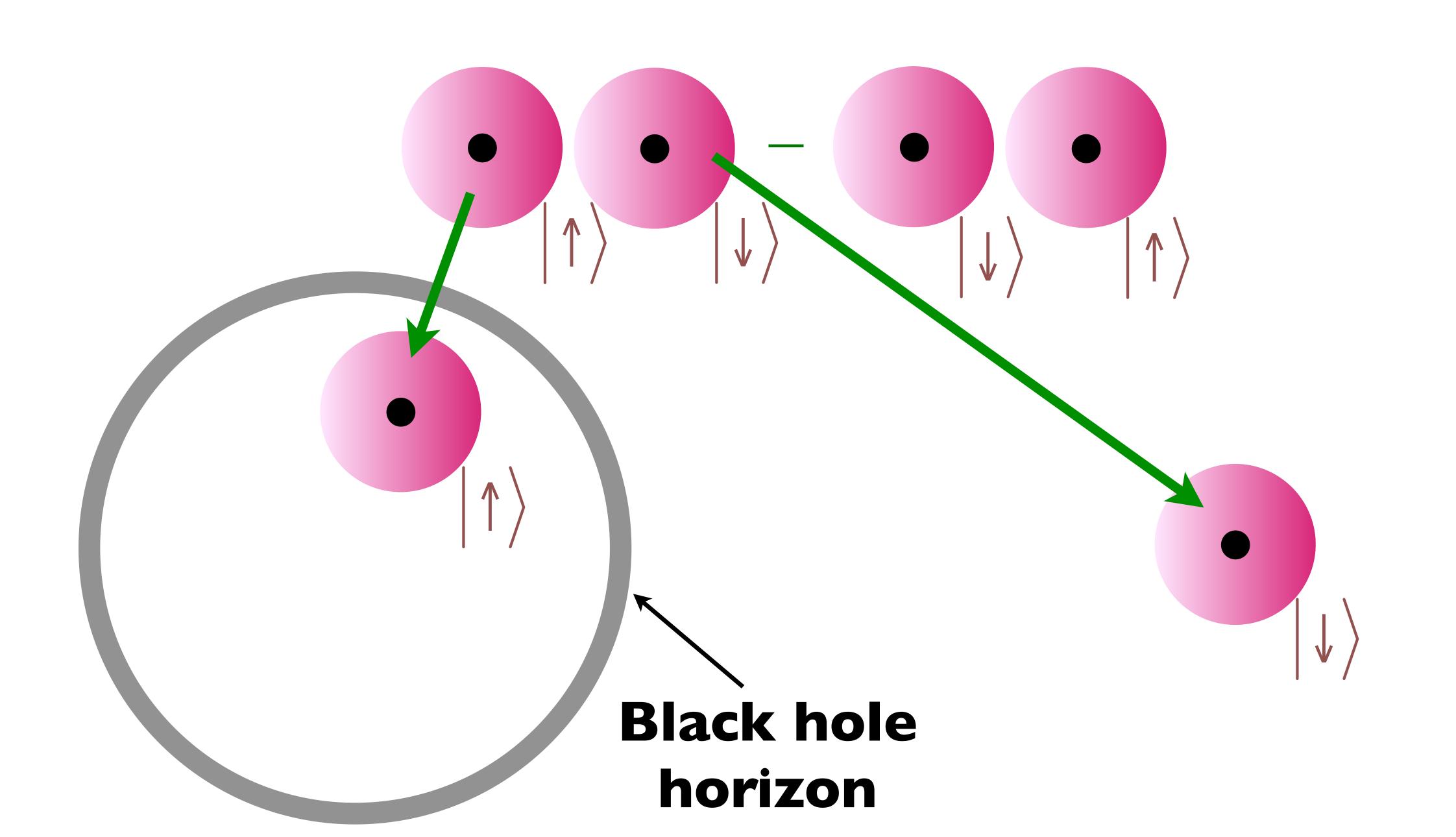
Horizon radius
$$R = \frac{2GM}{c^2}$$

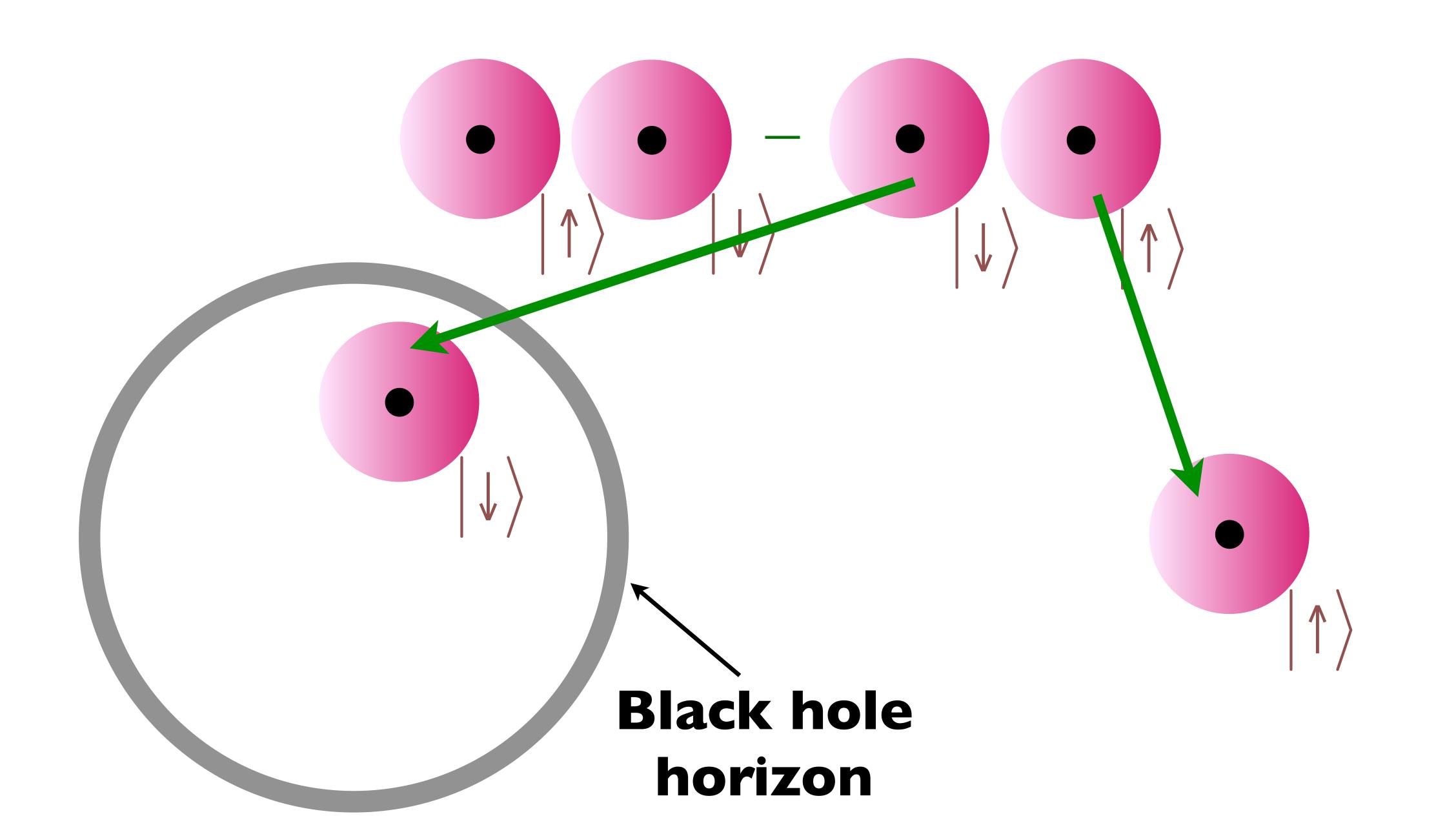


Karl Schwarzschild (1916)

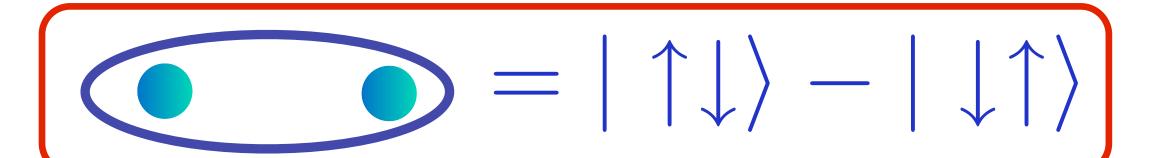
G Newton's constant, c velocity of light, M mass of black hole For M = earth's mass, $R \approx 9 \, mm!$

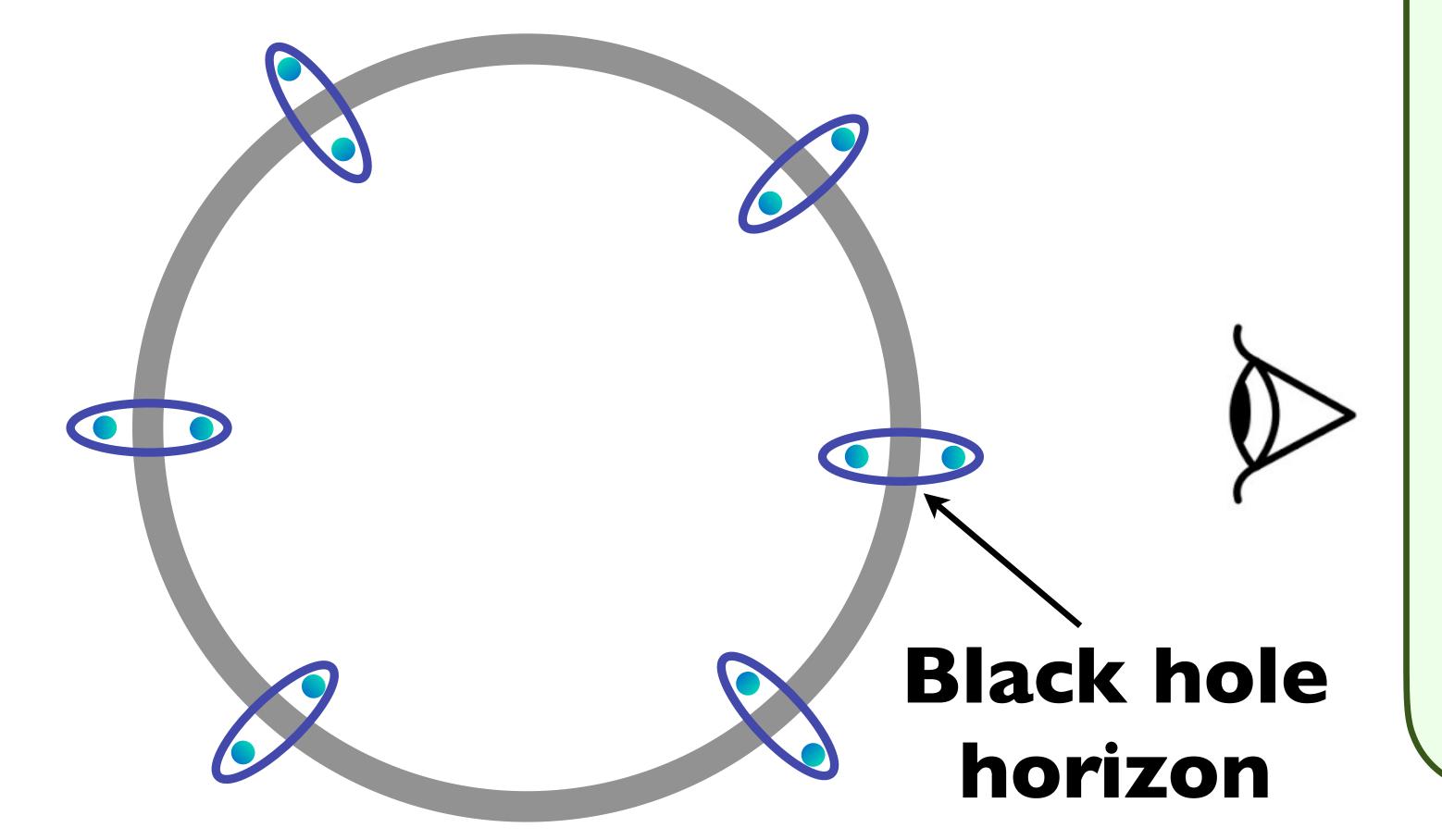






Quantum entanglement on the surface



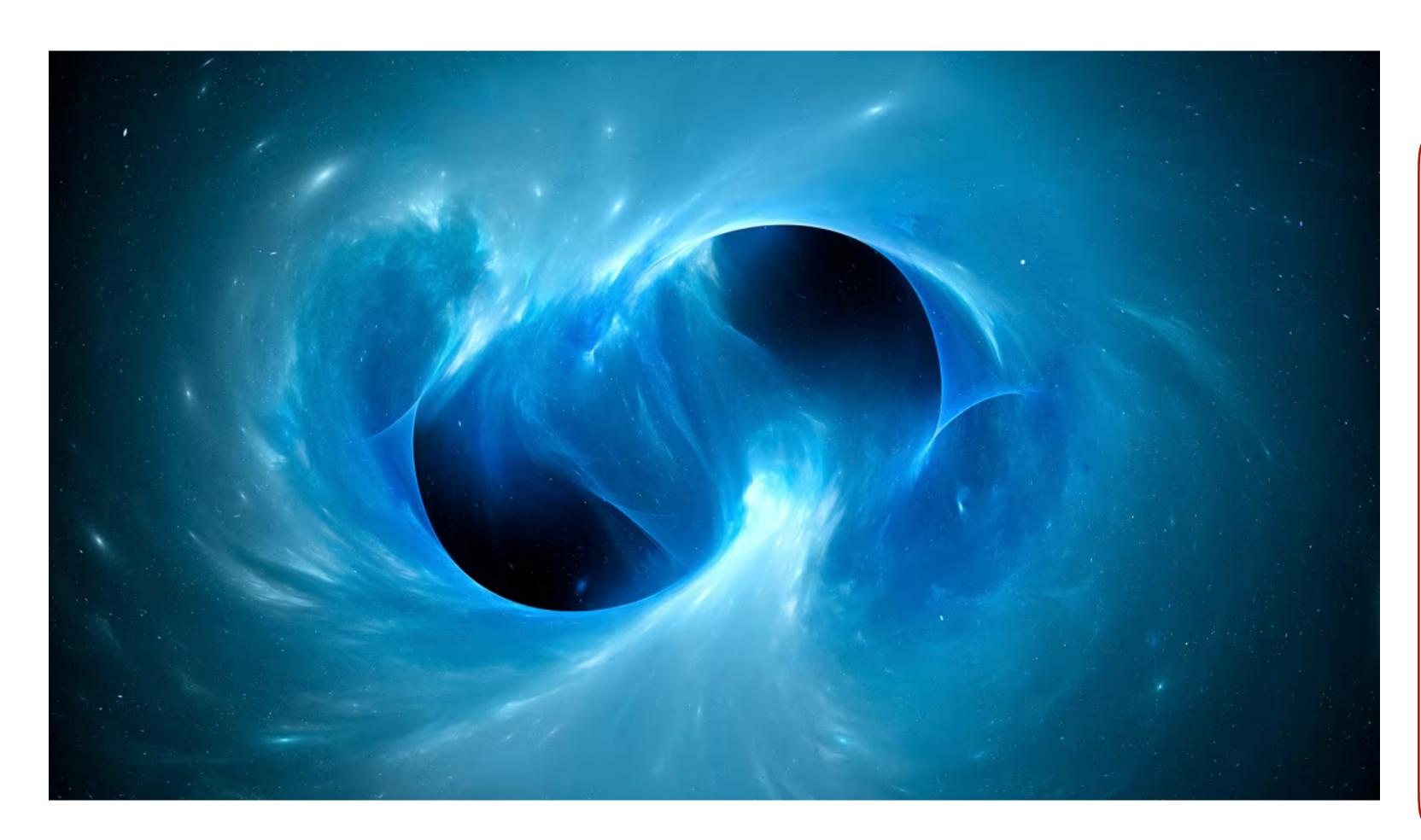


By computations <u>outside</u>
the black hole,
Hawking obtained
the black hole entropy

$$S = \frac{Ac^3}{4G\hbar}$$

where A is area of the black hole horizon.

All other systems have entropy proportional to their volume.



$$au_{
m ring-down} \sim rac{m}{k_B T}$$

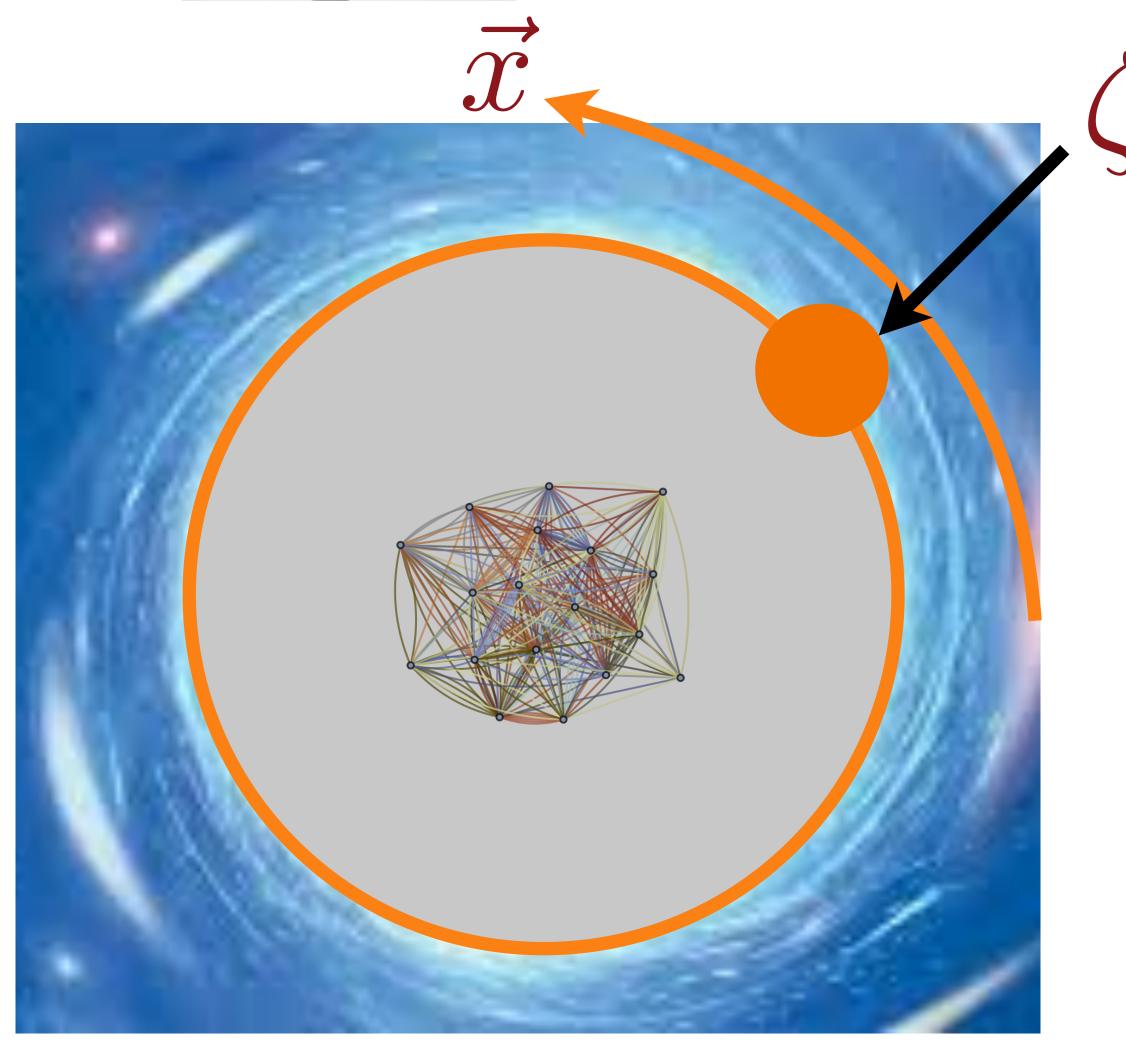
Planckian dynamics!

T is the Hawking temperature of the black hole

Sakkmesterke/Science Photo Library RF/Getty Images

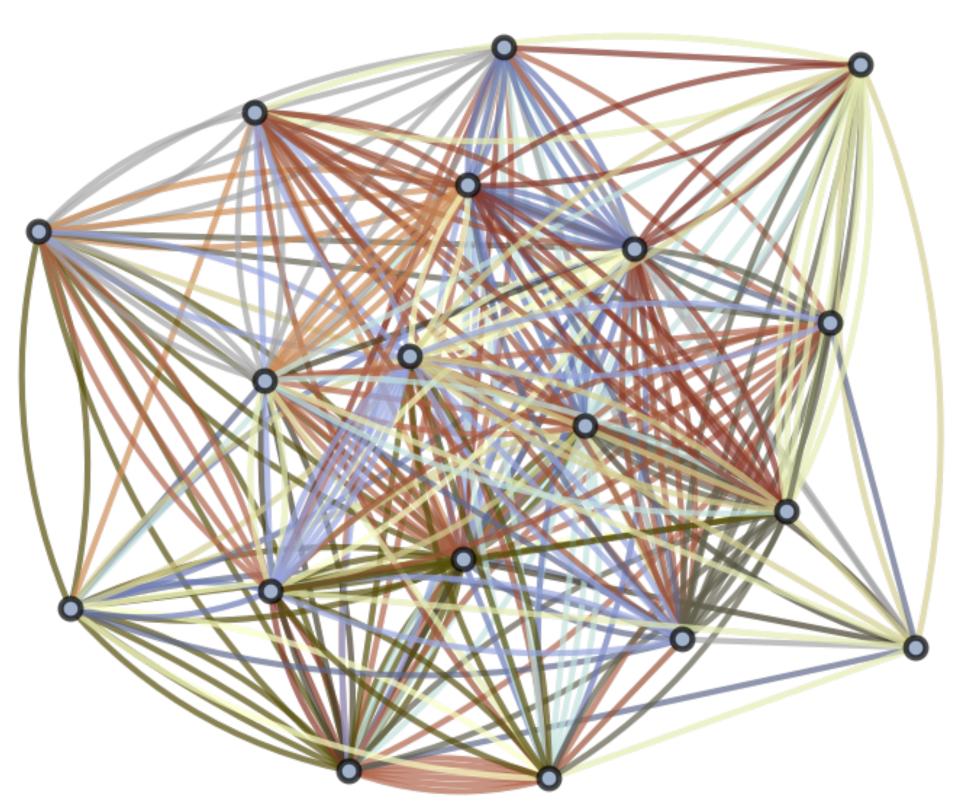


Maxwell's electromagnetism and Einstein's general relativity allow black hole solutions with a net charge

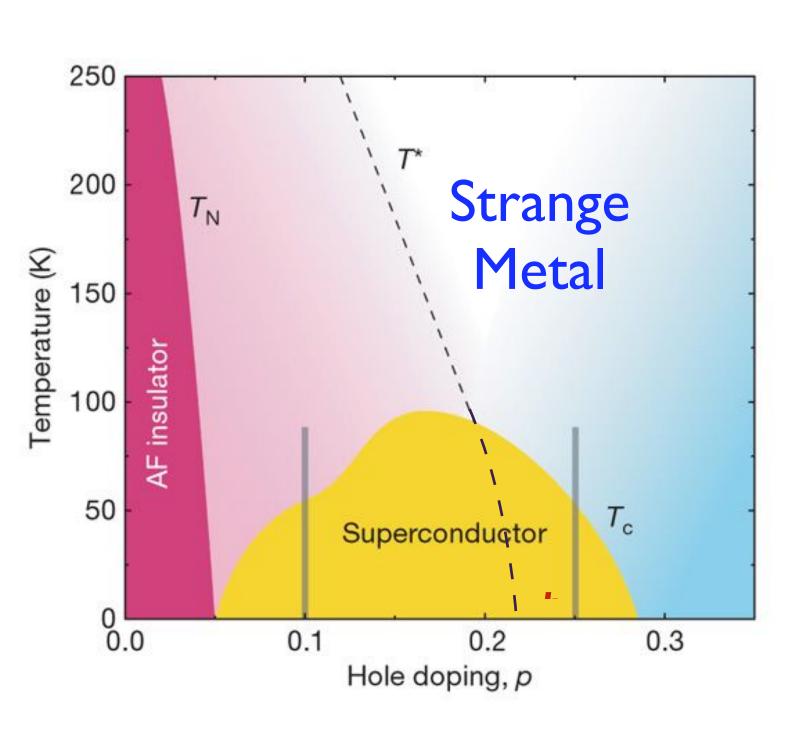


The quantum versions of Maxwell's and Einstein's equations in ζ space and time are also the equations describing electron entanglement in the SYK model!

The SYK model describes multi-particle quantum entanglement resulting in the loss of identity of the particles



The SYK model describes multi-particle quantum entanglement resulting in the loss of identity of the particles



In one set of variables, it helps describe the *strange* electrical properties of YBCO

Sachdev, Ye (1993)

The SYK model describes multi-particle quantum entanglement resulting in the loss of identity of the particles

In one set of variables, it helps describe the *strange* electrical properties of YBCO

Sachdev, Ye (1993)



The SYK model describes multi-particle quantum entanglement resulting in the loss of identity of the particles

